## Error Growth Dynamics within Convection-Allowing Ensemble Forecasts over Central U.S. **Regions for Days of Active Convection**

XIAORAN ZHUANG,<sup>a,b,c</sup> MING XUE,<sup>b,c</sup> JINZHONG MIN,<sup>d</sup> ZHIMING KANG,<sup>a</sup> NAIGENG WU,<sup>d,e</sup> AND FANYOU KONG<sup>c</sup>

<sup>a</sup> Jiangsu Meteorological Observatory, Jiangsu Meteorological Bureau, Nanjing, China <sup>b</sup> Center for Analysis and Prediction of Storms, University of Oklahoma, Norman, Oklahoma

 $^{\circ}$  School of Meteorogy, University of Oklahoma, Norman, Oklahoma

<sup>d</sup> Collaborative Innovation Center on Forecast and Evaluation of Meteorological Disasters, Key Laboratory of

Meteorological Disaster of Education, Nanjing University of Information Science and Technology, Nanjing, China

<sup>e</sup> Key Laboratory of Regional Numerical Weather Prediction, Institute of Tropical and Marine Meteorology,

China Meteorological Administration, Guangzhou, China

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ABSTRACT: Error growth is investigated based on convection-allowing ensemble forecasts starting from 0000 UTC for 13 active convection events over central to eastern U.S. regions from spring 2018. The analysis domain is divided into the northwest (NW), northeast (NE), southeast (SE), and southwest (SW) quadrants (subregions). Total difference energy and its decompositions are used to measure and analyze error growth at and across scales. Special attention is paid to the dominant types of convection with respect to their forcing mechanisms in the four subregions and the associated difference in precipitation diurnal cycles. The discussions on the average behaviors of error growth in each region are supplemented by four representative cases. Results show that the meso- $\gamma$ -scale error growth is directly linked to precipitation diurnal cycle while meso- $\alpha$ -scale error growth has a strong link to large-scale forcing. Upscale error growth is evident in all regions/cases but up-amplitude growth within its own scale plays different roles in different regions/cases. When large-scale flow is important (as in the NE region), precipitation is strongly modulated by the large-scale forcing and becomes more organized with time, and upscale transfer of forecast error is stronger. On the other hand, when local instability plays more dominant roles (as in the SE region), precipitation is overall less organized and has the weakest diurnal variations. Its associated errors at the  $\gamma$  and  $\beta$  scale can reach their peaks sooner and meso- $\alpha$ -scale error tends to rely more on growth of error with its own scale. Small-scale forecast errors are directly impacted by convective activities and have a short response time to convection while increasingly larger-scale errors have longer response times and delayed phase within the diurnal cycle.

KEYWORDS: Ensembles; Numerical weather prediction/forecasting; Convection; Forcing

### 1. Introduction

Convective events frequently occur over central United States in the spring season and the associated flooding can produce significant threats to life and properties (Ashley and Ashley 2008). Recent studies revealed that convection-allowing numerical prediction models have advantages over coarserresolution models in representing convective modes and diurnal cycle of precipitation (e.g., Clark et al. 2007), but the forecast skill does not always improve as model resolution increases (Lean et al. 2008; Mass et al. 2002; Walser et al. 2004). On the other hand, forecast skill often decreases fast with forecast range due to rapid forecast error growth (Kain et al. 2010; Surcel et al. 2016). These issues speak to the need for better understanding the predictability of convective events, and associated error growth across scales (Sun and Zhang 2016; Zhuang et al. 2020).

Understanding forecast error growth is a fundamental issue within the realm of predictability (Fritsch and Carbone 2004; Hohenegger and Schär 2007b; Johnson et al. 2013; Kong et al. 2006), and related research issues include the growth of errors at different scales and their interactions (Bachmann et al. 2019; Bierdel et al. 2017), and the predictability limitation estimation

Corresponding author: Ming Xue, mxue@ou.edu

(Judt et al. 2016; Walser et al. 2004). Through the study of error growth dynamics within a highly idealized model, Lorenz (1969) revealed important scale interactions pertaining to atmospheric predictability. Studies in more realistic settings have shown that very small amplitude and small-scale initial errors can grow upscale and contaminate mesoscale and large-scale processes (Hohenegger et al. 2006; Tan et al. 2004; Zhang et al. 2003). Zhang et al. (2007) proposed a three-stage error growth conceptual model using an idealized baroclinic wave model. This conceptual model suggests that the intrinsic predictability at larger scales is limited by upscale transfer of smaller scale errors: Stage 1 encompasses fast increase and an early saturation of small-scale errors that are confined to precipitation regions in presence of convective instability and latent heat release; Stage 2 corresponds to the transition stage when smallscale errors begin to spread from the precipitation regions and project to balanced motions through geostrophic adjustment processes (Bierdel et al. 2017). After that, errors continue to grow through background baroclinic instability at a slower rate in Stage 3. The model has been subsequently applied to investigating and explaining error growth dynamics in both idealized and more realistic modeling studies (Selz and Craig 2015; Sun and Zhang 2016; Zhang 2019). On the contrary, initial errors at larger scales have been reported by other authors to account for much of the error growth and for controlling forecast accuracy

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regardless of the presence of small scale errors (Durran and Gingrich 2014; Durran and Weyn 2015; Weyn and Durran 2017, 2018, 2019).

Another important question concerning error growth is what mechanism determines the diurnal aspect of error growth (Keil et al. 2014; Klasa et al. 2019; Nielsen and Schumacher 2016; Wu et al. 2020; Zhang et al. 2007). In general, the baroclinic instability associated with horizontal temperature gradients and the convective instability associated with unstable vertical profiles for moist convection are considered as the two main driving mechanisms for forecast error growth at the large and small scales, respectively (Bei and Zhang 2014; Nielsen and Schumacher 2016; Zhang et al. 2007). Zhang et al. (2007) found that moist convection is not only important in initiating error, but also in maintaining subsequent error growth at small scales. Weyn and Durran (2017) showed that the forecast error also exhibits up-amplitude growth in addition to upscale growth. Nielsen and Schumacher (2016) concluded that the forecast error evolution can be decomposed into a steadily growing mode that determines the amplitude increase, and a superimposed mode dominated by strong moist convection activities (e.g., those associated with solar-forced diurnal precipitation peak) that determine the "shape" of error growth curve. However, since convective events are inherently scale sensitive, it is important to understand characteristics of error growth across scales.

Previous studies also reported that the predictability of convective events depends on the impact of large-scale forcing on convection, and the convective events are often categorized into different regimes, namely, those that are strongly forced and weakly forced. As reported by Keil et al. (2014), in case of strongly forced convection, large-scale flow dominates error growth, while for weakly forced convection controlled by local instabilities the contributions from both sources are approximately equal. Nielsen and Schumacher (2016) also found that in a case with strong convective to synoptic-scale interactions the forecast error can continuously increase. By investigating error evolution under different convective regimes, Klasa et al. (2019) also indicated through case studies that large-scale flow and diurnal solar forcing together determine the overall evolution of error growth.

During the spring of the central U.S. regions, convective systems are often active with multiscale interactions (Carbone and Tuttle 2008; Carbone et al. 2002b; Dai et al. 1999; Knievel et al. 2004; Surcel et al. 2010; Trier et al. 2006); it is common for initially more isolated storm cells to organize into mesoscale convective systems (MCSs) in the region. In this study, we investigate scale-dependent error growth for 13 convective events during May 2018 with convection-allowing model (CAM) ensemble forecasts at 3-km grid spacing covering the contiguous United States (CONUS). The large convectionallowing grid allows for the representation of scales from meso- $\gamma$  through meso- $\alpha$  scales. We will focus on the forecast error analyses in a domain that covers the Central Plains east of the Rockies through the Midwest and much of the southeast regions, sampling convection of different types. The study period spans early spring (when large-scale forcing is more prevalent) to late spring (when locally forced convection is more prevalent) (Surcel et al. 2016, 2017), allowing for a diverse collection of different convection types and forcing mechanisms that regulate error growth dynamics within CAM forecasts. We use the total difference energy within the forecast ensemble and the scale decompositions of the difference energy as the proxy to measure error growth at and across scales. So far, studies examining growth of errors across scales and within their scales with large continent-sized CAM models, and how the error growth depends on the type of convection and the degree of synoptic scale forcing are few and limited (e.g., Surcel et al. 2016, 2017), and some of the existing studies are based on individual case studies (e.g., Flack et al. 2017; Wapler et al. 2015). More studies on these issues are needed.

As the main goals, this study is to answer the following questions: 1) What are the general characteristics of precipitation and associated error growth with respect to different convection types and forcing mechanisms; 2) What are the characteristics of error growth in terms of different spatial scales and in regions dominated by different convection types; 3) What mechanisms dominate the diurnal evolution of forecast error. These goals provide insights into the predictability of convective events across the central U.S. regions within CAM forecasts, and potentially aid the optimal design of CAM ensemble forecast systems and provide guidance to ensemble data assimilation and forecast model improvement. For example, a better understanding of the relative impact of initial condition perturbations at different scales on ensemble variances across the scales within the forecasts of different ranges, and how the impact depends on weather regimes can provide guidance on where attention should be focused when creating initial condition perturbations for CAM ensemble forecasting systems of limited size and the best method to use for creating such perturbations

The rest of this study is organized as follows. The datasets employed in this study are introduced in section 2. Section 3 to section 5 discuss the general characteristics of precipitation systems and error growth, and the error growth mechanisms, and section 6 discusses four specific cases in more detail. Conclusions and further discussions are given in section 7.

#### 2. Data and methods

### a. Forecasts from the CAPS HWT Spring Forecast Experiment ensemble

The Spring Forecast Experiments have been organized by the NOAA Hazardous Weather Testbed (HWT, http:// hwt.nssl.noaa.gov/spring\_experiment) every spring since 2007, and the Center for the Analysis and Prediction of Storms (CAPS) has been contributing the largest number of CAM ensemble forecasts every year until recently (e.g., Clark et al. 2009, 2018; Xue et al. 2007). In 2018, most ensemble forecasts produced by CAPS used the Advanced version of the Weather Research and Forecasting (WRF-ARW) Model (Skamarock et al. 2008). Similar to experiments described in Clark et al. (2018) for 2016 forecast experiments, the CAPS CAM ensemble forecasts of 2018 included several sets, one included initial



FIG. 1. The forecast model domain with terrain height in shading. The red rectangle corresponds to the analysis domain that is divided into four equal-sized quadrants or subregions used in our analyses.

condition (IC)/lateral boundary condition (LBC) perturbations as well as different physics parameterizations, and one included IC and LBC perturbations only (i.e., all members used the same physics). The third set used stochastic perturbations based on a single suite of physics instead of multiple physics. In this study, the set using the same physics is used given our focus on IC error growth. The physics package includes the Thompson microphysics (Thompson et al. 2008), Noah land surface model (Mitchell 2005), and MYJ planetary boundary layer (Janić 2001) scheme. The Stage-IV precipitation product (Lin and Mitchell 2005) is employed as the observed precipitation data for verification purpose and we focus on the first 24 h of the forecast.

The IC of the control member of ensemble was produced by assimilating radar (reflectivity and velocity) and conventional (surface observations and radiosondes) data using the ARPS 3DVar data assimilation system (Xue et al. 2003) together with its cloud analysis package (Hu et al. 2006a,b), using the 0000 UTC 12-km North American Mesoscale Forecast System (NAM) model analysis at the background. The 3-hourly NAM forecasts are used as the LBCs. The perturbed ICs and LBCs for other ensemble members are generated by adding perturbations derived from the 2100 UTC cycle forecasts of the operational short-range ensemble forecast (SREF) system of NCEP (Du et al. 2009) to the IC and LBC of the control member. All forecasts are initialized at 0000 UTC (1800 CST) on weekdays with a forecast range to 60 h, on the 3-km grid spacing CONUS grid (see Fig. 1). Previous studies on similarly configured forecasts produced by CAPS have reported that diurnal cycles of precipitation over central U.S. regions can be reasonably reproduced by the forecasts (Berenguer et al. 2012; Surcel et al. 2010, 2016, 2017). The radar data assimilation significantly alleviates the precipitation spinup problem (Kain et al. 2010). The 24-h forecasts from 13 days of the CAPS ensemble forecasts from May 2018 that have active convection starting at the initial condition time (0000 UTC) are chosen to analyze IC error growth in this study.

### b. Representation of forecast error

Following Nielsen and Schumacher (2016), the root mean difference total energy (RMDTE) is used to represent forecast

error, in which the horizontal DTE (Zhang et al. 2003) as a function of the grid point and time can be defined as

$$DTE(\lambda)_{i,j,i} = \frac{1}{N} \sum_{n=1}^{N} \sum_{k=0}^{K} \frac{p(k+1) - p(k)}{p(0)} \frac{1}{2} \\ \times \left\{ u(\lambda)' + v(\lambda)' + \frac{C_p}{T_r} \left[ T(\lambda)' \right]^2 \right\}, \qquad (1)$$

where u', v', and T' are, respectively, the differences of zonal wind, meridional wind, and temperature from the ensemble mean. The term  $C_p = 1004.9 \text{ J kg}^{-1} \text{ K}^{-1}$  is the heat capacity of dry air at constant pressure and  $T_r = 270 \text{ K}$  is a reference temperature. The variable N is the number of ensemble members, and the subscripts i, j, k, t, n, and  $\lambda$  represent the grid indices in x, y, and vertical directions, forecast time level, ensemble member, and spatial scale, respectively. The k index covers vertical layers from 925 to 500 hPa where most precipitation systems occur; p denotes the pressure of each vertical layer.

Since RMDTE values vary significantly across the convective events, we use the normalized RMDTE (NRMDTE) to reduce variations across convective events following Nielsen and Schumacher (2016). The NRMDTE is defined as the ratio of RMDTE to total mean kinetic energy (TMKE), and TMKE is given as

$$\text{TMKE}_{i,j,t} = \sum_{k=0}^{K} \frac{p(k+1) - p(k)}{p(0)} \bigg[ \frac{1}{N} \sum_{n=1}^{N} \frac{1}{2} (\overline{u}_{i,j,k,t,n}^2 + \overline{v}_{i,j,k,t,n}^2) \bigg],$$
(2)

where the overbar denotes the ensemble mean. Then NRMDTE can be computed

NRMDTE(
$$\lambda$$
)<sub>*i,j,t*</sub> =  $\sqrt{\frac{\text{DTE}(\lambda)_{i,j,t}}{\text{TMKE}_{i,j,t}}}$ . (3)

In Eq. (2), the temperature term is excluded from Eq. (1) to allow the TMKE to dominantly vary with the convective situation in question rather than with latitudinal variation in temperature (Nielsen and Schumacher 2016). Based on the above, the evolution of forecast error (as measured in a form of ensemble perturbations) can be quantitatively assessed by calculating NRMDTE over time, which can also be used to measure practical predictability. In general, the predictability within ensemble forecasts for a convective case is destroyed when there is large increase in NRMDTE (Judt et al. 2016). In summary, RMDTE provides a measure of the magnitude of forecast errors and is applicable to individual cases while NRMDTE does not measure the absolute magnitude but assesses the mean behaviors of forecast error growth for a group of cases and informs predictability. In section 3, we employ NRMDTE to understand the mean error growth dynamics over all 13 cases, while in sections 5 and 6, RMDTE is used for correlation analysis and case studies.

### c. Analysis domain and case selection

The analyses of the CAM forecasts and observations are carried out over the central U.S. region with four subregions as illustrated in Fig. 1. The overall analysis region is between the Rocky Mountains and Appalachian Mountains, which is



FIG. 2. The convective available potential energy (CAPE) averaged over the entire analysis domain with rainfall higher than  $0.5 \text{ mm h}^{-1}$  as a function of forecast lead time for each case indicated in the legend.

further divided into four quadrants with equal size to allow for examination of precipitation diversity in the northwest (NW), northeast (NE), southeast (SE), and southwest (SW) regions. The 24-h forecasts from 13 days of May 2018 that have active convection at the IC time are chosen from the CAPS ensemble forecasts to analyze IC error growth in this study (see Fig. 2 for a list of dates). All forecasts start at 0000 UTC. With radar data assimilated into the ICs containing active convection, errors at all scales are expected to grow from the beginning.

## **3.** The general characteristics of precipitation systems in the forecasts

#### a. Mean synoptic overview

Figure 2 gives the temporal evolution of convective available potential energy (CAPE) computed from the control forecast averaged over the entire analysis domain for each of the 13 cases. The CAPE values show clear diurnal cycles with steep increases after 12 h (0600 CST) due to daytime solar heating and they reach maximum at around 20 h (1400 LST). Specifically, cases during late May show more pronounced diurnal variations and higher CAPE values than early May cases. This is consistent with previous studies (Dai et al. 1999; Surcel et al. 2016), in which early spring CAPE is affected more by large scale circulations while late spring CAPE is more controlled by diurnal cycle due to solar heating. In the horizontal plane view (Fig. 3), the CAPE averaged over all cases is mainly concentrated in the southern part of the analysis domain that is associated with a strong mean 925-hPa low-level jet (LLJ) originated from the Gulf coast. Diurnal characteristics consistent with the boundary layer LLJs predicted by the inertial oscillation theory of Blackadar (1957) are found with the LLJ; it strengthens during the nocturnal time (Figs. 3a-d) and weakens during the day with the development of boundary layer vertical mixing (Figs. 3e-h). The enhanced nocturnal LLJ transports more moisture into the central Great Plains and also produces low-level convergence at its northern terminus that promotes organized convection (Carbone and Tuttle 2008; Trier et al. 2017).

### b. Classification of precipitation types

Figure 4 displays the spatial distributions of total frequency (number of times across the 13 days) of 1-h precipitation exceeding  $0.5 \text{ mm h}^{-1}$  with different ending times. In general, there are four primary modes of precipitation that are linked to different forcing mechanisms over the analysis domain. The main precipitation in the NW quadrant is found near the western boundary of the region at 0300 and 0600 UTC (Figs. 4a,b), which is mostly from convective systems that originated in the afternoon over the Rocky Range in central Colorado and moved eastward into the region (Carbone et al. 2002a; Sun et al. 2016; Surcel et al. 2010). By 0900 and 1200 UTC (Figs. 4c,d), the precipitation is mainly found in central and eastern Nebraska, along a zone that extends eastward into the NE quadrant. This zone is associated with a quasistationary front that forms between the generally southerly flows from the Gulf and the higher latitude air mass (see Fig. 3). The zone is also the northern terminus of the boundary layer LLJ where low level convergence is strong and prone to trigger night time convection when the LLJ jet is enhanced (Savijärvi 1991; Trier et al. 2017). The precipitation in Nebraska between 0600 and 1200 UTC should be the combined result of eastward propagation of afternoon convection from the Rockies and those that develop at the northern terminus of the nocturnal LLJ. The convection in the northern part of the NE quadrant is mainly found at the quasi-stationary front, and it weakens by 1500 UTC (Fig. 4e) and mostly disappears by 1800 UTC or close to noon local time. The latter should be related to the weakening of the southerly flows associated with the boundary layer LLJ as daytime boundary layer mixing slows down the flows (Blackadar 1957; Xue et al. 2018). The quasi-stationary front is in a sense analogous to the mei-yu front found over eastern Asia in late spring to early summer (Chen et al. 2018).

In the southern quadrants, the direct effects of the diurnal changes in solar heating are strong, and convection tends to be strongest in the afternoon into early evening. In the SW quadrant (Fig. 4e), precipitation is most prominent in the Texas panhandle region in a north-south zone that is associated with a quasistationary dryline that frequently triggers convection in the late afternoon in the spring (Liu and Xue 2008; Schaefer 1986; Xue and Martin 2006). The convective storms initiated along the dryline often move eastward across the southern Great Plains and organize into quasi-linear convective systems or squall lines in the process. In the SE quadrant, we observe mostly small-scale and scattered popcorn-type convection in the daytime, especially in the afternoon and early evening (Figs. 4a,g,h), some along the Gulf Coast. These cells form due to solar heating and associated land/see-breeze circulations (Berenguer et al. 2012; Surcel et al. 2010). Given that the precipitation in the four quadrants or subregions appears to be dominated by convective systems of mostly different origins and forcing mechanisms, many of our subsequent discussions will be focused on the four subregions, and we will investigate and contrast the precipitation diurnal cycles and associated characteristics of error growth for the respective regions.

### c. Mean diurnal cycles of precipitation

Figure 5 shows the subdomain-averaged hourly precipitation over 24 h for the 13 forecasts and their mean, and the



FIG. 3. Ensemble mean CAPE (shaded) and 925-hPa horizontal wind vectors, from (a) 0000 UTC to (h) 2100 UTC, every 3 h averaged over all 13 cases.

corresponding observations. The observed precipitation rates show different diurnal features for different subregions. As discussed earlier, in the NW region that is mainly affected by propagating convective systems coming from the Rockies and somewhat by convection forced by the nocturnal LLJ, the peak precipitation is found around 0000 UTC (1800 CST, Fig. 5a). The rate decreases steadily into the evening and reaches minimum at around 1600 UTC (1000 CST). The precipitation starts



FIG. 4. Spatial distribution of 3-h accumulated precipitation frequency maps with precipitation rate exceeding 0.5 mm h<sup>-1</sup> at different ending times: (a) 0300, (b) 0600, (c) 0900, (d) 1200, (e) 1500, (f) 1800, (g) 2100, and (h) 2400 UTC.



FIG. 5. Time evolution of region-averaged forecast and observed precipitation for the (a) NW, (b) NE, (c) SW, and (d) SE subregions. The color solid lines are for the individual cases for each subregion (with the color legend shown in Fig. 2), the black dashed line for the average of all cases, and the solid line is for observation.

to pick up significantly in early afternoon (~2000 UTC or 1400 CST) and increase to the second day peak at 0000 UTC. In the NE region (Fig. 5b), the precipitation peaks at 0600 UTC or around midnight, consistent with the fact that the nocturnal LLJ forcing plays the largest role in that region in this season (Dai et al. 1999). The minimum is around 1700 UTC. For the SW region, precipitation mostly occurs in the local afternoon after 1700 UTC (1200 EST) and before 0200 UTC, and the maximum occurs at around 2100 UTC, due to the predominant effect of solar heating (Fig. 5d). For the SW region, precipitation peaks around 0000 UTC or 1800 CST, due to frequent initiation of convection along the dryline in western Texas in late afternoon, and subsequent eastward propagation. These observed diurnal characteristics are reasonably well reproduced by the model (cf. black dashed and solid lines in Fig. 5) although there are magnitude errors. For the individual cases, several of them had rather weak precipitation throughout the 24 h. For those that have significant amount of precipitation, the general diurnal trends mostly match the mean observation. The cases with more precipitation are often associated with favorable synoptic scale flow patterns and related forcing.

Overall, the northern regions tend to be more affected by synoptic scale circulations (cyclones) in May (especially for the NE region), and at the low levels by convergence induced by nighttime LLJ. For the southern regions, synoptic scale forcing tends to be weaker, and boundary layer thermal forcing dominates, especially in the SE region. In the SW region, dryline dynamics play additional roles. The fact that the mean precipitation diurnal cycles are reproduced reasonably well in the model suggest that the forecasts can be used to investigate diurnal cycle-dependent forecast error growth. It is noted that the time-averaged forecast precipitation rates in the



FIG. 6. Hovmöller diagrams (latitudinal averaged, time-longitude) for NRMDTE (shaded) and precipitation (contours) for (a) the northern subdomains and (b) southern subdomains, averaged over all 13 cases.

subdomains all show significant precipitation (NW: 0.23, NE: 0.25, SW: 0.15, SE: 0.21 mm  $h^{-1}$ ).

### 4. Characteristics of error growth in forecasts

### a. Spatiotemporal characteristics of total error growth

Previous studies have revealed a strong relationship between error (energy) growth and precipitation (Flack et al. 2017; Johnson et al. 2013; Nielsen and Schumacher 2016; Wu et al. 2020). Given the strong zonal propagation of convection (Surcel et al. 2010 and Fig. 4), we first analyze the mean error growth and associated precipitation rate in time–longitude coordinates in terms of Hovmöller diagrams (for the northern and southern half of the domain with averaging over the latitudinal range of the half domains). Figure 6 shows the time– longitude Hovmöller diagrams of the total NRMDTE and corresponding precipitation rates averaged over all 13 cases, plotted for the northern (Fig. 6a) and southern half of the overall domain (Fig. 6b).

In the northern half domain (combination of NW and NE subdomains), the total NRMDTE corresponds well with the two progressive precipitation systems (Fig. 6a): the orographically forced precipitation systems coming out the Rockies in the afternoon propagating through the NW region (indicated by the long gray arrow labeled NW) and the nocturnally forced precipitation systems forming in the northcentral part along the quasi-stationary front that propagate eastward and dissipate in the morning hours in the NE subdomain (the gray arrow labeled NE, and see also Figs. 4a-d). West of 100°W, the NRMDTE grows quickly, reaching over 0.3 after  $\sim 3h$  (Fig. 6a), the region of large NRMDTE spreads downstream in a fan pattern, with the largest values more or less tracking the maximum precipitation "ridge" in the Hovmöller diagram while lagging in time in terms of the "ridge line" by a couple of hours. Corresponding to the precipitation initiated along the quasi-stationary front near and east of 96°W and sustaining through the night while propagating eastward (along the arrow labeled NE), errors develop more or less following the precipitation track in the Hovmöller diagram and expand in east-west extent. The two regions of NRMDTE > 0.31 (red shadings) merge together after 10 h, and occupy the zone between 88° and 104°W through 24 h, with the expanding region of high NRMDTE (gray color) being mostly associated with western propagating band of precipitation. These results clearly show that the NRMDTE growth is strongly tied to the development and decay, and propagation of convective systems which exhibit clear diurnal cycles. For the eastern band, NRMDTE decreases after 16 h when the precipitation intensity decreases in the late morning hours. The western band has larger NRMDTE values, indicating greater uncertainties and lower predictability with these precipitation systems in the NW domain.

For the southern part of the overall domain (Fig. 6b), there are clearly two branches of larger NRMDTE values, corresponding to the eastward propagating dryline-initiated precipitation systems in the SW region and the local thermally forced precipitation systems in the SE region. The NRMDTE associated with the thermally forced convection in SE clearly develops much faster and the gray color fills much of the domain after 10h, indicating low predictability with such oftendisorganized thermal convection that is mainly active in the afternoon through midnight hours. The error remains larger in the morning hours though, indicating the effects of widespread afternoon convection that also cause upscale error growth (Hohenegger et al. 2006). In comparison, errors associated with the convection in the SW region grow much slower and gain lower values; this may be partly because the drylineinitiated convection tends to become organized when they propagate through the southern Great Plains, where the boundary layer tends to be capped by an inversion layer to prevent widespread convection. The decay of convection from late morning also limited further error growth (Fig. 6b).

The above results indicate that forecast error growth within a CAM ensemble often closely follows the precipitation systems and the errors tend to grow upscale from the



FIG. 7. Time evolution of NRMDTE at different scales: (a) total, (b) meso  $\gamma$ , (c) meso  $\beta$ , and (d) meso  $\alpha$ , for the entire (black) and four subregions (color lines).

precipitation regions, and the behaviors of error growth are highly dependent on the characteristics of the precipitation systems, including their primary forcing mechanism, propagation and organization.

Figure 7a shows the temporal evolution of total NRMDTE averaged over all 13 cases for the entire analysis domain and each of the subdomains, respectively. Diurnal variations in the NRMDTE over the entire domain (black dashed curve) similar to that found in Nielsen and Schumacher (2016) are observed, with growth mainly found in the first ~12 h and last ~5 h of the 24-h forecasts, corresponding to the evening through early morning hours, and the afternoon hours. NRMDTE remains level after sunrise through noon due to suppression of much of the convection. The total NRMDTEs for different subregions exhibit different magnitudes and trends. The NRMDTE for the SE region is the largest from the beginning (indicating larger uncertainties in its IC) and continues to grow throughout

the 24 h, and grows the fastest in the afternoon and early evening, not surprisingly. The NRMDTE in the NW region is the second largest, and goes through growth, decay and growth cycles, with the decay between 1000 and 1400 CST being the most evident. Given the faster error growth, the predictability of convection in these two regions is lower (Judt et al. 2016; Nielsen and Schumacher 2016). In comparison, convective systems in the SW and NE regions have lower errors and generally similar diurnal variations. These systems have higher predictability due to stronger control of synoptic and mesoscale environments that are associated with dryline and quasistationary frontal circulations, respectively.

# b. Spatiotemporal characteristics of error growth at different scales

To further understand the error growth dynamics, the NRMDTEs at and across different scales are assessed. The



FIG. 8. Hovmöller diagrams (latitudinal averaged, time–longitude) for the case-averaged NRMDTE (color) at different scales and precipitation (contours), (a),(d) meso  $\gamma$ ; (b),(e) meso  $\beta$ ; (c),(f) meso  $\alpha$  for the (top) northern and (bottom) southern regions. The ordinate indicates the forecast hour starting from 0000 UTC.

discrete cosine transform (DCT) (Denis et al. 2002; Surcel et al. 2014; Zhuang et al. 2020) is employed to decompose the dynamic variables into three scales, i.e., the meso- $\gamma$ , meso- $\beta$ , meso- $\alpha$  scales (the longest resolved wavelength for the analysis domain is 3720 km or twice the east–west width of the domain), with the dividing wavelengths being 20 and 200 km between them. In this paper, we refer to these scales as convective scale, mesoscale and, synoptic or large-scale, or as  $\gamma$ ,  $\beta$ , and  $\alpha$  scales for brevity. NRMDTEs are then calculated for these three scales.

As shown in Figs. 7b–d, the scale-dependent error growth for each subregion exhibits a "stepwise" feature, i.e., the NRMDTEs increase with increasing spatial scales at lagging times, reaching their peaks at successively later hours as the scale increases, indicative of upscale transfer of errors (Selz and Craig 2015; Zhang et al. 2007). At the first stage, the  $\gamma$ -scale NRMDTEs rapidly increase in the precipitation regions and reach peak between 2 (SE) and 5 h (NW) (Figs. 7b and 8a,d). The  $\gamma$ -scale errors at the initial time are very low because convection was introduced into the IC using the deterministic cloud analysis of radar observations (without convective scale perturbations) while the SREF-derived IC perturbations span only mesoscales and up (Johnson et al. 2013).

The errors at the  $\beta$ -scale increase rapidly in the first  $\sim 3$  h, then continue to grow through  $\sim 8$  h and spread beyond the precipitation regions (Figs. 7c and 8b,e); this may be partly attributed to the slower error growth at longer wavelengths (Lorenz 1969) and partly to the upscale transfer of errors from

 $\gamma$  scale (Selz and Craig 2015; Sun and Zhang 2016). After the peak error is reached, the error decreases noticeably in most of the subregions (Fig. 7c), and such decreases correspond closely to the weakening of precipitation as shown in the Hovmöller diagrams (Figs. 8b,e). The growth picks up again (Fig. 7c) when precipitation redevelops after 18 h (Figs. 8b,e), indicating the direct contribution of moist convection to mesoscale error growth, as emphasized by Zhang et al. (2007).

At the  $\alpha$  scale, the NRMDTE starts at relatively high levels, which comes from the initial perturbations derived from SREF 3-h forecasts. The NRMDTE at initial time is the highest in the SE subdomain mainly because the ensemble mean total energy used to do normalization is lower in this weakly forced region (see Fig. 14a later for an individual case for the region). Compared to other regions, the diurnal variations of precipitation in SE region are weaker and there is much less east–west propagation (Fig. 8f), and its NRMDTE is able to grow monotonically throughout the 24 h (green curve in Fig. 7d).

The  $\alpha$ -scale NRMDTE in other three subregions grows slowly in the first 3–4 h (Fig. 7d), then goes into a stage of fast growth before levelling off at 10–12 h. The NRMDTE decreases somewhat afterward then starts to grow again at 20 h (Fig. 7d) when precipitation redevelops again in the afternoon (Fig. 8f). The apparent connection of  $\alpha$ -scale NRMDTE to the diurnal cycles of precipitation, and the delayed phase of error growth compared to those at  $\gamma$  and  $\beta$  scales clearly indicates significant upscale error growth feeding off moist convection in these regions.



FIG. 9. Scatterplots of the normalized RMDTE at different scales (a) meso  $\gamma$ , (b) meso  $\beta$ , and (c) meso  $\alpha$  vs normalized precipitation (>0.5 mmh<sup>-1</sup>) at different lead times (see legend for corresponding colors).

Overall, similar to the precipitation rate (Fig. 5), errors in the  $\gamma$  scales (Fig. 7b) exhibit pronounced diurnal cycles given their direct link and fast response to convective activities. The errors at these scales usually decay when convection die out. For errors at the  $\beta$  and  $\alpha$  scales, the diurnal responses are weaker and the peaks are delayed, due to their slower growth. Given the clear importance of precipitation or moist convection, and based on the sequence of error growth in terms of the timing of peak error, as well as the time evolution of the spatial scales of errors in the Hovmöller diagrams, we think there is clearly upscale error growth from the convective  $(\gamma)$  scale through the mesoscale ( $\beta$  scale) and synoptic ( $\alpha$ ) scale. At the same time, because of the presence of significant large scale errors in the IC, effects of large scale errors on the smaller scales are also at work (Durran and Gingrich 2014; Weyn and Durran 2019); in fact, the storms initialized from radar data are the same within the ICs of all ensemble members (cf. curves in Fig. 7b). Therefore, the error growth model in our situation appears to be: IC errors at the mesoscale and synoptic scale grow in the ensemble and create errors at the convective scale that grow the fastest. The fast-growing convective scale errors then propagate upscale. The precipitation activities strongly modulate error growth at all scales, resulting in significant diurnal cycles of error dynamics, which are also affected by the precipitation regimes (Durran and Gingrich 2014; Weyn and Durran 2019). The upscale error propagation is the weakest in weakly forced situations. These are discussed further in the next section.

# 5. Effects of convection intensity and large-scale forcing on forecast error

Since error growth within CAM forecasts depends on the type of convective system or precipitation type (Keil et al. 2014; Klasa et al. 2019; Nielsen and Schumacher 2016), in this

section, we evaluate the impact of precipitation type on error growth with respect to the spatial scale and forecast range via a correlation analysis.

# a. Relation between moist convection intensity and forecast error

The intensity of moist convection has been reported to dominate error growth at small scales during first few forecast hours in precipitation regions (Figs. 7b and 8a,d) (Hohenegger et al. 2006; Selz and Craig 2015; Zhang et al. 2007; Zhang 2019). However, the impact of moist convection intensity on error growth at longer forecast ranges, especially with different precipitation diurnal cycles, is less clear. In this subsection, the area-average precipitation rate exceeding  $0.5 \text{ mm h}^{-1}$  is used as an indicator of the intensity of moist convection, RMDTE is used to represent error growth, and their relationship is evaluated with a linear regression method.

Figure 9 shows the scatterplots between RMDTE and moist convection intensity (both variables are normalized prior to calculating the regression coefficient (Reynolds et al. 2002)) at different scales and over different subregions. Different colors are used to represent different forecast periods based on consideration of the stages of error growth and the diurnal variability of precipitation and errors at different scales: 1) the black dots represent period 1 (0-9 h, 1800-0300 LST), encompassing the fast increase of  $\gamma$ -scale errors and their associated saturation; 2) the cold color dots indicate period 2 (10-15 h, 0400-0900 LST), containing the increase and saturation of  $\beta$ -scale and  $\alpha$ -scale errors; and 3) the warm color dots indicate period 3 (16-24 h, 1000-1800 LST) in which secondary error growth occurs in the second day. Different cases are characterized by different markers. Lines in different colors represent the fitting lines for different periods using linear regression.

Overall, the correlation between forecast error magnitude and moist convection intensity increases with decreasing scales, strong positive correlations between them can be found at the  $\gamma$  scale in all three periods (Figs. 9a1–a4). In some regions (e.g., SW), the positive relationship is even stronger in period 3 (Figs. 9a4) when afternoon thermal convection is active (cf. Fig. 7b and 8d). In comparison, weak positive correlations or even negative correlations are observed at the  $\beta$  scale (Figs. 9b1–b4) and  $\alpha$  scale at shorter forecast ranges (Figs. 9c1– c4). The correlation coefficients are generally larger during periods 2 and 3 than that of period 1, even for the  $\gamma$  scale. This result implies that the impact of moist convection on error growth increases with forecast time, apparently due to the accumulative effects of moist convection on forecast error.

Specifically, for the NW, NE, and SW regions where mesoscale to large-scale forcing linked to the nocturnally strengthened LLJ during period 1 plays significant roles, the RMDTEs can be negatively correlated to the strength of moist convection at the larger scales (Figs. 9b1-b3, c1-c3), and the negative trend is stronger for the  $\alpha$  scale. Weaker negative correlations are also found for the SE region (Figs. 9b4, c4). Such negative correlation appears to be due to the delayed response of larger scale errors to moist convection so that the error growth is out of phase with the convection intensity time evolution. If we consider the  $\gamma$ -scale error shown in Fig. 7b as a proxy of moist convection intensity (because of the fast response to  $\gamma$ -scale error to moist convection), we can see that the  $\beta$ -scale (Fig. 7c) and  $\alpha$ -scale (Fig. 7d) errors are increasing throughout period 1 while the  $\gamma$ -scale errors are decreasing after 2–4 h (Fig. 7b). Such out-of-phase evolution is also evident in Fig. 8 when comparing the precipitation intensity and error growth in the first 9 h for the two larger scales.

In summary, moist convection impacts forecast error growth during the whole 24-h forecast range. The correlation between error growth and moist convection decreases with increasing spatial scale because of the increasing error response time to convection. The correlation increases with forecast hours due, we believe, to the accumulative effects of convection. For the initial 8 h of forecast, the correlation is actually negative for forecast errors at the  $\beta$  and  $\alpha$  scales; this is believed to be related to the phase difference between the errors at these scales and smaller scale convection.

# b. Relationship between large-scale forcing and forecast error

The impact of large-scale forcing on convection is often objectively assessed by the rate at which instability is removed by convection (Keil et al. 2014). Following Done et al. (2012, 2006) and Surcel et al. (2016), the convective adjustment time scale  $\tau_c$  is introduced

$$\tau_c = \frac{1}{2} \frac{C_p \rho_0 T_0}{L_v g} \frac{\text{CAPE}}{p_{\text{rate}}},\tag{4}$$

where  $C_p$  is the specific heat capacity of air at constant pressure,  $\rho_0$  and  $T_0$  are the reference density and temperature,  $L_v$  is the latent heat of vaporization, g is the acceleration of gravity, and  $p_{\text{rate}}$  is the precipitation rate. Prior to calculation, both CAPE and  $p_{\text{rate}}$  are spatially smoothed using a Gaussian method with a radius of 20 km and masked with a threshold of



FIG. 10. The convective adjustment time scale  $\tau_c$  averaged over the entire analysis domain with rainfall higher than 0.5 mm h<sup>-1</sup> as a function of forecast lead time for each case indicated in the legend.

 $0.5 \text{ mm h}^{-1}$  to avoid dry events. Lower  $\tau_c$  indicates a stronger degree of large-scale forcing and vice versa. In general, a threshold at the lower bounds of the 3–12-h range for  $\tau_c$  could be used to distinguish strongly forced events and weakly forced events (Zimmer et al. 2011), and in this study a threshold of 3 h is chosen (Keil et al. 2014). In reality, as discussed in Surcel et al. (2017), there can be events in which large areas of instability are consumed by convection that was initialized at the small scale and the errors grow upscale through e.g., organization of small storms into larger mesoscale systems. The readers should be aware of such caveats.

As shown in Fig. 10,  $\tau_c$  has a similar diurnal cycle as CAPE with lower nighttime value (stronger large-scale forcing) and higher daytime value (weaker large-scale forcing). Despite the typical use of  $\tau_c$  to distinguish precipitation situations, Keil et al. (2014) also suggested that  $\tau_c$  could be an indicator of forecast uncertainty. However, the relationship between  $\tau_c$  and forecast error across and at different spatial scales is still not clear.

Figure 11 shows the scatterplots between RMDTE and  $\tau_c$  at different scales and different subregions during different forecast periods. In general, the correlation coefficient is clearly dependent on the forecast period. For all regions, with the initial weakening of large-scale forcing (Fig. 10) with time (from nighttime to daytime), the correlation decreases correspondingly. Specifically, during period 1 which is from early evening through early morning, CAPE is relatively low, so that convection is more of forced type or large-scale forcing is relatively strong, we see clear negative correlation between error and  $\tau_c$ , especially at the two larger scales (Figs. 11b1–b4, c1–c4). The correlation at the  $\gamma$  scale is much weaker though still negative (Figs. 11a1-4). These results indicate that the presence of larger-scale forcing is favorable for the organization of convective cells into larger MCSs and for growth of errors at the two larger scales. They also suggest that the largescale flows have more control on error growth at larger scales, consistent with expectation.

For the longer forecast ranges in periods 2 and 3, the relationship between forecast error and forcing is less clear. For the two smaller scales, the correlation for period 2 is mostly



FIG. 11. As in Fig. 9, but for normalized RMDTE vs normalized convective adjustment time scale  $\tau_c$ .

negative or close to zero (for SW region), but is positive for the  $\alpha$  scale for all except NW region. This is the morning period when precipitation is weakest. In period 3 when convection becomes active again, the correlation becomes negative again for the two larger scales in all four regions (Figs. 11b1–4, c1–4). Therefore, the relationship between large-scale forcing and forecast error growth has diurnal variations, with connection to the precipitation diurnal cycle.

### 6. Case studies

In this section, four representative convective cases (A–D) primarily from the four subregions with different dominant types are selected to present the forecast error growth in a more intuitive manner. To simplify the description, the division of forecast range in section 5 is retained in this section.

### a. Case A: 18 May 2018

In the afternoon of 17 May 2018, convective storms formed over the Rocky Mountains in central Colorado and propagated eastward into western Nebraska and South Dakota by early evening (0200 UTC 18 May, Fig. 12a) and moved into central Nebraska by early morning (Fig. 12c). The associated areaaveraged precipitation in the NW region (black stars in Fig. 13) presents persistent decrease after 4 h (2200 CST) until 17 h (1100 CST) and a subsequent daytime increase due to solar heating (Fig. 12d), conforming to the mean diurnal cycle in the NW region presented in Fig. 5. These features indicate that Case A is under the influence of multiscale system interactions. The corresponding total RMDTE exhibits a clear diurnal cycle with a maximum occurring at  $\sim$ 7 h (0100 CST) and a minimum at 21 h (1500 CST). At the  $\gamma$  scale, with the influence of strong moist convection, the RMDTE depicts pronounced up-amplitude growth during the first 1 h and a slower but still significant growth until 3 h. The rapid growth in the first hour is partly due to the essential absence of  $\gamma$ -scale perturbations in the ensemble ICs as mentioned earlier; the ensemble dispersion increases rapidly in response to initial mesoscale and synoptic-scale perturbations derived from SREF. The RMDTE remains flat between 3 and 5h then decreases with weakening moist convection continually until 18h (1200 CST) when the error starts to increase rapidly again with the development of thermally forced afternoon convection within a weak forcing environment. The  $\beta$ - and  $\alpha$ -scale RMDTEs depict similar diurnal cycles but with phase lag, with the peaks being reached about 4 and 9h later, respectively, due to delayed response of larger-scale errors to convection. The results also indicate significant upscale transfer of convective scale error.

### b. Case B: 4 May 2018

Case B is a synoptically forced convective event with a surface low pressure center moving toward northeastern United States, producing intense precipitation in the NE subregion (black stars in Figs. 12e-h). Strong southerly low-level flows in the form of synoptic LLJ coming from the Gulf of Mexico exist around the western peripheral of the westward extending subtropical high, bringing rich moisture and energy into the Midwest region to support and maintain convection. The southerly low-level flows are further enhanced at night due to boundary layer inertial oscillation (Blackadar 1957) (Fig. 12f). It is clear that Case B is characterized by strong large-scale forcing with a pronounced lower  $\tau_c$  (Fig. 13). Different from Case A in the NW region, the total RMDTE in Case B does not have the typical diurnal feature of decreased values in the morning, but shows instead double peaks at 8 h (0300 EST) and 18h (1300 EST) (Fig. 13a); this is mostly due to the large contribution of  $\alpha$ -scale error during the day time, which peaks at around 18 h (1300 EST). Specifically, being more of a forced type, the  $\gamma$ -scale RMDTE (Fig. 14b) of Case B has a slower growth rate than that of Case A and reaches peak at 5 h. Interestingly, the  $\beta$ -scale RMDTE reaches peak at a similar



FIG. 12. Ensemble mean most unstable CAPE (MUCAPE; shaded), 925-hPa horizontal wind vectors, and precipitation rate (dotted shading) for (top) Case A and (bottom) Case B at different valid times: (a),(e) 0200; (b),(f) 0600; (c),(e) 1200; and (d),(h) 2000 UTC.

time (Fig. 13c), suggesting that organized convection dominates. During period 3, there is no secondary peak in the  $\gamma$ - or  $\beta$ -scale RMDTE; this is so even though there is a significant increase in precipitation in this period. The large increase in RMDTE at the  $\alpha$  scale in period 3 is linked to the strengthening of the low pressure system and the corresponding increase in organized frontal precipitation (Fig. 12h). As a short summary, both precipitation and error growth are dominated by evident large scale forcing in Case B, and the forecast error fits more closely to the three-stage error growth model (Zhang et al. 2007), indicative of much more prominent upscale growth of forecast error.

### c. Case C: 15 May 2018

In Case C the ensemble mean fields show an eastward propagating shallow trough at 500 hPa (not shown) through Texas as the convective event unfolds in the SW region (Figs. 14a-d). There are moderately strong southerly to southeasterly low-level flows from the Gulf into south-central and western Texas, which together with a jet aloft form strong deep-layer shear. Discrete supercells form along a north-south dryline located in eastern Texas panhandle into western Oklahoma (Fig. 14a) and move eastward (Figs. 14b,c) under the influence of large scale upper-level flows. The precipitation diurnal cycle is broadly similar to that of Case A, in that daily precipitation maximum occurs around 0000 UTC (1800 CST), and the precipitation minimum occurs at around 1700 UTC (1100 CST). The main difference is that Case C precipitation has a secondary maximum in the early morning (0900 UTC), and the precipitation throughout the morning is larger than Case A. Such early morning maximum should be related to enhancement of the nocturnal LLJ due to boundary layer inertial oscillations, which also cause clockwise rotation of boundary layer winds (Figs. 14a,b) (Blackadar 1957; Xue et al. 2018). By the afternoon of the second day, the low-level flow is restored to the southeasterly toward the panhandle areas (Fig. 14d), producing new convection along the dryline (near the western edge of subregion SW, Fig. 14d).

The total RMDTE in Case C (red curve in Fig. 13a) has similar, strong diurnal evolution as in Case A, although its peak is reached at around 9 h, 2–3 h later than in Case A (Fig. 13a). This delay is mainly due to the delay in  $\alpha$ -scale RMDTE (Fig. 13d) while the peaks of  $\gamma$ - and  $\beta$ -scale RMDTE are reached at essentially the same times as in Case A (Figs. 13b,c). This is consistent with the fact that the secondary precipitation peak at 0900 UTC is mainly due to forced convection at night (by nocturnal LLJ-induced convergence), which have large scales and act to mainly cause growth of larger-scale error that reaches its peak at ~1100 UTC. After reaching their minimum at ~1800 and ~2000 UTC, respectively, the smaller-scale RMDTEs increase rapidly again as new convection develops in the afternoon (Figs. 13b,c) but the  $\beta$ -scale RMDTE does not start to grow until 2200 UTC, and at a slower rate. In Case C, large-scale forcing is weak in the afternoon and early evening hours (marked by red circles in Fig. 13), so that the precipitation is of convective nature. The phase relations between precipitation intensity and RMDTEs at different scales again show significant roles of upscale error propagation.

### d. Case D: 16 May 2018

In Case D, the precipitation is mainly in the SE region, which is located in a zone of weak convergent flows between northerly flows from the north, and southwesterly flows on the north side of a high pressure system over the Gulf (Figs. 14e–h). Precipitation is from scattered convective cells that are heavier in the afternoon (16–24h) and evening hours (0–6h) when CAPE is higher (Figs. 14e,h); the precipitation diurnal cycle is weaker than Cases A–C mainly because the morning precipitation minimum is at a higher level. Clearly, the precipitation in the SE region in this case is mainly associated with local



FIG. 13. Time evolution of RMDTEs (solid curves) for four selected cases averaged in the corresponding regions at different scales: (a) total, (b) meso  $\gamma$ , (c) meso  $\beta$ , and (d) meso  $\alpha$ ; the stars indicate area-averaged precipitation exceeding 0.5 mm h<sup>-1</sup>, and the circles are indicators of weakly forcing (defined in section 5b) at certain times. The cases are color coded.

thermal instability under generally favorable thermodynamic conditions with weak large-scale forcing (high  $\tau_c$ ; Fig. 13). Like the average NRMDTEs for all cases in the SE region (Figs. 7a,d), the total RMDTE and that for the  $\alpha$  scale of Case D show almost monotonic increase throughout the 24 h (Figs. 13a,d), mainly due to the monotonic increase of the  $\alpha$  scale RMDTE. The RMDTEs for the  $\gamma$  and  $\beta$  scales show similar diurnal variations as those for Cases C and B, except that the maximum and minimum are reached faster (Figs. 13b,c), suggesting less organization of scattered convective cells into mesoscale convective systems that can sustain smaller scale error growth for longer; this is consistent with the weaker large-scale forcing in this region. This behavior leads to earlier saturation of smaller scale errors and smaller amplitudes reached. The more persistent precipitation throughout the 24 h and the weaker large-scale forcing appear to work together to produce relatively slow, but steady and monotonic growth in large-scale error in Case D (Fig. 13d).

Among the four cases, Cases B and D can be considered two extremes; Case B has the strongest large-scale forcing (having the least number of circles in Fig. 13), and the error growth in second half of the 24 h is mainly dominated by large-scale flow dynamics, while Case D is dominated by disorganized thermal convection with the weakest large scale forcing (most number of green circles in Fig. 13). In Case B, the total RMDTE continues to increase through 18 h of forecast, in the first half mainly through rapid growth of small-scale errors and upscale transfer, and in the second half as a result of both upscale transfer and large-scale error growth in association with the large-scale dynamic system. For Case D, because of the general lack of organization of scattered convective cells into larger mesoscale convective systems, the upscale transfer of  $\gamma$ - and  $\beta$ -scale errors to  $\alpha$  scale is less, not enough to create a significant peak in the early morning as in other cases; the  $\alpha$ -scale error increases mainly as a result of steady and generic growth of  $\alpha$ -scale



FIG. 14. Ensemble mean most unstable CAPE (MUCAPE, shaded), 925-hPa horizontal wind vectors, and precipitation rate (dotted shading) for (top) Case C and (bottom) Case D at different valid times: (a),(e) 0200; (b),(f) 0600; (c),(e) 1200; and (d),(h) 2000 UTC.

error itself, resulting in a monotonic curve that is less dependent on the precipitation diurnal cycle as in other cases.

#### 7. Summary and conclusions

This study investigates the error growth dynamics of convective events over the central U.S. regions using 3-km grid spacing CAM ensemble forecasts for 13 active convection days of May 2018. The ensemble uses the same forecast model configuration among its members, and the ensemble dispersion arises purely from the IC (at 0000 UTC or 1800 CST and 1900 EST) and LBC perturbations derived from a mesoscale ensemble forecasting system. Given that the model domain covers the full CONUS, and our analysis domain is east of the Rocky Mountains and only forecasts in the first 24 h are evaluated; since it takes some time for the upstream boundary condition to influence forecasts in the analysis domain, the IC perturbations play the primary role in ensemble dispersion (e.g., Johnson et al. 2011). In the ensemble ICs, convective-scale or  $\gamma$ -scale information is introduced through radar data assimilation without any perturbation. The forecast error is quantitatively characterized in terms of the (normalized) root mean difference total energy (N) RMDTE, which is used as a proxy of forecast error following earlier studies (e.g., Klasa et al. 2019; Nielsen and Schumacher 2016).

The analysis domain between the Rockies and the Appalachian Mountains is equally divided into the NW, NE, SE and SW subregions, and during May each subregion has its own dominant precipitation type with respect to the initiation and forcing mechanisms of convection, and hence different precipitation diurnal cycles. The discussions on the average behaviors over the 13 cases in each region are supplemented by four cases representative of precipitation in each region.

It is shown that when large-scale flow (synoptic scale system) is important (e.g., in the NE region), the region-average precipitation is strongly modulated by the large-scale forcing, while in the SE region, local thermal instability dominates and precipitation arises mostly from less organized convection. Within the 24 h, the total forecast error growth approximately follows the precipitation systems within Hovmöller diagrams, revealing a strong relationship between forecast error growth and precipitation. Specifically, the temporal evolutions of total NRMTE for each subregion are clearly linked to the precipitation diurnal cycles and convective system propagation.

Analyses on scale-dependent error growth show evident upscale error growth (Hohenegger and Schär 2007a; Selz and Craig 2015; Zhang et al. 2007) in all four regions/cases while up-amplitude growth within own scale plays different roles in different regions/cases. The meso- $\gamma$ -scale error growth is most directly linked to precipitation diurnal cycles while meso- $\alpha$ -scale error growth has strong link to large scale forcing. With the specific setup of the ensemble,  $\gamma$ -scale errors grow very rapidly in the first few hours as a result of IC perturbations at  $\beta$  and  $\alpha$  scales and the presence of moist convection in the IC, and the first peak of  $\gamma$ -scale NRMDTE is reached in 2 (in the SE region) to 5 (in the NE region) h. The  $\beta$ -scale NRMDTE grows slower and reaches the first peak in 6-9 h. The NRMDTE at both scales decreases significantly after the first peak through early afternoon due to decay/suppression of precipitation but increases rapidly again in the afternoon after the onset of new afternoon convection. The  $\alpha$ -scale NRMDTE generally follows a similar trend, but the first peak is reached much later in 11-18h, clearly an indication of successively upscale transfer of errors from smaller scales. In the specific example of NE precipitation case, the  $\alpha$ -scale NRMDTE continues to amplify until 18 h to a much higher level than in other cases due to the presence of an evolving low pressure system and the associated differences in strong synoptic-scale forcing. In a specific case in the SE region when large systems are much less dynamic, the precipitation is least organized and has weaker diurnal variations. As such, the  $\gamma$ - and

 $\beta$ -scale NRMDTE peaks are reached sooner, and the  $\alpha$ -scale NRMDTE continues monotonic increase throughout the 24 h. These results suggest that for regions where large-scale forcing is weak and when convection is mostly disorganized, upscale transfer of forecast error tends to be more limited and up-amplitude growth of the large-scale error can be as important. For the two cases producing precipitation mainly in the SW and NW regions, the convective cells tend to undergo organization into MCSs while moving eastward and experiencing nighttime boundary layer convergence forcing, the NRMDTEs of all three scales experience growth, decay and growth cycles within the 24-h forecasts, with successive delay in the phase of error evolution, indicating clear upscale error growth feeding off diurnally varying convection.

The relationships between RMDTE and intensity of moist convection or large-scale forcing are investigated based on correlation analyses for different scales and regions for different forecast periods. In particular, the correlation between forecast error magnitude and moist convection intensity increases with forecast hours with the forecast range due to accumulative effects of convection but decreases with increasing spatial scale. At the convective scales, the correlation is positive throughout the forecast period while for the  $\beta$  and  $\alpha$  scales the correlation is often negative during the initial period of forecast due to the delayed response of larger-scale errors to small-scale convection and the resulting phase differences.

The effect of large-scale forcing on forecast error is also examined in terms of the correlation between RMDTE and convective adjustment time scale  $\tau_c$ ; the forcing is considered stronger for smaller  $\tau_c$ . The correlation is strong and negative (positive correlation with forcing) during first 9 h at the  $\beta$  and  $\alpha$  scales and but much weaker at the  $\gamma$  scale. This implies that at a short forecast range, large-scale forcing has direct positive impact on larger-scale forecast errors, while convective-scale errors are controlled much less by forcing but more by thermodynamic instability. During the forecast periods between 10 and 15 h, and beyond 16 h, the correlation between forecast error and forcing strength is much weaker, and fluctuates around zero. This may be partly due to the specific definition of the forcing degree used because convective adjustment time is usually no more than several hours. For the specific case in the NE region (Case B), strong synoptic scale forcing in the second day afternoon does cause large increase in large scale error.

Overall, the error growth dynamics on CAM forecasts in the presence of significant moist convection are strongly dependent on the intensity, type and organization of precipitation, the forecast period with respect to the time of day and forecast range, and the spatial scale of the error. Small-scale forecast errors are directly impacted by convective activities and have short response time to convection while increasingly larger scale errors have longer response times and delayed phase. Within the 24-h forecasts, forecast errors generally experience growth, decay, and growth cycles following the precipitation diurnal cycle. Upscale transfer of forecast error is stronger when convective cells can become more organized with time which usually occur under stronger large scale forcing.

The results of this study shed light on the predictability of spring time convective weather in different regions of the United States and may be applicable to other parts of the world with similar flow and precipitation regimes. The understanding of error growth dynamics can help guide the optimal design of CAM ensemble forecasting systems. In future studies, the inclusion of meso- $\gamma$ -scale perturbations in the IC should also be considered and their impacts examined.

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#### REFERENCES

- Ashley, S. T., and W. S. Ashley, 2008: Flood fatalities in the United States. J. Appl. Meteor. Climatol., 47, 805–818, https://doi.org/ 10.1175/2007JAMC1611.1.
- Bachmann, K., C. Keil, G. C. Craig, M. Weissmann, and C. A. Welzbacher, 2019: Predictability of deep convection in idealized and operational forecasts: Effects of radar data assimilation, orography, and synoptic weather regime. *Mon. Wea. Rev.*, **148**, 63–81, https://doi.org/10.1175/MWR-D-19-0045.1.
- Bei, N., and F. Zhang, 2014: Mesoscale predictability of moist baroclinic waves: Variable and scale-dependent error growth. *Adv. Atmos. Sci.*, **31**, 995–1008, https://doi.org/10.1007/s00376-014-3191-7.
- Berenguer, M., M. Surcel, I. Zawadzki, M. Xue, and F. Kong, 2012: The diurnal cycle of precipitation from continental radar mosaics and numerical weather prediction models. Part II: Intercomparison among numerical models and with nowcasting. *Mon. Wea. Rev.*, **140**, 2689–2705, https://doi.org/ 10.1175/MWR-D-11-00181.1.
- Bierdel, L., T. Selz, and G. C. Craig, 2017: Theoretical aspects of upscale error growth through the mesoscales: An analytical model. *Quart. J. Roy. Meteor. Soc.*, **143**, 3048–3059, https:// doi.org/10.1002/qj.3160.
- Blackadar, A. K., 1957: Boundary layer wind maxima and their significance for the growth of nocturnal inversions. *Bull. Amer. Meteor. Soc.*, **38**, 283–290, https://doi.org/10.1175/1520-0477-38.5.283.
- Carbone, R. E., and J. D. Tuttle, 2008: Rainfall occurrence in the U.S. warm season: The diurnal cycle. J. Climate, 21, 4132–4146, https://doi.org/10.1175/2008JCLI2275.1.
- —, —, D. A. Ahijevych, and S. B. Trier, 2002a: Inferences of predictability associated with warm season precipitation episodes. J. Atmos. Sci., 59, 2033–2056, https://doi.org/10.1175/ 1520-0469(2002)059<2033:IOPAWW>2.0.CO;2.
- —, —, and —, 2002b: Inferences of predictability associated with warm season precipitation episodes. J. Atmos. Sci., 59, 2033–2056, https://doi.org/10.1175/1520-0469(2002) 059<2033:IOPAWW>2.0.CO;2.
- Chen, X., H. Yuan, and M. Xue, 2018: Spatial spread-skill relationship in terms of agreement scales for precipitation forecasts in a convection-allowing ensemble. *Quart. J. Roy. Meteor. Soc.*, 144, 85–98, https://doi.org/10.1002/qj.3186.
- Clark, A. J., W. A. Gallus, and T.-C. Chen, 2007: Comparison of the diurnal precipitation cycle in convection-resolving and

non-convection-resolving mesoscale models. *Mon. Wea. Rev.*, **135**, 3456–3473, https://doi.org/10.1175/MWR3467.1.

- —, —, M. Xue, and F. Kong, 2009: A comparison of precipitation forecast skill between small convection-permitting and large convection-parameterizing ensembles. *Wea. Forecasting*, 24, 1121–1140, https://doi.org/10.1175/2009WAF2222222.1.
- —, and Coauthors, 2018: The Community Leveraged Unified Ensemble (CLUE) in the 2016 NOAA/Hazardous Weather Testbed Spring Forecasting Experiment. *Bull. Amer. Meteor. Soc.*, **99**, 1433–1448, https://doi.org/10.1175/BAMS-D-16-0309.1.
- Dai, A., F. Giorgi, and K. E. Trenberth, 1999: Observed and modelsimulated diurnal cycles of precipitation over the contiguous United States. J. Geophys. Res., 104, 6377–6402, https:// doi.org/10.1029/98JD02720.
- Denis, B., J. Côté, and R. Laprise, 2002: Spectral decomposition of two-dimensional atmospheric fields on limited-area domains using the discrete cosine transform (DCT). *Mon. Wea. Rev.*, **130**, 1812–1829, https://doi.org/10.1175/1520-0493(2002)130<1812:SDOTDA>2.0.CO;2.
- Done, J. M., G. C. Craig, S. L. Gray, P. A. Clark, and M. E. B. Gray, 2006: Mesoscale simulations of organized convection: Importance of convective equilibrium. *Quart. J. Roy. Meteor. Soc.*, 132, 737–756, https://doi.org/10.1256/qj.04.84.
- —, —, —, and —, 2012: Case-to-case variability of predictability of deep convection in a mesoscale model. *Quart.* J. Roy. Meteor. Soc., **138**, 638–648, https://doi.org/10.1002/ qj.943.
- Du, J., G. Dimego, Z. Toth, D. Jovic, B. Zhou, J. Zhu, J. Wang, and H. Juang, 2009: Recent upgrade of NCEP short-range ensemble forecast (SREF) system. 23rd Conf. on Weather Analysis and Forecasting/19th Conf. on Numerical Weather Prediction, Omaha, NE, Amer. Meteor. Soc., 4A.4, https:// ams.confex.com/ams/23WAF19NWP/techprogram/paper\_ 153264.htm.
- Durran, D. R., and M. Gingrich, 2014: Atmospheric predictability: Why butterflies are not of practical importance. J. Atmos. Sci., 71, 2476–2488, https://doi.org/10.1175/JAS-D-14-0007.1.
- —, and J. A. Weyn, 2015: Thunderstorms do not get butterflies. Bull. Amer. Meteor. Soc., 97, 237–243, https://doi.org/10.1175/ BAMS-D-15-00070.1.
- Flack, D. L. A., S. L. Gray, R. S. Plant, H. W. Lean, and G. C. Craig, 2017: Convective-scale perturbation growth across the spectrum of convective regimes. *Mon. Wea. Rev.*, **146**, 387–405, https://doi.org/10.1175/MWR-D-17-0024.1.
- Fritsch, J. M., and R. E. Carbone, 2004: Improving quantitative precipitation forecasts in the warm season: A USWRP research and development strategy. *Bull. Amer. Meteor. Soc.*, 85, 955–966, https://doi.org/10.1175/BAMS-85-7-955.
- Hohenegger, C., and C. Schär, 2007a: Predictability and error growth dynamics in cloud-resolving models. J. Atmos. Sci., 64, 4467–4478, https://doi.org/10.1175/2007JAS2143.1.
- —, and —, 2007b: Atmospheric predictability at synoptic versus cloud-resolving scales. *Bull. Amer. Meteor. Soc.*, 88, 1783–1794, https://doi.org/10.1175/BAMS-88-11-1783.
- —, D. Lüthi, and C. Schär, 2006: Predictability mysteries in cloud-resolving models. *Mon. Wea. Rev.*, **134**, 2095–2107, https://doi.org/10.1175/MWR3176.1.
- Hu, M., M. Xue, and K. Brewster, 2006a: 3DVAR and cloud analysis with WSR-88D level-II data for the prediction of the Fort Worth, Texas, tornadic thunderstorms. Part I: Cloud analysis and its impact. *Mon. Wea. Rev.*, **134**, 675–698, https:// doi.org/10.1175/MWR3092.1.

- —, —, J. Gao, and K. Brewster, 2006b: 3DVAR and cloud analysis with WSR-88D level-II data for the prediction of the Fort Worth, Texas, tornadic thunderstorms. Part II: Impact of radial velocity analysis via 3DVAR. *Mon. Wea. Rev.*, **134**, 699–721, https://doi.org/10.1175/MWR3093.1.
- Janić, Z. I., 2001: Nonsingular implementation of the Mellor-Yamada level 2.5 scheme in the NCEP Meso Model. NCEP Office Note 437, 61 pp.
- Johnson, A., X. Wang, M. Xue, and F. Kong, 2011: Hierarchical cluster analysis of a convection-allowing ensemble during the Hazardous Weather Testbed 2009 Spring Experiment. Part II: Ensemble clustering over the whole experiment period. *Mon. Wea. Rev.*, **139**, 3694–3710, https://doi.org/10.1175/MWR-D-11-00016.1.
- —, and Coauthors, 2013: Multiscale characteristics and evolution of perturbations for warm season convection-allowing precipitation forecasts: Dependence on background flow and method of perturbation. *Mon. Wea. Rev.*, **142**, 1053–1073, https://doi.org/10.1175/MWR-D-13-00204.1.
- Judt, F., S. S. Chen, and J. Berner, 2016: Predictability of tropical cyclone intensity: Scale-dependent forecast error growth in high-resolution stochastic kinetic-energy backscatter ensembles. *Quart. J. Roy. Meteor. Soc.*, **142**, 43–57, https://doi.org/ 10.1002/qj.2626.
- Kain, J. S., and Coauthors, 2010: Assessing advances in the assimilation of radar data and other mesoscale observations within a collaborative forecasting-research environment. *Wea. Forecasting*, **25**, 1510–1521, https://doi.org/10.1175/2010WAF2222405.1.
- Keil, C., F. Heinlein, and G. C. Craig, 2014: The convective adjustment time-scale as indicator of predictability of convective precipitation. *Quart. J. Roy. Meteor. Soc.*, **140**, 480–490, https://doi.org/10.1002/qj.2143.
- Klasa, C., M. Arpagaus, A. Walser, and H. Wernli, 2019: On the time evolution of limited-area ensemble variance: Case studies with the convection-permitting ensemble COSMO-E. *J. Atmos. Sci.*, **76**, 11–26, https://doi.org/10.1175/JAS-D-18-0013.1.
- Knievel, J. C., D. A. Ahijevych, and K. W. Manning, 2004: Using temporal modes of rainfall to evaluate the performance of a numerical weather prediction model. *Mon. Wea. Rev.*, **132**, 2995–3009, https://doi.org/10.1175/MWR2828.1.
- Kong, F., K. K. Droegemeier, and N. L. Hickmon, 2006: Multiresolution ensemble forecasts of an observed tornadic thunderstorm system. Part I: Comparsion of coarse- and fine-grid experiments. *Mon. Wea. Rev.*, **134**, 807–833, https://doi.org/10.1175/ MWR3097.1.
- Lean, H. W., P. A. Clark, M. Dixon, N. M. Roberts, A. Fitch, R. Forbes, and C. Halliwell, 2008: Characteristics of high-resolution versions of the Met Office unified model for forecasting convection over the United Kingdom. *Mon. Wea. Rev.*, **136**, 3408–3424, https://doi.org/10.1175/ 2008MWR2332.1.
- Lin, Y., and K. E. Mitchell, 2005: The NCEP stage II/IV hourly precipitation analyses: Development and applications. 19th Conf. on Hydrology, San Diego, CA, Amer. Meteor. Soc., 1.2, https://ams.confex.com/ams/Annual2005/techprogram/paper\_ 83847.htm.
- Liu, H. X., and M. Xue, 2008: Prediction of convective initiation and storm evolution on 12 June 2002 during IHOP\_2002.
   Part I: Control simulation and sensitivity experiments. *Mon. Wea. Rev.*, 136, 2261–2282, https://doi.org/10.1175/ 2007MWR2161.1.

- Lorenz, E. N., 1969: The predictability of a flow which possesses many scales of motion. *Tellus*, **21**, 289–307, https://doi.org/ 10.3402/tellusa.v21i3.10086.
- Mass, C. F., D. Ovens, K. Westrick, and B. A. Colle, 2002: Does increasing horizontal resolution produce more skillful forecasts? *Bull. Amer. Meteor. Soc.*, 83, 407–430, https://doi.org/ 10.1175/1520-0477(2002)083<0407:DIHRPM>2.3.CO;2.
- Michell, K. E., 2005: The community Noah land surface model (LSM): User's guide, public release version 2.7.1. NCEP/EMC Doc., 26 pp., http://www.emc.ncep.noaa.gov/mmb/gcp/noahlsm/ Noah\_LSM\_USERGUIDE\_2.7.1.htm.
- Nielsen, E. R., and R. S. Schumacher, 2016: Using convectionallowing ensembles to understand the predictability of an extreme rainfall event. *Mon. Wea. Rev.*, **144**, 3651–3676, https://doi.org/10.1175/MWR-D-16-0083.1.
- Reynolds, R. W., N. A. Rayner, T. M. Smith, D. C. Stokes, and W. Wang, 2002: An improved in situ and satellite SST analysis for climate. J. Climate, 15, 1609–1625, https://doi.org/10.1175/ 1520-0442(2002)015<1609:AIISAS>2.0.CO;2.
- Savijärvi, H., 1991: The United States Great Plains diurnal ABL variation and the nocturnal low-level jet. *Mon. Wea. Rev.*, **119**, 833–840, https://doi.org/10.1175/1520-0493(1991)119<0833: TUSGPD>2.0.CO;2.
- Schaefer, J. T., 1986: The dryline. Mesoscale Meteorology and Forecasting, P. Ray, Ed., Amer. Meteor. Soc., 549–570.
- Selz, T., and G. C. Craig, 2015: Upscale error growth in a highresolution simulation of a summertime weather event over Europe. *Mon. Wea. Rev.*, **143**, 813–827, https://doi.org/10.1175/ MWR-D-14-00140.1.
- Skamarock, and Coauthors, 2008: A description of the Advanced Research WRF version 3. NCAR Tech. Note NCAR/TN-475+STR, 113 pp., https://doi.org/10.5065/D68S4MVH.
- Sun, X., M. Xue, J. Brotzge, R. McPherson, X. Hu, and X.-Q. Yang, 2016: An evaluation of dynamic downscaling of central plains summer precipitation using a WRF-based regional climate model at a convection-permitting 4-km resolution. J. Geophys. Res. Atmos., 121, 13 801–13 826, https://doi.org/ 10.1002/2016JD024796.
- Sun, Y. Q., and F. Zhang, 2016: Intrinsic versus practical limits of atmospheric predictability and the significance of the butterfly effect. J. Atmos. Sci., 73, 1419–1438, https://doi.org/10.1175/ JAS-D-15-0142.1.
- Surcel, M., M. Berenguer, and I. Zawadzki, 2010: The diurnal cycle of precipitation from continental radar mosaics and numerical weather prediction models. Part I: Methodology and seasonal comparison. *Mon. Wea. Rev.*, **138**, 3084–3106, https://doi.org/ 10.1175/2010MWR3125.1.
- —, I. Zawadzki, and M. K. Yau, 2014: A study on the scale dependence of the predictability of precipitation patterns. J. Atmos. Sci., 72, 216–235, https://doi.org/10.1175/JAS-D-14-0071.1.
- —, —, and —, 2016: The case-to-case variability of the predictability of precipitation by a storm-scale ensemble forecasting system. *Mon. Wea. Rev.*, **144**, 193–212, https:// doi.org/10.1175/MWR-D-15-0232.1.
  - —, —, M. Xue, and F. Kong, 2017: More on the scale dependence of the predictability of precipitation patterns: Extension to the 2009–13 CAPS spring experiment ensemble forecasts. *Mon. Wea. Rev.*, **145**, 3625–3646, https://doi.org/ 10.1175/MWR-D-16-0362.1.
- Tan, Z.-M., F. Zhang, R. Rotunno, and C. Snyder, 2004: Mesoscale predictability of moist baroclinic waves: Experiments with parameterized convection. J. Atmos. Sci., 61, 1794–1804, https://doi.org/ 10.1175/1520-0469(2004)061<1794:MPOMBW>2.0.CO;2.

- Thompson, G., P. R. Field, R. M. Rasmussen, and W. D. Hall, 2008: Explicit forecasts of winter precipitation using an improved bulk microphysics scheme. Part II: Implementation of a new snow parameterization. *Mon. Wea. Rev.*, **136**, 5095–5115, https://doi.org/10.1175/2008MWR2387.1.
- Trier, S. B., C. A. Davis, D. A. Ahijevych, M. L. Weisman, and G. H. Bryan, 2006: Mechanisms supporting long-lived episodes of propagating nocturnal convection within a 7-day WRF model simulation. J. Atmos. Sci., 63, 2437–2461, https:// doi.org/10.1175/JAS3768.1.
- —, J. W. Wilson, D. A. Ahijevych, and R. A. Sobash, 2017: Mesoscale vertical motions near nocturnal convection initiation in PECAN. *Mon. Wea. Rev.*, **145**, 2919–2941, https:// doi.org/10.1175/MWR-D-17-0005.1.
- Walser, A., D. Lüthi, and C. Schär, 2004: Predictability of precipitation in a cloud-resolving model. *Mon. Wea. Rev.*, 132, 560–577, https://doi.org/10.1175/1520-0493(2004)132<0560: POPIAC>2.0.CO;2.
- Wapler, K., F. Harnisch, T. Pardowitz, and F. Senf, 2015: Characterisation and predictability of a strong and a weak forcing severe convective event—A multi-data approach. *Meteor. Z.*, 24, 393–410, https://doi.org/10.1127/metz/2015/0625.
- Weyn, J. A., and D. R. Durran, 2017: The dependence of the predictability of mesoscale convective systems on the horizontal scale and amplitude of initial errors in idealized simulations. J. Atmos. Sci., 74, 2191–2210, https://doi.org/10.1175/ JAS-D-17-0006.1.
- —, and —, 2018: Ensemble spread grows more rapidly in higher-resolution simulations of deep convection. J. Atmos. Sci., 75, 3331–3345, https://doi.org/10.1175/JAS-D-17-0332.1.
- —, and —, 2019: The scale dependence of initial-condition sensitivities in simulations of convective systems over the southeastern United States. *Quart. J. Roy. Meteor. Soc.*, 145, 57–74, https://doi.org/10.1002/qj.3367.
- Wu, N., X. Zhuang, J. Min, and Z. Meng, 2020: Practical and intrinsic predictability of a warm-sector torrential rainfall event in the South China monsoon region. J. Geophys. Res. Atmos., 125, e2019JD031313, https://doi.org/10.1029/ 2019JD031313.
- Xue, M., and W. J. Martin, 2006: A high-resolution modeling study of the 24 May 2002 dryline case during IHOP. Part II: Horizontal convective rolls and convective initiation. *Mon. Wea. Rev.*, **134**, 172–191, https://doi.org/10.1175/MWR3072.1.
- —, D.-H. Wang, J.-D. Gao, K. Brewster, and K. K. Droegemeier, 2003: The Advanced Regional Prediction System (ARPS), storm-scale numerical weather prediction and data assimilation. *Meteor. Atmos. Phys.*, 82, 139–170, https://doi.org/10.1007/ s00703-001-0595-6.
- —, and Coauthors, 2007: CAPS realtime storm-scale ensemble and high-resolution forecasts as part of the NOAA Hazardous Weather Testbed 2007 spring experiment. 22nd Conf. on Weather Analysis and Forecasting/18th Conf. on Numerical Weather Prediction, Park City, UT, Amer. Meteor. Soc., 3B.1, https://ams.confex.com/ams/22WAF18NWP/techprogram/ paper\_124587.htm.
- —, X. Luo, K. Zhu, Z. Sun, and J. Fei, 2018: The controlling role of boundary layer inertial oscillations in Meiyu frontal precipitation and its diurnal cycles over China. J. Geophys. Res. Atmos., 123, 5090–5115, https://doi.org/10.1029/2018JD028368.
- Zhang, F., C. Snyder, and R. Rotunno, 2003: Effects of moist convection on mesoscale predictability. J. Atmos. Sci., 60, 1173–1185, https://doi.org/10.1175/1520-0469(2003)060<1173: EOMCOM>2.0.CO:2.

- —, N. Bei, R. Rotunno, C. Snyder, and C. C. Epifanio, 2007: Mesoscale predictability of moist baroclinic waves: Convectionpermitting experiments and multistage error growth dynamics. J. Atmos. Sci., 64, 3579–3594, https://doi.org/10.1175/ JAS4028.1.
- Zhang, X., 2019: Multiscale characteristics of different-source perturbations and their interactions for convection-permitting ensemble forecasting during SCMREX. *Mon. Wea. Rev.*, **147**, 291–310, https://doi.org/10.1175/MWR-D-18-0218.1.
- Zhuang, X., J. Min, L. Zhang, S. Wang, N. Wu, and H. Zhu, 2020: Insights into convective-scale predictability in east China: Error growth dynamics and associated impact on precipitation of warm-season convective events. *Adv. Atmos. Sci.*, **37**, 893– 911, https://doi.org/10.1007/s00376-020-9269-5.
- Zimmer, M., G. C. Craig, C. Keil, and H. Wernli, 2011: Classification of precipitation events with a convective response timescale and their forecasting characteristics. *Geophys. Res. Lett.*, **38**, L05802, https://doi.org/10.1029/2010GL046199.