

## Ensemble Kalman Filter Assimilation of Doppler Radar Data with a Compressible Nonhydrostatic Model: OSS Experiments

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### ABSTRACT

A Doppler radar data assimilation system is developed based on an ensemble Kalman filter (EnKF) method and tested with simulated radar data from a supercell storm. As a first implementation, it is assumed that the forward models are perfect and that the radar data are sampled at the analysis grid points. A general purpose nonhydrostatic compressible model is used with the inclusion of complex multiclass ice microphysics. New aspects of this study compared to previous work include the demonstration of the ability of the EnKF method to retrieve multiple microphysical species associated with a multiclass ice microphysics scheme, and to accurately retrieve the wind and thermodynamic variables. Also new are the inclusion of reflectivity observations and the determination of the relative role of the radial velocity and reflectivity data as well as their spatial coverage in recovering the full-flow and cloud fields. In general, the system is able to reestablish the model storm extremely well after a number of assimilation cycles, and best results are obtained when both radial velocity and reflectivity data, including reflectivity information outside of the precipitation regions, are used. Significant positive impact of the reflectivity assimilation is found even though the observation operator involved is nonlinear. The results also show that a compressible model that contains acoustic modes, hence the associated error growth, performs at least as well as an anelastic model used in previous EnKF studies at the cloud scale.

Flow-dependent and dynamically consistent background error covariances estimated from the forecast ensemble play a critical role in successful assimilation and retrieval. When the assimilation cycles start from random initial perturbations, better results are obtained when the updating of the fields that are not directly related to radar reflectivity is withheld during the first few cycles. In fact, during the first few cycles, the updating of the variables indirectly related to reflectivity hurts the analysis. This is so because the estimated background covariances are unreliable at this stage of the data assimilation process, which is related to the way the forecast ensemble is initialized. Forecasts of supercell storms starting from the best-assimilated initial conditions are shown to remain very good for at least 2 h.

### 1. Introduction

Since its introduction by Evensen (1994), the ensemble Kalman filter (EnKF) technique for data assimilation has received much attention. A rapidly increasing number of studies are appearing that examine its performance for various applications. In the field of meteorology, EnKF was first applied to large-scale data assimilation problems and observations are treated as random variables that are subject to perturbations (Evensen 1994; Burgers et al. 1998; Houtekamer and Mitchell 1998; Houtekamer 2001; Evensen 2003). Deterministic methods were developed more recently to avoid sampling errors associated with the use of perturbed observations or to address the adaptive observational network design problem; these methods

include the ensemble square-root filter (EnSRF; Whitaker and Hamill 2002; Tippett et al. 2003), the ensemble adjustment filter (Anderson 2001), and the ensemble transform Kalman filter (Bishop et al. 2001), which all belong to the broader class of square-root filters (Tippett et al. 2003).

In general, EnKF and related methods are designed to simplify or make possible the computation of flow-dependent error statistics. Rather than solving the equation for the time evolution of the probability density function of the model state, EnKF methods apply the Monte Carlo method to estimate the forecast error statistics. A large ensemble of model states are integrated forward in time using the dynamic equations; the moments of the probability density function are then calculated from this ensemble for different times (Evensen 2003).

In recent years, various techniques have been developed for analyzing and retrieving the atmospheric state at the convective scale from Doppler radar data. These methods range from purely kinematic to the so-

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phisticated 4D variational data assimilation method (4DVAR), which employs a nonhydrostatic prediction model and its adjoint (e.g., Gal-Chen 1978; Sun et al. 1991; Qiu and Xu 1992; Shapiro et al. 1995; Sun and Crook 1997; Gao et al. 1999; Wu et al. 2000; Weygandt et al. 2002). Most of the work deals with the retrieval and assimilation of radial velocity and/or reflectivity data from single-Doppler radar because dual- or multiple-Doppler coverage is not generally available. For the purpose of initializing NWP models, the 4DVAR method (e.g., Sun and Crook 1997; Gao et al. 1998) promises to provide an initial condition that is consistent with the prediction model and is able to effectively use multiple volume scans from a radar. However, the high cost of developing and maintaining an adjoint code, especially one that can run efficiently on distributed-memory parallel computer systems, and the need to include in the adjoint detailed physical processes that are more important at the convective scales have limited 4DVAR assimilations of Doppler radar and other high-resolution data to relatively simple applications and model settings.

Very recently, EnKF was applied to the assimilation of simulated Doppler radar data for a modeled convective storm (Snyder and Zhang 2003; Zhang et al. 2004) and of real radar data (Dowell et al. 2004). Very encouraging results are obtained in these studies in retrieving wind, temperature, and moisture field data for convective storms. The first two studies assimilated only radial velocity data, while in Dowell et al. (2004), the use of reflectivity data is limited to the update of the rainwater mixing ratio only. Neither of these studies included ice microphysics processes, and the assimilation system was based on an anelastic cloud model. A warm-rain microphysics scheme is also used in all of the aforementioned 4DVAR studies except for Wu et al. (2000) in which a simplified ice microphysics scheme was used. Dual-polarization radar data were assimilated by Wu et al. (2000) by first deriving hydrometeor mixing ratios from regular and differential reflectivities.

Because of the need to run an ensemble of the forecast and analysis of nontrivial sizes (usually a few tens to a few hundreds runs), the overall computational cost of ensemble-based assimilation methods is also significant. Fortunately, a sizeable portion of the assimilation procedure, including the forecast components, is easily parallelizable. There is no need, in general, for the adjoint of the forward observation operators, therefore indirect observations with complex observation operators, at least those that involve primarily local influences, can be easily included. Furthermore, the analysis code is more or less independent of the prediction model, which is just the opposite of the 4DVAR method. In addition, the system provides valuable uncertainty information on both analysis and forecast, and when combined with an existing ensemble prediction system, the incremental cost can be small.

The EnKF method is, however, not as mature as

4DVAR. No ensemble Kalman filter assimilation system has been implemented so far for operational use; EnKF also shares some common problems with 4DVAR, including issues with model errors, linear assumption associated with the optimality of solution, and the Gaussian error assumption. For observations, such as the integrated total water along the slant paths of global positioning system (GPS) data, the data influence region tends to be nonlocal. In such a case, the covariance localization will have to be done around the entire slant path instead of around local observation points. Additional issues may arise in such cases, with cost being one. For systems that involve error growth at very different temporal and spatial scales, more difficulties may arise. For these reasons, much research is still needed before reliable operational implementations of ensemble-based assimilation methods can be achieved. More recently, work has been done in comparing the relative performance of the 4DVAR and EnKF methods when assimilating Doppler radar data (Crook et al. 2002; Dowell et al. 2002; Caya et al. 2005, hereafter CSS).

In this study, we report on the development of an EnKF system based on a general purpose compressible nonhydrostatic model, and on the application of the system to the assimilation of the simulated radial velocity and/or reflectivity data from a single Doppler radar. The forecast model employs a complex multi-class ice microphysics scheme. The performance of the EnKF scheme in “recovering” the complete state of the model thunderstorms, including wind, temperature, pressure, and all water and ice fields, is examined. The relative impact of radial velocity and reflectivity data as well as their spatial coverage on the analysis are also investigated. The use of a compressible model, the inclusion of three-category ice microphysics in addition to the liquid water species, and the retrieval of multiple microphysics species with and without reflectivity data are aspects that are new compared to previous studies.

Even though we also performed experiments using an ensemble square-root filter, we report here only results using the perturbed observation method. The rest of the paper is outlined as follows. In section 2, we describe our EnKF assimilation system and the design of our observing system simulation (OSS) experiments. In section 3 we present the experiment results. The impact of various analyses on the forecast is discussed in section 4. A concluding section is given at the end of the paper.

## 2. Assimilation system and experimental design

### *a. The prediction model and truth simulation*

In this study, we test our EnKF assimilation system using simulated data from a classic supercell storm case that occurred on 20 May 1977 in Del City, Oklahoma

(Ray et al. 1981). Such simulation experiments are commonly referred to as observing system simulation experiments (OSSEs; see, e.g., Lord et al. 1997). The forecast model used is the Advanced Regional Prediction System (ARPS; Xue et al. 2000, 2001, 2003). In this study, the ARPS model is used in a 3D cloud model mode and the prognostic variables include three velocity components,  $u$ ,  $v$ ,  $w$ ; potential temperature,  $\theta$ ; pressure,  $p$ ; and six categories of water substances: water vapor specific humidity,  $q_v$ ; and mixing ratios for cloud water,  $q_c$ ; rainwater,  $q_r$ ; cloud ice,  $q_i$ ; snow,  $q_s$ ; and hail,  $q_h$ . In addition, turbulence kinetic energy is also predicted, which is used to determine turbulent mixing coefficients based on a 1.5-order turbulence closure scheme. The microphysical processes are parameterized using the three-category ice scheme of Lin et al. (1983) and its implementation follows Tao and Simpson (1993). More details on the model can be found in Xue et al. (2000, 2001).

For all experiments, the physical domain is  $64 \text{ km} \times 64 \text{ km} \times 16 \text{ km}$ . The model grid comprises  $35 \times 35 \times 35$  grid points (including points that facilitate the specification of boundary conditions), with grid intervals of 2 km in the horizontal directions and 0.5 km in the vertical. The truth simulation or nature run is initialized from a modified real sounding as used in Xue et al. (2001). The CAPE of the sounding is about  $3300 \text{ J kg}^{-1}$ . A 4-K ellipsoidal thermal bubble centered at  $x = 48$ ,  $y = 16$ , and  $z = 1.5 \text{ km}$ , with radii of 10 km in the  $x$  and  $y$  directions and 1.5 km in the  $z$  direction is used to initiate the storm. Open conditions are used at the lateral boundaries. A wave radiation condition is also applied at the top boundary. Free-slip conditions are applied to the bottom boundary. The length of simulation is up to 3 h. A constant wind of  $u = 3 \text{ m s}^{-1}$  and  $v = 14 \text{ m s}^{-1}$  is subtracted from the observed sounding to keep the primary storm cell near the center of the model grid. Despite the differences in resolutions, the evolution of the simulated storms is very similar to those documented in Xue et al. (2001).

During the truth simulation, the initial convective cell strengthens over the first 20 min. The strength of the cell then decreases over the next 30 min or so, which is associated with the splitting of the cell into two at around 55 min (Fig. 1). The right-moving (relative to the storm motion vector, which is toward the north-northeast) cell tends to dominate the system; the updraft reaches a peak value of  $44 \text{ m s}^{-1}$  at 90 min. The left-moving cell starts to split again at 95 min. The initial cloud started to form at about 10 min, and rainwater formed at about 15 min. Ice-phase fields appeared at about 20 min.

### b. Simulation of radar observations

As a first implementation, we assume that the simulated observations are available on the scalar grid points. Future work will assume the availability of data

in the radar coordinates. The simulated radial velocity,  $V_r$ , is calculated from

$$V_r = u \cos \alpha \sin \beta + v \cos \alpha \cos \beta + w \sin \alpha + \text{a random error}, \quad (1)$$

where  $\alpha$  is the elevation angle and  $\beta$  the azimuth angle of radar beams, and  $u$ ,  $v$ , and  $w$  are the model-simulated velocities interpolated to the scalar points of the staggered model grid. The random error is drawn from a normal distribution with zero mean and a standard deviation of  $1 \text{ m s}^{-1}$ . Since  $V_r$  is sampled directly from velocity fields, the effect of hydrometeor sedimentation does not come into play.

The simulated logarithmic reflectivity factor (referred to simply as reflectivity in most parts of this paper; in dBZ) is estimated from the following equations:

$$Z = 10 \log_{10} \left( \frac{Z_e}{1 \text{ mm}^6 \text{ m}^{-3}} \right) + \text{a random error}. \quad (2)$$

The equivalent reflectivity factor,  $Z_e$ , is made up of three components,

$$Z_e = Z_{er} + Z_{es} + Z_{eh}, \quad (3)$$

where  $Z_{er}$ ,  $Z_{es}$ , and  $Z_{eh}$  are contributions from rainwater, snow, and hail. The random error is drawn from a normal distribution with zero mean and standard deviation of 5 dB. Reflectivity relations corresponding to the 10-cm wavelength of the Weather Surveillance Radar-1988 Doppler (WSR-88Ds) are given below and used in our experiments.

The rain component of the reflectivity is calculated, based on Smith et al. (1975), from

$$Z_{er} = \frac{10^{18} \times 720 (\rho q_r)^{1.75}}{\pi^{1.75} N_r^{0.75} \rho_r^{1.75}}, \quad (4)$$

where  $\rho_r = 1000 \text{ kg m}^{-3}$  is the density of rainwater and  $\rho$  (in  $\text{kg m}^{-3}$ ) is the density of air;  $N_r = 8.0 \times 10^6 \text{ m}^{-4}$  is the intercept parameter in the assumed Marshall-Palmer exponential raindrop size distribution.

If the temperature is less than  $0^\circ\text{C}$ , then the component of the reflectivity is, for dry snow,

$$Z_{es} = \frac{10^{18} \times 720 K_i^2 \rho_s^{0.25} (\rho q_s)^{1.75}}{\pi^{1.75} K_r^2 N_s^{0.75} \rho_i^{1.75}}. \quad (5)$$

Here  $\rho_s = 100 \text{ kg m}^{-3}$  is the density of snow and  $\rho_i = 917 \text{ kg m}^{-3}$  is the density of ice,  $N_s = 3.0 \times 10^6 \text{ m}^{-4}$  is the intercept parameter for snow, and  $K_i^2 = 0.176$  is the dielectric factor for ice while  $K_r^2 = 0.93$  is the same for water. Wet snow, which occurs at temperatures higher than  $0^\circ\text{C}$ , is treated in a similar way as rainwater, and the equivalent reflectivity factor-mixing ratio relation is

$$Z_{es} = \frac{10^{18} \times 720 (\rho q_s)^{1.75}}{\pi^{1.75} N_s^{0.75} \rho_s^{1.75}}. \quad (6)$$



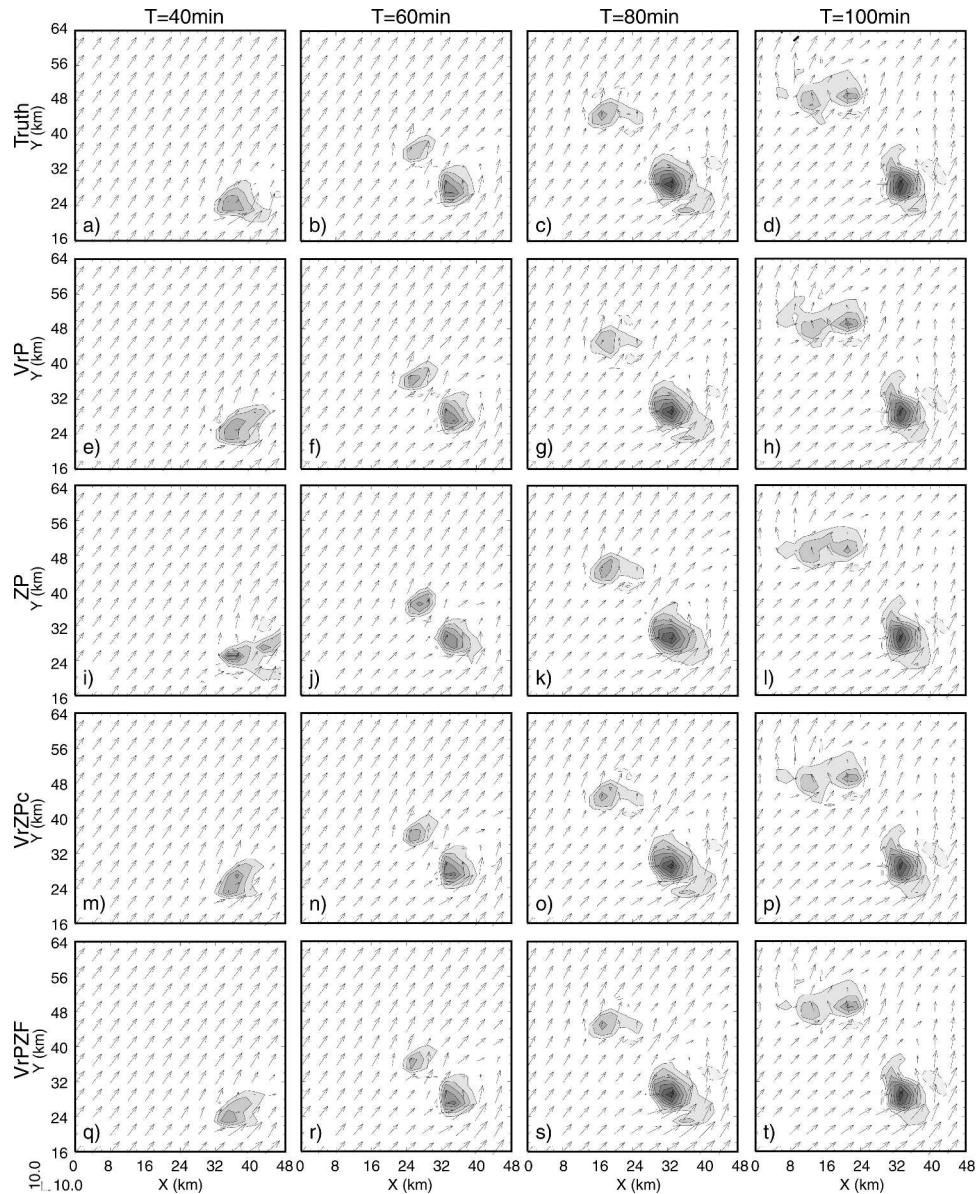


FIG. 1. Vertical velocity (contours and shading at intervals of  $4 \text{ m s}^{-1}$ ) and horizontal wind (vectors, plotted every other grid point;  $\text{m s}^{-1}$ ), at level  $z = 6 \text{ km}$ : (a)–(d) truth simulation; and analyses from (e)–(h) VrP, (i)–(l) ZP, (m)–(p) VrZPc, and (q)–(t) VrPZF, at  $t = 40, 60, 80$ , and  $100 \text{ min}$  during the assimilation period.

For hail, the wet hail formulation of Smith et al. (1975) is used:

$$Z_{\text{eh}} = \left( \frac{10^{18} \times 720}{\pi^{1.75} N_h^{0.75} \rho_h^{1.75}} \right)^{0.95} (\rho q_h)^{1.6625}, \quad (7)$$

where  $\rho_h = 913 \text{ kg m}^{-3}$  is the density of hail. The hail intercept parameter of  $N_h = 4.0 \times 10^4 \text{ m}^{-4}$  is used, which is slightly larger than that used in Smith et al. (1975), implying more occurrences of hail at smaller sizes. The same value is used in the ARPS implementation of the Lin et al. (1983) microphysics scheme.

Note that SI units are used in all equations above. Relations similar to the above are used in, for example, Ferrier (1994). The above equations define the observation operator denoted as  $H$  in the following section. When creating simulated observations for our OSS experiments, we impose a lower limit of  $1 \text{ mm}^6 \text{ m}^{-3}$  on the equivalent reflectivity factor to yield a lower limit of  $0 \text{ dBZ}$  for the logarithmic reflectivity factor.

The ground-based radar is located at the southwest corner of the computational domain, that is, at the origin of the  $x$ – $y$  coordinates (cf. Fig. 1). For data sampling and assimilation, we assume that the observation op-

erators, given by the above equations, are perfect. As with most atmospheric data assimilation systems, the prediction model is also assumed to be perfect; that is, no model error is explicitly taken into account. It is worth noting here that observation operators for reflectivity factors are nonlinear and because of that the error distribution of the reflectivity data is likely non-Gaussian. Discussions on the non-Gaussian nature of error distributions associated with nonlinear observation operators can be found in, for example, Lorenc (2003). One of the goals of this study is to assess the effectiveness of such data given these characteristics that violate the basic assumptions used in deriving the optimal EnKF solution.

### c. The EnKF data assimilation procedure

Our EnKF implementation is primarily based on the algorithm described by Evensen (1994), Burgers et al. (1998), and Houtekamer and Mitchell (1998), which uses the perturbed-observation method. In this algorithm, the ensemble mean is supposed to be the best estimate of the true state and the spread of the ensemble around the mean is a good estimate of the error in the ensemble mean (Evensen 2003). The forecast and analysis error covariances, given by the matrix  $\mathbf{P}$ , are defined as

$$\mathbf{P}^f \equiv \mathbf{P}_e^f = \overline{(x^f - \bar{x}^f)(x^f - \bar{x}^f)^T} \quad \text{and} \quad (8)$$

$$\mathbf{P}^a \equiv \mathbf{P}_e^a = \overline{(x^a - \bar{x}^a)(x^a - \bar{x}^a)^T}, \quad (9)$$

where the overbar denotes the ensemble mean and superscripts  $a$  and  $f$  denote analysis and forecast, respectively. Each ensemble member is updated by the analysis equation

$$x_i^a = x_i^f + \mathbf{P}^f \mathbf{H}^T [\mathbf{H} \mathbf{P}^f \mathbf{H}^T + \mathbf{R}]^{-1} (y_i^o - H x_i^f), \quad (10)$$

where  $i$  represents the  $i$ th ensemble member and  $x_i^f$  is the first guess obtained from the  $i$ th ensemble forecast. In addition,  $H$  is the observation operator, which converts the model states to the observed parameters, and  $\mathbf{H}$  in its standard notion is the linearized version of  $H$  in a matrix form but will not be explicitly evaluated anywhere in the analysis procedure. The linearization is required to arrive at the optimal analysis covariance minimizing solution (see, e.g., Kalnay 2002). Following Evensen (2003) and Houtekamer and Mitchell (1998), observations are treated as random variables having a distribution with a mean equal to the first-guess observations  $y^o$  and error covariances given by matrix  $\mathbf{R}$ . Thus an ensemble of observations is obtained by

$$y_i^o = y^o + \varepsilon_i, \quad (11)$$

and the observation error covariance matrix is calculated from the random errors added to the observations, as given in Eq. (11):

$$\mathbf{R} \approx \mathbf{R}_e = \overline{\varepsilon \varepsilon^T}, \quad (12)$$

where  $\varepsilon$  is observation error. The above calculation of  $\mathbf{R}$  is only possible with OSSE experiments where observations contaminated by errors with known variance and distribution are constructed. For real observations, a certain estimate of  $\mathbf{R}$  has to be made. Also, our assumption about the noncorrelation among the observational errors determines that  $\mathbf{R}$  is diagonal. Finally, in our current application,  $y^o$  includes the radial velocity and reflectivity.

The forecast error covariances are calculated from

$$\mathbf{P}^f \mathbf{H}^T \equiv \frac{1}{N-1} \sum_i^N (x_i^f - \bar{x}^f) [H(x_i^f) - \overline{H(x^f)}]^T, \quad (13)$$

and

$$\mathbf{H} \mathbf{P}^f \mathbf{H}^T \equiv \frac{1}{N-1} \sum_i^N [H(x_i^f) - \overline{H(x^f)}] [H(x_i^f) - \overline{H(x^f)}]^T, \quad (14)$$

where  $N$  is the number of ensemble members. The use of the nonlinear observation operator in the evaluation of covariances in Eqs. (13) and (14) is an advantage of EnKF compared to a traditional extended Kalman filter for nonlinear problems (Evensen 2003).

As can be seen, the nonlinear observation operator  $H$  is directly used in Eqs. (13)–(14), and  $\mathbf{H}$  and its transpose are not evaluated directly (the transpose of  $\mathbf{H}$  or the adjoint of the observation operator is needed by variational assimilation methods). The underlying assumption of standard extended Kalman filter theory (which is the basis of EnKF) is that the forecast model and the observation operator are linear. The nonlinearity in the forecast model and the observation operator (such as that of reflectivity data) can make the algorithm suboptimal. Strong nonlinearity would also render initially Gaussian error distributions non-Gaussian. In this study, the performance of the EnKF in such a situation will be examined.

We start the initial ensemble forecast at 20 min of model time when the storm cell developing out of an initial bubble reaches peak intensity. To initialize the ensemble members, random noises are added to the initially horizontally homogeneous background that is based on the environmental sounding. The random noises are sampled from Gaussian distributions with zero mean and standard deviation of  $3 \text{ m s}^{-1}$  for  $u$ ,  $v$ , and  $w$ , and  $3 \text{ K}$  for potential temperature. The pressure, moisture, and microphysical variables are not perturbed. The technique of adding initial perturbation has been discussed by former studies of Snyder and Zhang (2003) and Dowell et al. (2004), who found that adding initial perturbations to the entire computational domain would introduce spurious cells in individual members. Limiting the perturbation region around the observed storm area helps improve the assimilation result. However, for general applications of EnKF, the ensemble forecast should cover all scales of motion. We

TABLE 1. List of data assimilation experiments.

Expt	Observation: radial velocity ( $V_r$ ) and/or reflectivity ( $Z$ )	Update of $q_r$ , $q_s$ , and $q_h$	Update of $u$ , $v$ , $w$ , $q_v$ , $q_c$ , and $q_i$ when assimilating reflectivity
VrP	$V_r$ ( $Z > 10$ dBZ)	Yes	
VrF	$V_r$	Yes	
ZP	$Z$ ( $Z > 10$ dBZ)	Yes	Yes
VrZPa	$V_r$ & $Z$ ( $Z > 10$ dBZ)	Yes	Yes
VrZPb	$V_r$ & $Z$ ( $Z > 10$ dBZ)	Yes	No
VrZPc	$V_r$ & $Z$ ( $Z > 10$ dBZ)	Yes	Yes, start from fourth cycle
VrPZF	$V_r$ ( $Z > 10$ dBZ) and $Z$	Yes	Yes, start from the fourth cycle
VrPnoIce	$V_r$ ( $Z > 10$ dBZ)	No	

chose to apply the initial perturbations to the entire domain except for the grid points at the lateral boundary to keep the system more general. The open lateral boundary condition is sensitive to boundary errors and initial perturbations introduced at the boundary were found to trigger spurious storm development within some ensemble members. Assimilating reflectivity in clear-air region is found to help suppress spurious cells in the interior domain, hence allowing a more general application of the initial perturbations.

The observations are assimilated every 5 min. The first analysis is performed at 25 min and 100 ensemble members are used. As mentioned earlier, observations are perturbed by adding Gaussian noise, with a standard deviation of  $1 \text{ m s}^{-1}$  for radial velocity and 5 dBZ for reflectivity. The observation errors are assumed to be uncorrelated; therefore, observations can be and are analyzed sequentially one at a time, following Houtekamer (2001). When using a small (relatively to the degrees of freedom of the analysis system) ensemble to estimate the background error covariances, the estimated values between distant grid points are not reliable. Therefore covariance localization is necessary (Houtekamer and Mitchell 1998; Anderson 2001; Hamill et al. 2001; Houtekamer 2001).

In our early study (Tong and Xue 2004), we limited the influence region of each observation to a rectangular region with a half-width of two grid intervals in both horizontal and vertical directions, equivalent to 4 and 1 km in the horizontal and vertical, respectively. Some useful information beyond that region of influence was not utilized (though the computation was faster). To spatially smooth the analysis increments as well as to localize covariances, Houtekamer (2001) proposed a method that applies a Schur (elementwise) product of the background error covariance calculated from the ensemble and a correlation function with local support. This method was also used by Dowell et al. (2004). In the same way, we multiply each element of the background error matrix  $\mathbf{P}^{\text{H}}$  with a weight computed from the correlation function given by Eq. (4.10) of Gaspari and Cohn (1999). The weight decreases gradually from 1 at the observation point to zero at an effective cutoff radius and remains zero beyond. Through assimilation experiments with cutoff radii ranging from 4 to 10 km, we found that 8 km worked the best with 100 ensemble

members. This value is therefore used in all experiments presented in this paper. The use of a smooth filter function is found to produce a significantly better analysis than the sharp cutoff function used earlier in Tong and Xue (2004).

The EnKF algorithm tends to underestimate the analysis uncertainty owing to the use of limited ensemble size. To solve this problem, we tested the double-ensemble method (Houtekamer and Mitchell 1998), in which the statistics estimated from one ensemble are used to update the other. However, this approach overestimated the analysis uncertainty in our case and did not help improve our analysis. We also tested the covariance inflation approach of Anderson (2001), which did not work well at first. As found in Snyder and Zhang (2003), it enhances the spurious cell in ensemble members. A modification is then made by applying covariance inflation to the grid points that will be influenced directly during the analysis update by the observations found within the precipitation (where observed  $Z > 10$  dBZ) regions. To do this, we check for each grid point to see if within an 8-km radius (the same radius used by the covariance localization) there is at least one reflectivity data point greater than 10 dBZ. If it is true, then covariance inflation is applied to this grid point. This is found to improve our analysis. The inflation factor we used is 1.07 or 7% when radial velocity or/and reflectivity data in the precipitation region are assimilated. When reflectivity data of complete coverage are used, the inflation factor is increased to 1.1 (10%). Zhang et al. (2004) proposed another alternative to the traditional covariance inflation that is to avoid enhancing spurious cells but CSS found that the use of the method degrades the quality of analysis.

### 3. The assimilation experiments

Table 1 lists eight experiments to be discussed in this paper. The assimilation scheme is first tested by assimilating radial velocity or reflectivity data alone or by assimilating both. Further, data coverage tests are performed in which each data type is available either in the entire domain or only in regions where reflectivity exceeds 10 dBZ (referred to as the precipitation region). Additional variations have to do with the ways analysis



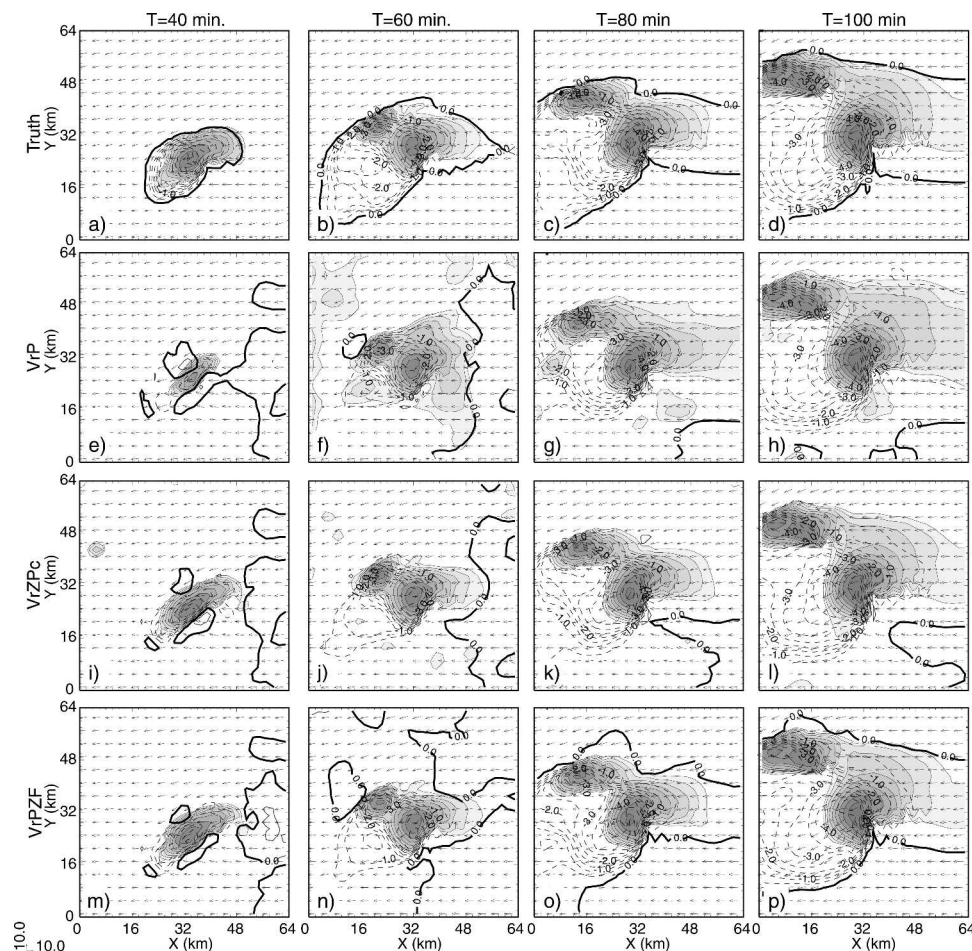


FIG. 2. Horizontal perturbation wind (vectors;  $\text{m s}^{-1}$ ), perturbation potential temperature (thick black lines for 0 K and thin-dashed contours at 0.5-K intervals) and computed reflectivity (thin solid contours and shading at intervals of 5 dBZ, starting from 15 dBZ) at  $z = 250$  m: (a)–(d) truth, and EnKF analyses from (e)–(h) VrP, (i)–(l) VrZPc, and (m)–(p) VrPZF.

variables are updated during the assimilation cycles. The results are discussed in the following sections.

#### a. Assimilations using radial velocity data only

In experiment VrP (see Table 1), we assume that the radial velocity data are available in precipitation regions where the reflectivity is greater than 10 dBZ. After only one analysis cycle (at  $t = 25$  min), the basic patterns of middle-level horizontal winds around the storm appear reasonable (not shown). After three more analysis cycles, that is, by 40 min, the basic structures of updraft and horizontal flow (Fig. 1e) as well as perturbation temperature (not shown) above the low-level cold pool are reasonably well retrieved. The low-level cold pool and the associated divergence are too weak at this time (Fig. 2e). Some hydrometeors can be retrieved at this time, but their amount and locations are not yet accurate. Two assimilation cycles later, at 50 min, the strength of the updraft and the magnitude of the tem-

perature perturbation (except that in the low-level cold pool) become reasonably good.

At 60 min, the retrieved microphysical fields also become rather close to the truth as seen from the vertical cross sections [Figs. 3a(2)–f(2)], and so do most other fields (Figs. 1f and 2f). The largest differences at this time are found at the low levels (Fig. 2f), where precipitation and cooling in the otherwise unperturbed low-level inflow region exist, and near the western boundary. Evaporative cooling due to spurious precipitation in some ensemble members was the cause. Much of the error is corrected by subsequent analyses and, by 100 min (Fig. 2h), the precipitation in the inflow region is generally gone except for a small area ahead of the rear-flank gust front. The low-level flow and reflectivity patterns as well as the shape of the cold pool now agree quite well with the truth (Figs. 2h and 2d) although small differences are still found with the exact location of the boundary of rain-cooled regions (as indicated by the  $0^\circ \theta'$  contours) and in the areal coverage of the

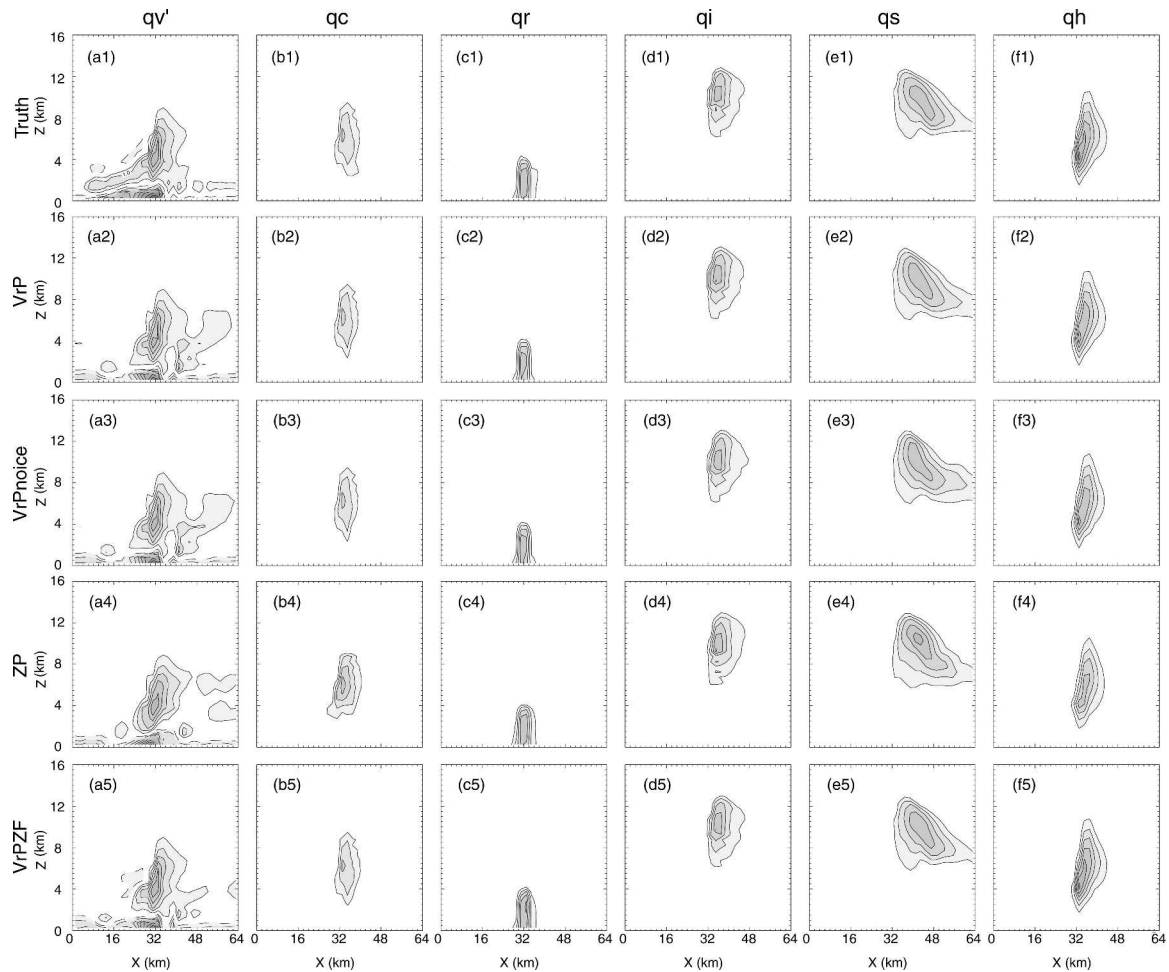


FIG. 3. The retrieved (a) perturbation  $q_v$  [solid (dashed) contours represent positive (negative) values], (b)  $q_c$ , (c)  $q_r$ , (d)  $q_i$ , (e)  $q_s$ , and (f)  $q_h$ . (contours and shading at intervals of  $0.5 \text{ g kg}^{-1}$  for  $q_v$  perturbation,  $q_c$ ,  $q_i$ , and  $q_s$ , and of  $1.0 \text{ g kg}^{-1}$  for  $q_r$  and  $q_h$ ) in the  $x$ - $z$  plane at  $y = 29 \text{ km}$  that pass through the maximum updraft at  $t = 60 \text{ min}$ : (a1)–(f1) truth simulation, (a2)–(f2) VrP, (a3)–(f3) VrPnoIce, (a4)–(f4) ZP, and (a5)–(f5) VrPZF.

leading precipitation region on the east-northeast side. The agreement at the 6-km level is even better (Figs. 1h and 1d). These results indicate that even with radial velocity data in the precipitation region only, the EnKF system is able to rebuild the model storm remarkably well after a sufficient number of assimilation cycles. Analysis of such quality can only be expected of methods that make use of multiple radar volume scans effectively and in a way that is compatible with the hopefully correct model physics.

We use the root-mean-square (rms) error of the ensemble mean analysis to judge quantitatively the quality of the analysis. The rms errors are averaged over those grid points where the reflectivity is greater than 10 dBZ. The rms errors of velocities, temperature, cloud, and hydrometeor variables in experiment VrP are seen to decrease rapidly during the first four assimilation cycles (over 20 min) and the analysis tends to converge at about 70 min (Fig. 4, black curves). When

the analysis converges, the rms analysis error for the horizontal wind components is generally less than  $1 \text{ m s}^{-1}$  and about  $0.5 \text{ m s}^{-1}$  for the vertical velocity. For perturbation potential temperature  $\theta'$ , the analysis error decreases to less than  $0.5 \text{ K}$  at 60 min. Such velocity errors are similar to or less than the observational errors added to the radial velocity, which means that after 8–10 assimilation cycles, the EnKF system is producing a very good estimate of the state of the simulated storm.

In experiment VrF, in which  $V_r$  data cover the entire domain, the analysis converges more quickly and the analysis errors are smaller (black dotted lines in Fig. 4). The retrieved winds, potential temperature, pressure, and water vapor content are significantly better than those of the VrP case. The retrieved microphysical fields are also improved, but not as much as when the full coverage reflectivity data are used (results to be presented later). For radial velocity data to be available outside the precipitation region, the radar has to be



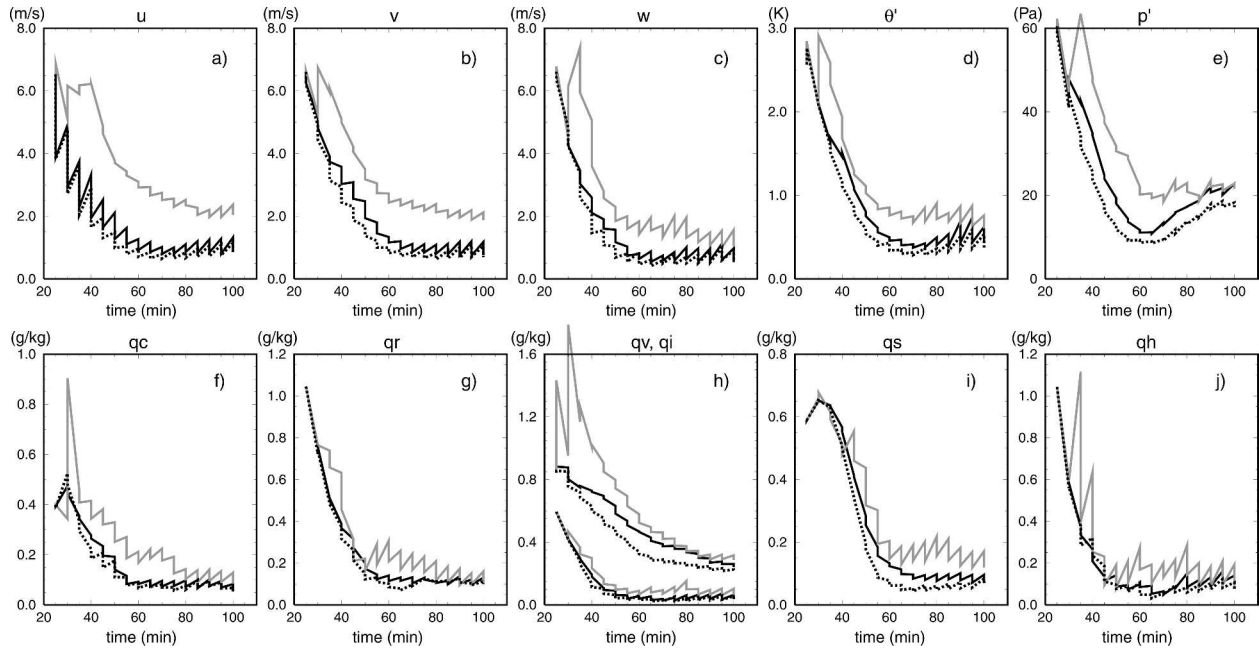


FIG. 4. The rms errors of the ensemble-mean forecast and analysis, averaged over points at which the reflectivity is greater than 10 dBZ for (a)  $u$ , (b)  $v$ , (c)  $w$ , and (d) perturbation potential temperature  $\theta'$ , (e) perturbation pressure  $p'$ , (f)  $q_c$ , (g)  $q_r$ , (h)  $q_v$  (the curves with larger values),  $q_i$  (the curves with lower values), (i)  $q_s$  and (j)  $q_h$ , for experiments VrP (black) and ZP (gray), and VrF (black dotted lines). Units are shown in the plots. The drops in the error curves at specific times correspond to the reduction of error by analysis.

operating in high-sensitivity mode, which is generally not the case with the WSR-88D network when precipitation is present. However, when such data are available, our experiment shows a clear positive impact of the data.

In our earlier study (Tong and Xue 2004), we found that when the pressure field is analyzed (updated by the analysis procedure), the pressure error increases (instead of decreases) after each analysis cycle. A careful examination of the results reveals that the main problem was associated with a domain-wide pressure drift in the forecast that often occurs in simulations using a small computational domain and an open boundary condition. The background error covariance between pressure and observations in the presence of the pressure drift was apparently not correct, causing a negative analysis impact on the pressure field. In all experiments presented here, the pressure detrending option of the ARPS model is turned on, which forces the domain-mean perturbation Exner function to zero after each forecast time step. The model solution, at least in the dry case, should be independent of the perturbation Exner function to an arbitrary constant.

After applying pressure detrending, the pressure drift is much more controlled and the update of the pressure by analysis does reduce its error in general, though not as much as for other fields (cf. e.g., black curves in Figs. 4e and 4c). At 40 min in the current experiment (VrP), the basic pattern of the perturbation

pressure can be reasonably reconstructed (not shown). Noticeable noises associated with acoustic oscillations remain at low levels at this time, which are reduced by additional assimilation cycles. However, as can be seen in Fig. 4e (black curve), the forecast error of the pressure perturbation starts to increase again at 65 min, and the error is not effectively reduced by further analysis. It is found that in this case some positive pressure drift still occurs in the ensemble-mean forecast and analysis below 4 km. The positive pressure perturbation associated with the cold pool is about 20 Pa higher than in the truth. The low pressure below the updraft is not as low as it should be. Such pressure biases appear to be preventing the EnKF scheme from working effectively in reducing the pressure errors, which is only indirectly related to  $V_r$ . It will be shown later that when reflectivity data are assimilated, the pressure drift problem is alleviated and the analysis of pressure is improved.

#### b. Impact of assimilating reflectivity data

Reflectivity is a measurement that is provided by all types of weather radar. In this section, we examine if reflectivity data alone are sufficient for the model to reproduce the true storm; we also study their value when used in combination with radial velocity data. We note that the observation operator for reflectivity is nonlinear and there exist more uncertainties with the reflectivity operator (because of uncertainties with the

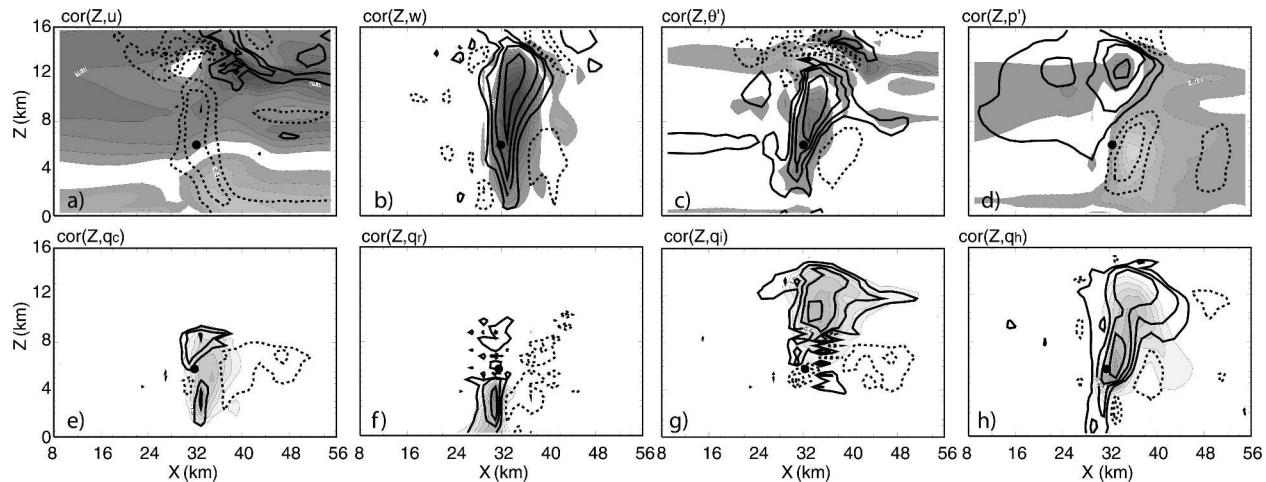


FIG. 5. Forecast error correlations estimated from an ensemble at  $t = 80$  min for experiment ZP in the  $x$ - $z$  plane at  $y = 29$  km, which passes through the maximum updraft. The error correlation [thick solid (dash) contours represent positive (negative) correlations at intervals of 0.2] between forecast reflectivity  $Z$  at  $x = 32$  km and  $z = 6$  km (indicated by a black dot) and (a)  $u$ , (b)  $w$ , (c)  $\theta'$ , (d)  $p'$ , (e)  $q_c$ , (f)  $q_r$ , (g)  $q_i$ , and (h)  $q_h$ . The shading and thin solid (thin dashed) contours in (a)–(d) indicate positive (negative) values of model fields from the truth simulation with increments of  $4 \text{ m s}^{-1}$  for  $u$  and  $w$ ;  $2 \text{ K}$  for  $\theta'$ , and  $40 \text{ Pa}$  for  $p'$ . The shading and thin contours in (e)–(h) indicate the values of the mixing ratios of water and ice fields from the truth simulation with an increment of  $0.5 \text{ g kg}^{-1}$  for  $q_c$ , and  $q_i$  and  $1 \text{ g kg}^{-1}$  for  $q_r$  and  $q_h$ .

cloud microphysics, the effects of attenuation, and others) than with the radial velocity. In our model, the rainwater, snow, and hail mixing ratios,  $q_r$ ,  $q_s$ , and  $q_h$ , are directly related to the observed reflectivity through Eqs. (3)–(7). Therefore, the experiments further test the performance of the EnKF scheme for nonlinear observations.

In experiment ZP (see Table 1), reflectivity ( $Z$ ) data greater than  $10 \text{ dBZ}$  are assimilated but not radial velocity. Generally, the analysis obtained by assimilating reflectivity data only is not as good as the analysis assimilating radial velocity data alone. As can be seen in Fig. 4 (gray curves), the analysis acts to reduce the rms errors in  $q_r$ ,  $q_h$ ,  $q_s$ ,  $q_c$ ,  $q_i$ ,  $w$ , and  $\theta'$  from the third cycle with the reduction of error in  $q_h$  being much larger. Significant reduction in the errors of the horizontal wind components and in  $q_v$  did not start until after four to five cycles. In fact, during the first two cycles, the update of most variables increases rather than decreases the error (see, e.g., the gray curves in Fig. 4d for  $\theta'$  and Fig. 4h for  $q_v$ ). A significant reduction in the errors of the horizontal wind components and in  $q_v$  did not start until after four to five cycles.

The delay in the reduction of or even an increase in the rms errors in variables not directly related to  $Z$  is related to our initial perturbation method. When the ensemble members are initialized, cloud and hydrometeor fields are not perturbed. This is reasonable because the location of the precipitation region is unknown before the observational data are introduced. Adding hydrometeor perturbations everywhere in the model is undesirable because nonzero values in certain variables like cloud ice should only exist under certain

conditions. If the initial background contains some information about the cloud, then random perturbations can be added to the related fields in a way similar to that for the other fields. Without direct initial perturbations to them, it takes the model a couple of assimilation cycles to develop clouds and hydrometeors and to establish coherent covariance structures for a reliable estimation of the error covariances. For these reasons, updating indirectly related variables in the first few cycles increases their errors. Enough ensemble spread is established starting from the third assimilation cycle; from then on, the analysis is able to correct forecast errors in fields including  $w$ ,  $\theta'$ ,  $q_c$ ,  $q_r$ ,  $q_i$ ,  $q_s$ , and  $q_h$  (Fig. 4). Reliable covariances between reflectivity and  $p$ ,  $q_v$ , and the horizontal wind components are slower to develop and the analysis correction starts a couple of cycles later.

Because of the lack of reliable covariances, the retrieved model fields in ZP are not good at 40 min (Fig. 1i). By 45 min, the storm updraft and temperature perturbation pattern become reasonable. The locations of the hydrometeors are now close to the truth. However, horizontal wind patterns are still not very good at this time. From 60 min on, the basic structure and the evolution of the storm, including the split storm cells, become rather accurate. The errors in all fields are further reduced in the subsequent assimilation cycles (Fig. 4), but remain higher than those in the VrP case by the end of the assimilation period (100 min).

Retrieving the model state from the observed variables in the EnKF system relies heavily on a good estimate of the flow-dependent multivariate background error covariances. Figure 5 shows, for experiment ZP,

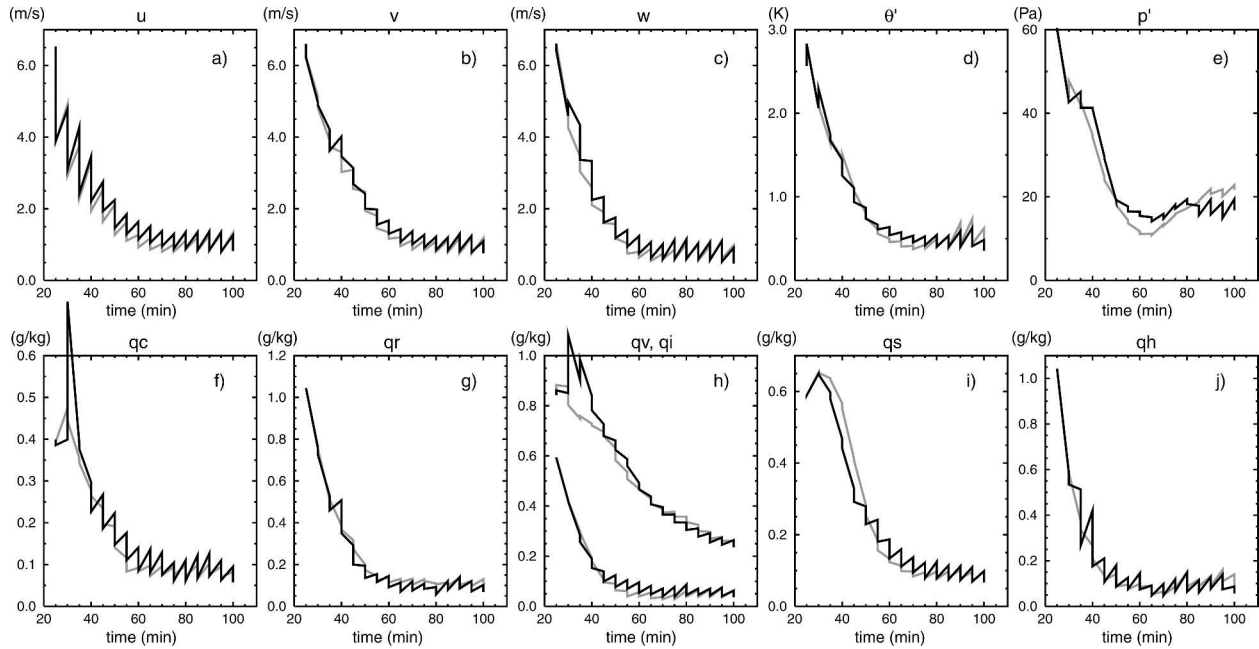


FIG. 6. As in Fig. 4, but for expt VrZPa (black) and expt VrP (gray).

the forecast background error correlations between reflectivity at point  $x = 32$  km,  $z = 6$  km and the model variables at each grid point in an  $x$ - $z$  vertical cross section through the maximum updraft ( $y = 29$  km) at 80 min (the correlation patterns for other experiments at this time are similar). As can be seen, for the water and ice fields, significant correlations are mostly confined to the regions where their nonzero values are found. For  $w$  and  $\theta'$ , the correlation patterns also match those of  $w$  and  $\theta'$  themselves in general, and significant correlations extend through much of the troposphere depth, which is consistent with the nature of deep convection. The maximum correlations for  $w$  and  $\theta'$  exceed 0.8, indicating that they are highly correlated with reflectivity. Generally, positive correlations are associated with updraft and high buoyancy; negative correlations are found in the recirculation regions. The correlation for  $\theta'$  spreads above the tropopause in a wavy pattern both upstream and downstream, which should be related to the gravity wave propagation in the stable stratification there.

Even for pressure, coherent structures of significant correlation exist. The maximum negative correlation is found at the midlevels where the perturbation pressure has a minimum; the maximum positive correlation exists near the cloud top. This correlation pattern can be explained by the rotating supercell storm dynamics. Stronger updraft rotation produces lower midlevel pressure, which promotes stronger updraft therefore producing more reflectivity. Stronger updraft, accompanied by larger reflectivity, will produce larger positive pressure perturbations at the cloud top due to both hydrostatic and Bernoulli effects. These suggest that

the error correlations estimated from the forecast ensemble are dynamically consistent. It is these valuable correlations that act to spread the information from the observation points to the finite domain surrounding them and that retrieve the unobserved variables from the observed ones. The results also justify our choice of the influence region in the covariance localization. Most of the significant correlations within 4 km of the center of the influence region are kept and smaller weights are given to the correlations extending up to 8 km.

### c. Assimilation of both radial velocity and reflectivity

In the next set of experiments (VrZPa-c, VrPZF; see Table 1), we combine the radial velocity and reflectivity data into the assimilation process. Experiment VrZPa is a combination of VrP and ZP, in which both the radial velocity and reflectivity in the precipitation regions ( $Z > 10$  dBZ) are assimilated, using the same procedure as in VrP and ZP. Compared to VrP (Fig. 6), when additional reflectivity data are introduced, the analyses of  $q_r$ ,  $q_s$ , and  $q_h$  are generally improved, especially for  $q_r$  and  $q_h$ , as indicated by lower errors after each analysis. The forecast error growth in this experiment is faster, however, even for those three variables directly related to  $Z$ .

The analysis errors of  $q_v$  and  $p'$  remain higher than those in VrP until 60 and 80 min, respectively, but become noticeably smaller afterward. For most of the assimilation period, the wind components are not as accurate as those retrieved by assimilating only  $V_r$ , but they can reach the same accuracy in the last few cycles.



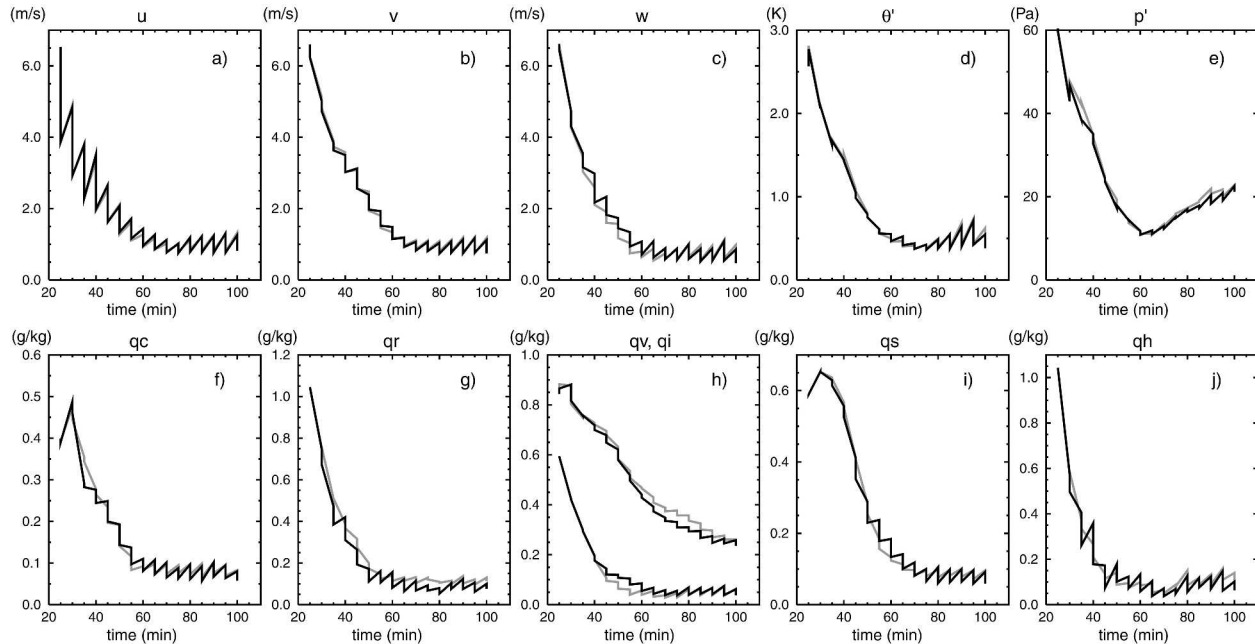


FIG. 7. As in Fig. 4, but for expt VrZPb (black) and expt VrP (gray).

For  $\theta'$ ,  $q_c$ , and  $q_i$ , the *analysis* errors from VrZPa are larger in the first two to three cycles, smaller in the next few, and then remain similar to those in VrP case.

The lack of significant positive impact by the inclusion of reflectivity data, especially during the first few assimilation cycles, is due to the reasons discussed earlier for ZP. In the first two to four cycles, background error covariances between reflectivity and the model variables that are not directly related to  $Z$  are not reliable. Updating these variables based on reflectivity data and the unreliable covariances hurts the analysis, as indicated by the increase of errors in  $w$ ,  $\theta'$ ,  $q_c$ , and  $q_v$  by, for example, the second analysis cycle (the error increase is actually rather bad for  $q_c$  and  $q_v$ ; see Fig. 6). The increased analysis errors lead to a less accurate forecast and faster error growth. Despite all of this, the analyses toward the end of the assimilation period are similar or better for most fields in VrZPa than in VrP, indicating the significant positive impact of  $Z$  when good error estimation becomes available. Interestingly, the degradation of the analysis in the early cycles by the assimilation of rainwater content is also noted by CSS, which includes warm rain microphysics.

We note that in Dowell et al. (2004), which employs warm rain microphysics, it is found that updating  $q_r$  only when assimilating reflectivity observations helps to maintain a realistic structure of the precipitation core and to improve the velocity verification score. We performed a corresponding experiment, VrZPb (black curves in Fig. 7), in which only  $q_r$ ,  $q_s$ , and  $q_h$  are updated when assimilating reflectivity. As was found in VrZPa, the *analyses* of  $q_r$ ,  $q_s$ , and  $q_h$  are improved over those of VrP. The analysis of  $q_v$  is also better. For most

of the other variables, the improvement over VrP is generally small, if any (Fig. 7). There are also a few cycles in which the retrieved  $w$  and  $q_i$  are not as good as those of VrP. Since it was shown earlier that reflectivity does have significant correlations with indirectly related variables (Fig. 5), we do not believe it appropriate to completely exclude those variables from the analysis update when assimilating reflectivity data. A better solution needs to be found.

From previous experiments, it can be seen that the negative impact of using reflectivity to update variables rather than  $q_r$ ,  $q_s$ , and  $q_h$  is mainly caused by the incorrect background covariances in the first two to three cycles. After that, the reflectivity becomes beneficial in retrieving those model fields. To see if we can further improve the analysis, in experiment VrZPc (Table 1), we apply the update due to reflectivity only to  $q_r$ ,  $q_s$ , and  $q_h$  before the fourth cycle. Starting from the fourth cycle, all model variables are updated. It is shown in Fig. 8 that doing so improves the analysis overall. The retrieved  $q_v$ , potential temperature and pressure are improved over VrP more than are those in experiment VrZPb. Significant improvement could also be found in  $q_c$  and  $q_s$ . For velocity components, the improvements are also slightly larger, especially in the later cycles.

The retrieved updraft and horizontal wind fields in the middle level are shown in Figs. 1m–1p. The detailed structures of the updrafts of the split cells starting from 60 min (Figs. 1n–1p) are retrieved better than those in either VrP (Figs. 1f–1h) or ZP (Figs. 1j–1l). At 80 and 100 min, the pattern and strength of the left mover, a less organized and therefore more difficult one to analyze, are clearly better retrieved by experiment VrZPc.

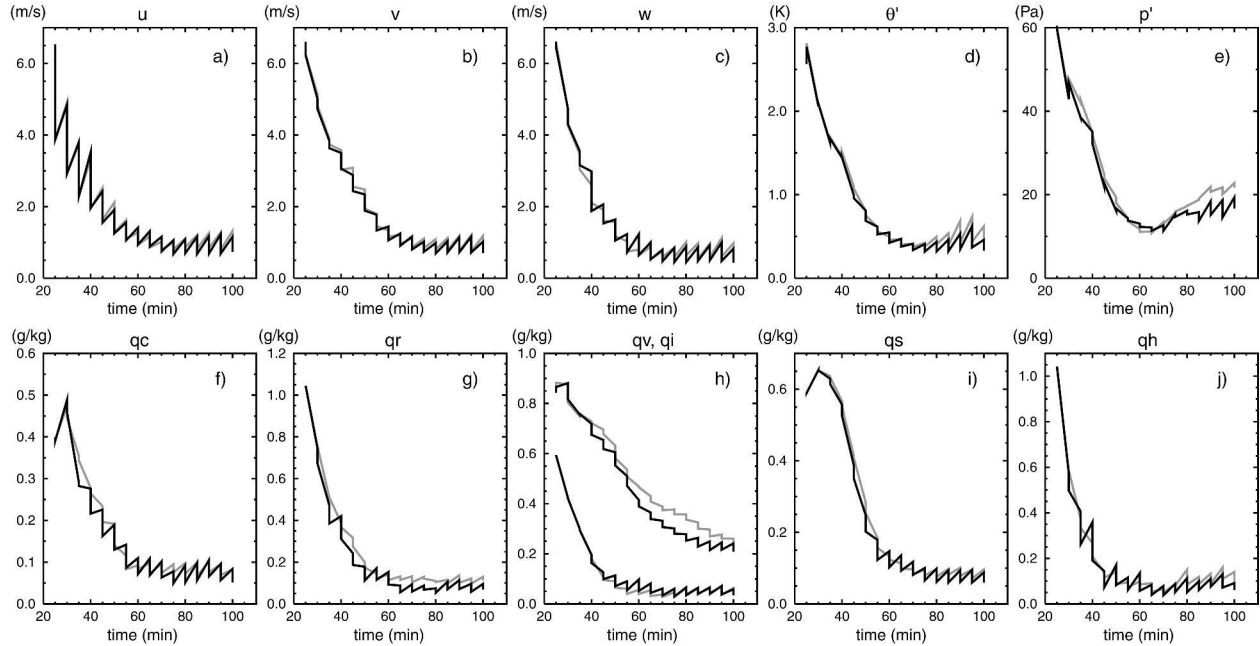


FIG. 8. As in Fig. 4, but for expt VrZPc (black) and expt VrP (gray).

Figure 2 shows the retrieved low-level cold pool, gust front, and precipitation pattern from different experiments, in terms of the low-level  $\theta'$ , wind vectors, and model-computed reflectivity. The benefit of using reflectivity data can be better seen from this figure. Without reflectivity data (VrP), the retrieved precipitation is much less, especially during the early cycles. Spurious echoes are found in the clear-air region in both cases but much less so in VrZPc (Fig. 2). They are related to spurious cells in individual ensemble members. The assimilation of reflectivity data reduced the spurious echoes.

In the previous experiments, only reflectivity larger than 10 dBZ is assimilated. In reality, reflectivity outside the precipitation regions also contains valid information. At least it indicates the absence of precipitating particles there. One can therefore assume that the reflectivity data cover the entire region within the radar range, which in our current case means the entire computational domain. In our next OSSE, named VrPZF (Table 1), reflectivity information is available everywhere while radial velocity data remain available in precipitation ( $Z > 10$  dBZ) regions only. As in VrZPc,  $u$ ,  $v$ ,  $w$ ,  $\theta'$ ,  $q_v$ ,  $q_c$ , and  $q_i$  are updated starting from the fourth cycle when assimilating reflectivity while  $q_r$ ,  $q_s$ , and  $q_h$  are updated from beginning.

The complete coverage of the reflectivity data can remove spurious cells that would otherwise develop in the data-void regions. The rms analysis errors in VrPZF (Fig. 9, thin black curves) are decreased more over those in VrP or VrZPc (Fig. 8). The retrieved horizontal wind fields, the strength of the updraft (Fig. 1), the low-level perturbation potential temperature (Fig. 2),

and the microphysical fields (Fig. 3) are more accurate than those retrieved by any of the previous experiments. The reflectivity computed from the analysis (Figs. 2m–p) very closely resembles that in the truth simulation with no spurious echoes found in the clear-air region. Toward the later period of the assimilation, the strength of the low-level cold pool can be retrieved very well by all three of the experiments (Fig. 2). However, only when complete reflectivity data coverage is used, as in the case of VrPZF, can the extent of the low-level rain-cooled air, as indicated by the 0-K contour of the perturbation potential temperature, be accurately determined. This is actually very important for the subsequent forecast as spurious cooling in the inflow region is found in some cases to reduce the CAPE in the inflow and adversely affects the evolution of ensuing forecast. Experiment VrPZF produces the best forecast (more later) among all of the assimilation experiments, for this and other reasons.

Finally, we briefly discuss the ensemble spread, which is defined as the square root of the ensemble variance and plotted in Fig. 9 for experiment VrPZF. Since EnKF estimates the forecast error using the ensemble spread, in an ideal situation, the ratio of the spread of the ensemble to the error of the ensemble mean forecast is equal to  $\sqrt{N_e/(N_e + 1)}$  (Murphy 1988). As we can see from Fig. 9, the ensemble spread gradually approaches the ensemble mean forecast error for most variables, a favorable sign. During the early cycles, the ensemble spread is much smaller than the rms error and therefore provides a poor representation of the forecast error, a behavior also observed by Snyder and Zhang (2003). The ratio increases rapidly dur-

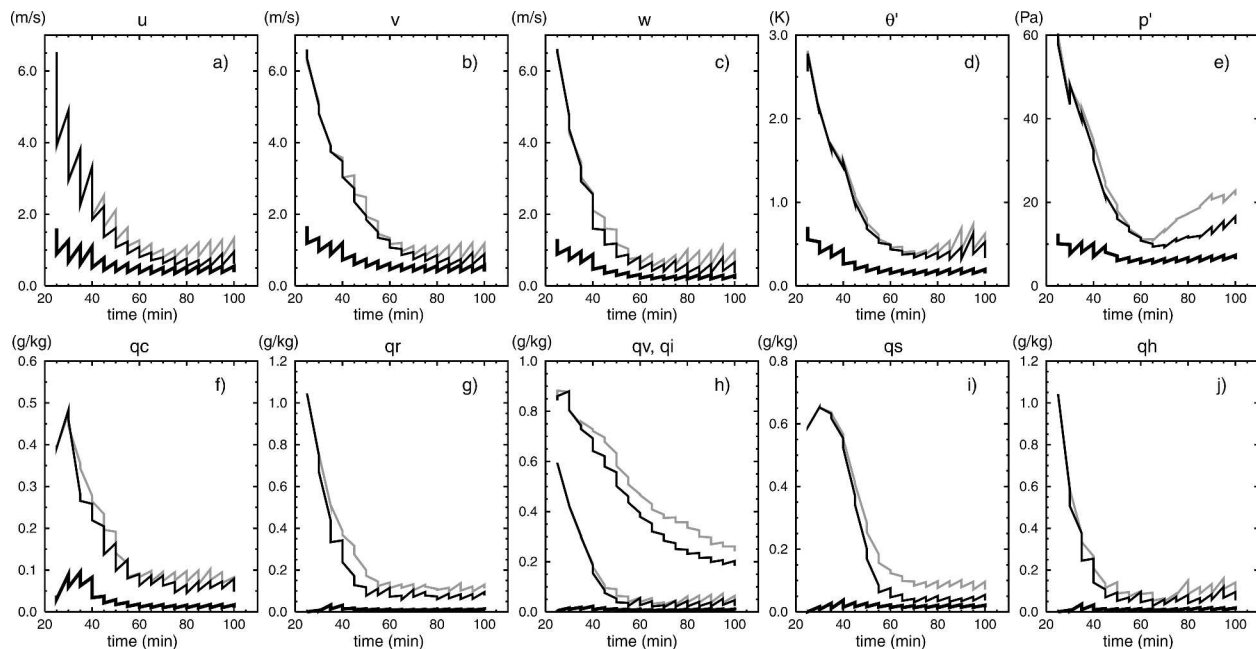


FIG. 9. As in Fig. 4, but for expt VrPZF (thin black curves) and expt VrP (thin gray curves). The additional thick black curves are for the analysis and forecast ensemble spread of VrPZF, and the spread is calculated only at the points where reflectivity is greater than 10 dBZ, as the errors are.

ing the first six to eight cycles for most variables (mainly because of the rapid decrease in forecast errors) then becomes more stable. In the last four or so cycles, this ratio starts to decrease again, especially for  $u$ ,  $v$ ,  $w$ ,  $\theta'$ , and  $p'$ . Such a decrease is typically observed as EnKF goes through successive assimilation cycles (e.g., Houtekamer and Mitchell 1998) owing to a systematic underestimation of the analysis variance. In our case, this decrease in the later cycles is mainly due to the faster error growth in the forecast rather than to a change in the ensemble spread; in fact, the ensemble spread remains essentially constant in the later cycles. The faster forecast error growth is, we believe, due to the more transient nature of the flow after the storm went through more than two splits. Snyder and Zhang (2003) noted, however, a continued increase in the spread-to-error ratio, and attributed the increase to the presence of spurious cells in individual members. Similar behavior is also observed in our experiment, VrP, in which spurious cells are not as effectively suppressed as they are in VrPZF. We further note that in the last few cycles of VrPZF, despite the increased forecast errors (Fig. 9), the analysis errors do not increase or increase very little, indicating that the filter is well behaved.

#### d. Retrieval of microphysical fields

The microphysics retrieval is an important aspect of convective-scale data assimilation. Relatively few previous data assimilation studies have focused on this problem. Most of these studies used only a simple mi-

crophysical parameterization and the ice phase is usually excluded. The more recent attempt of Wu et al. (2000) uses a 4DVAR system to assimilate dual-polarization radar data into a cloud model. Generally, a good bulk ice microphysics parameterization includes ice categories for cloud ice (individual crystals), snow (aggregates), and graupel and/or hail. As pointed out by Wu et al. (2000), such a model will have a complex adjoint model involving many nonlinearities, and the 4DVAR system based on such an adjoint tends to have poor convergence properties. For these reasons, Wu et al. (2000) made simplifications by using a scheme without the snow category and by merging the cloud water and cloud ice categories. Such simplifications reduce the degrees of freedom (or the number of control or analysis variables), and also reduce the number of, usually highly nonlinear, microphysical processes. In addition, in Wu et al. (2000), the reflectivity and differential reflectivity data are converted first to rain and hail mixing ratios before assimilation, rather than being assimilated directly. The differential reflectivity data are necessary for such a conversion.

In our study, the original detailed ice microphysics parameterization of Lin et al. (1983) is used and only standard reflectivity is assumed to be available. As a result, our problem is more difficult because more water and ice species have to be determined and no dual-polarization information is available. Yet, the EnKF scheme does not seem to have any serious difficulty. Figure 3 shows the distribution of the perturbation water vapor and five categories of water substances for the



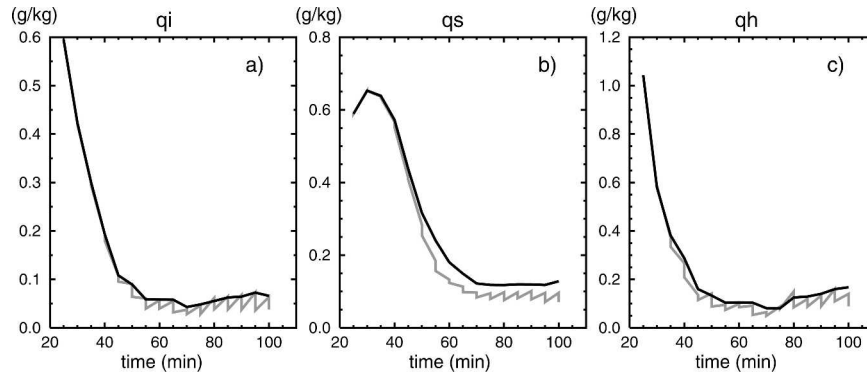


FIG. 10. Rms error of (a)  $q_i$ , (b)  $q_s$ , and (c)  $q_h$  for VrP (gray) and VrPnoIce (black).

truth run and for selected assimilation experiments. It can be seen that the EnKF data assimilation system is able to establish detailed microphysical structures that have very high fidelity. The quality of the actual analysis does depend on the usage and availability of the data, as indicated quantitatively by the error plots discussed earlier.

To better understand the way the EnKF scheme works and the role of updating microphysical fields, we performed another experiment, named VrPnoIce, in which ice variables  $q_i$ ,  $q_s$ , and  $q_h$  are not updated by the analysis and only radial velocity in the precipitation regions is assimilated. The differences in error between VrPnoIce and VrP start to show with the third cycle and increase with successive cycles (Fig. 10). It can be seen that without the analysis update to these three variables, the rms error of the  $q_s$  analysis is greater than even that of the ensemble-mean forecast of experiment VrP. The  $q_s$  field at 60 min [Fig. 3e(3)] exhibits larger spatial coverage in VrPnoIce and is less accurate than that of VrP [Fig. 3e(2)]. The smaller difference in the earlier period reflects a relatively weak link (through background error covariance) between  $V_r$  and these three variables. The link apparently becomes stronger and more effective in correcting errors in these fields at the later stage (as in the case of VrP). On the other hand, despite the lack of direct correction in VrPnoIce to  $q_i$ ,  $q_s$ , and  $q_h$ , the errors in these fields are still reduced with time in general. Such reductions are achieved through model dynamics; when other model fields are improved, fields that are not directly updated have to adjust and become consistent with these fields. This points to the power of model-based dynamic data assimilation methods.

Further comparison of VrP and ZP helps us understand the interactions between the analyses of different variables. We see from Fig. 4, that the errors in the wind, temperature, and pressure fields remain much higher in the ZP case than in VrP for almost the entire assimilation period, with the differences being largest during the earlier cycles. During this early period, the assimilation of the reflectivity data in ZP is very effective

in reducing errors in  $q_h$ ,  $q_s$  as well as in  $q_r$  while the generally poor analysis of the other fields is causing rapid increases in the forecast error. We note here that the fact that  $q_r$ ,  $q_s$ , and  $q_h$  are directly related to  $Z$  does not guarantee a good retrieval of them because without the help of the error covariances offered by the EnKF scheme, the problem is underdetermined. When reflectivity data are combined with radial velocity data, very accurate microphysical fields can be retrieved (Figs. 2 and 3). With  $V_r$  data only (the case of VrP), the maximum value of  $q_h$  in Fig. 3f(2) is  $5.73 \text{ g kg}^{-1}$  at 60 min while the true value is  $6.63 \text{ g kg}^{-1}$ . If the ice hydrometeors are not updated when assimilating  $V_r$  (experiment VrPnoIce), the maximum is larger than  $1 \text{ g kg}^{-1}$  smaller than the truth. The addition of the full-coverage reflectivity data [Fig. 3f(5)] yields a maximum value of  $6.37 \text{ g kg}^{-1}$  that is closer to the truth.

#### 4. Forecasts from ensemble-mean analyses

Since the goal of data assimilation is to provide a good initial condition for numerical weather prediction, in this section we look at the quality of forecasts produced from the analyses. Figure 11 shows the truth and two forecasts over a 130-min period that are initialized from the ensemble-mean analyses from experiments VrP and VrPZF at 80 min. Within the first 20 min (from 80 to 100 min), the forecast of VrPZF maintains most details of the storm very well, including the strength, structure, and location of the updraft and the further splitting of the left mover. Within the first hour of forecast, the position of the right mover is forecast very accurately by experiment VrPZF. After that, the center of the right-moving cell is displaced about 4–8 km eastward during its southeastward propagation. The forecast beginning from VrP roughly captures the evolution of the storm but not as accurately as in VrPZF. The right mover propagates southeastward even faster than in VrPZF and reaches the southern boundary earlier; at 210 min, the structure of the forecast storm is rather different from that of the true one.

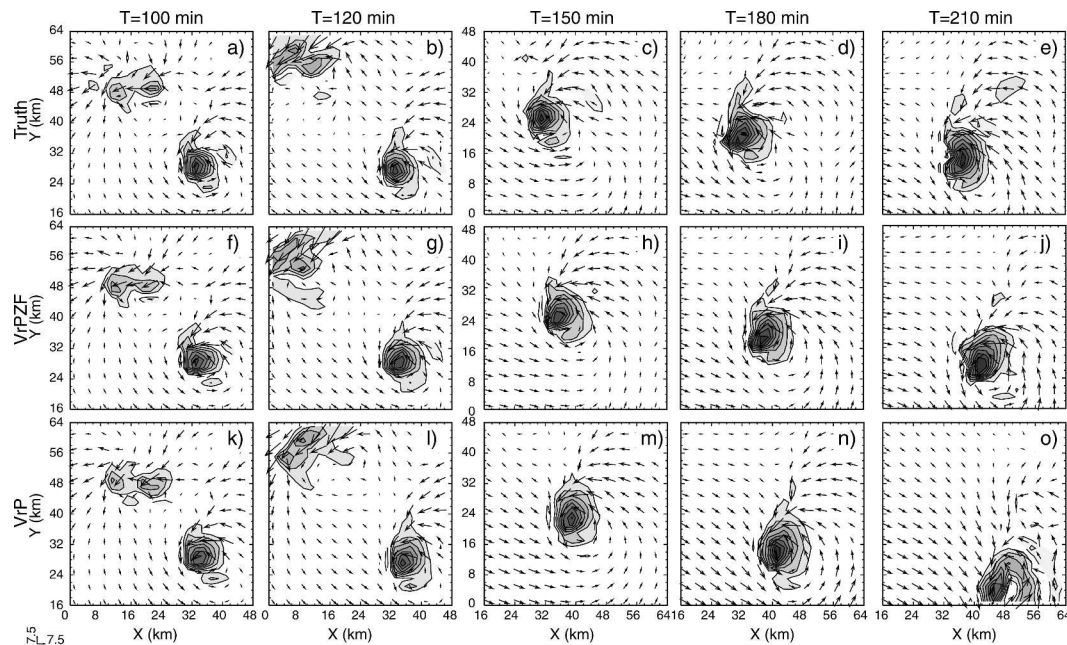


FIG. 11. Vertical velocity (contours and shading at intervals of  $4 \text{ m s}^{-1}$ ) and horizontal wind perturbation (vectors;  $\text{m s}^{-1}$ ) at the 6-km level for (a)–(e) the truth simulation and the forecast beginning from the ensemble-mean analysis at  $t = 80 \text{ min}$ ; (f)–(j) forecast from ensemble-mean analysis of VrPZF, and (k)–(o) forecast from ensemble-mean analysis of VrP. Note the difference in the plotting domains before and after 150 min.

Figure 12 shows the rms errors (averaged over the entire domain) of forecasts beginning from the ensemble-mean analyses of different times from experiments VrP and VrPZF. Generally, a more accurate estimate of the initial condition yields a better forecast. It can be seen in Fig. 12 that for all these forecasts, within the first 80 min, both the forecast error and the forecast error growth rate of VrPZF (black thick curves) are smaller than those of VrP (gray thin curves). For the forecasts starting from 80 min, a large difference is seen in rainwater at around 120 min between the forecast errors of these two experiments (Fig. 12c). Within the first 40 min of forecast, the  $q_r$  forecast error in VrP grows much faster than in VrPZF. The low-level rainwater was overforecast by experiment VrP. For example, at 105 min, the maximum value of the forecast rainwater at 250 m AGL is  $8.54 \text{ g kg}^{-1}$  for experiment VrP, while that of the truth is only  $5.91 \text{ g kg}^{-1}$  (not shown). The low-level rainwater was also overforecast by experiment VrPZF, but not by as much. The forecast distribution of the rainwater in VrPZF is always closer to the truth than in VrP. The comparison of the forecast errors of these two experiments further verifies the benefit of assimilating reflectivity data in both precipitation and clear-air regions. For forecasts starting from the ensemble-mean analysis of VrF (not shown here), the errors are smaller than those of VrP, but generally bigger than those of VrPZF within the 80 min of the forecast.

We note that for the forecasts starting from 100 min,

the errors of VrPZF grow faster after 175 min and eventually become larger than those of VrP. This is found to be mainly associated with the slower south-eastward propagation of the forecast storm in VrPZF than in the true storm. Usually, phase error increases with the length of the forecast. In this case, the center of the updraft forecast by experiment VrPZF is located 2–8 km, or one to four grid intervals, north of the true storm during the last 50 min. The center of the updraft in VrP is closer to the true storm during the later forecast period. However, within the last 20 min, phase error also occurs within VrP. The forecast storm moves faster than the true storm and the center of the updraft becomes displaced by 2–4 km to the south of the true storm. Still, the storm structure in VrPZF is better than that in VrP at this stage.

The success of the forecast depends not only on the accuracy of the analysis of the storm, but also on the analysis of the storm environment. In our initial tests, in which the boundary zone is perturbed at the initial time of ensemble forecast, we obtained similarly good analyses. However, the forecasts from some of these analyses deteriorated quickly with time. In a forecast starting from analysis at 100 min, the right mover quickly decays and moves northeastward. We found in that case the low-level air was drier and the CAPE was reduced in the storm inflow region. Spurious cells triggered near the boundary in individual ensemble members contributed to this. Not perturbing the boundary at the initial time and the use of zero reflectivity information outside

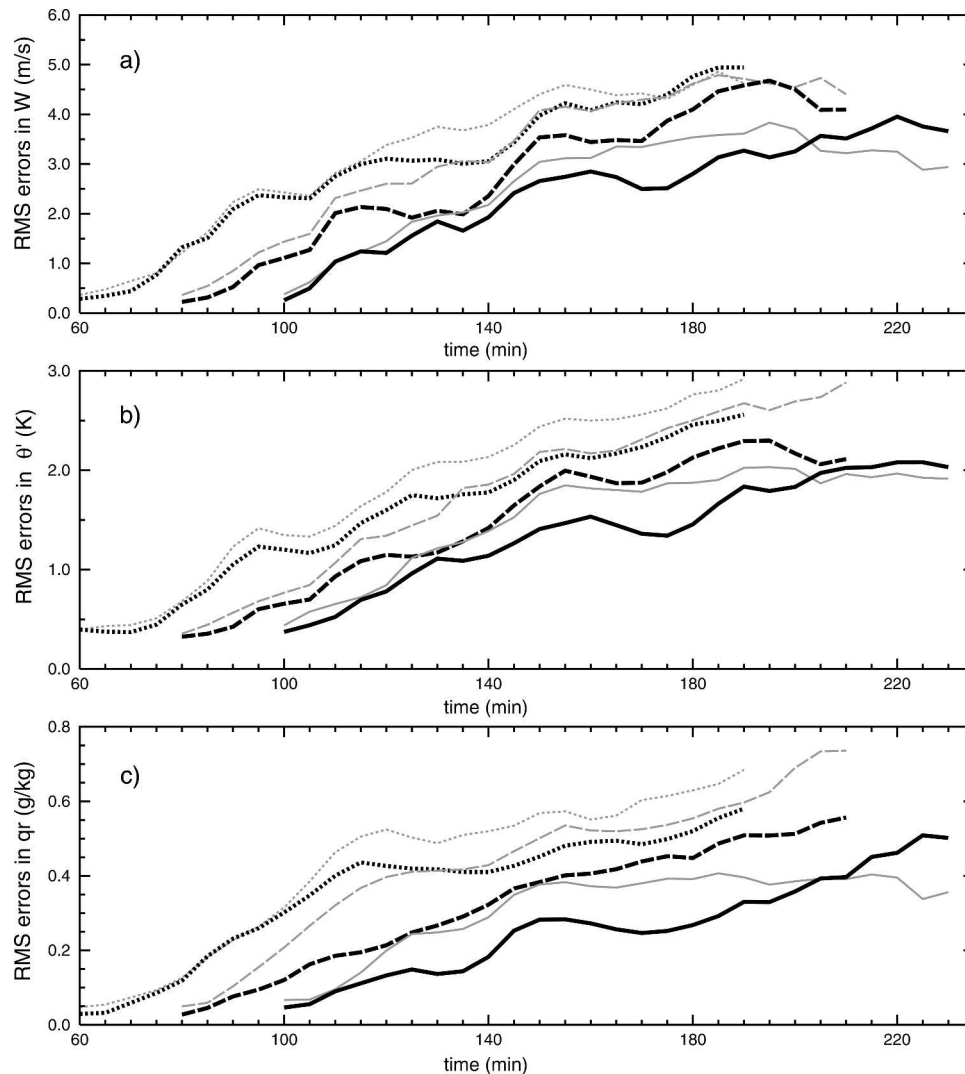


FIG. 12. The rms errors of the forecasts averaged over the entire domain for (a)  $w$  ( $\text{m s}^{-1}$ ), (b)  $\theta'$  (K), and (c)  $q_r$  ( $\text{g kg}^{-1}$ ). The forecasts begin from the ensemble-mean analysis at  $t = 60$  min (dotted),  $t = 80$  min (dashed), and  $t = 100$  min (solid) of expt VrP (gray thin curves) and expt VrPZF (black thick curves).

the precipitation regions helped alleviate the problem. For general applications, other means and data should be employed to ensure a good analysis of the storm environment, which for prediction purposes appears to be at least as important as the analysis of the storms themselves.

## 5. Summary and discussion

In this study we applied the ensemble Kalman filter technique to the assimilation of simulated radar radial velocity and reflectivity data, using a compressible model with a complex multiclass ice microphysics scheme. The inclusion of a complex multiclass ice microphysics scheme has not been done before in either

EnKF or 4DVAR assimilation of radar data. Doing so introduces additional model state (ice microphysics) variables that impose additional challenges to the retrieval problem. Previously published EnKF research did not carefully examine the impact of assimilating reflectivity data either, nor has attention been paid to the analysis quality of microphysical variables. Our work also represents the first time that a compressible model is used in the context of EnKF assimilation at the cloud scale.

The EnKF method is shown to have great potential for the assimilation of such data and for thunderstorm prediction. Although the observation operator for the reflectivity data is nonlinear, which may lead to non-Gaussian error distribution and violate the basic as-



sumptions of the Kalman filter algorithm, direct assimilation of reflectivity data is shown to provide positive impacts overall on the analysis and subsequent forecast.

Flow-dependent forecast error covariances estimated from the ensemble states play a critical role in the assimilation process. Through them not only can the wind and thermodynamic fields be retrieved accurately, all five categories of cloud and hydrometeor variables can also be retrieved successfully. Compared to 4DVAR, the EnKF is a much easier yet effective method for obtaining microphysical fields that are compatible with the model dynamics, thermodynamics, and microphysics. Compared to early efforts that insert radar observations directly into numerical models without the use of covariance information (e.g., Liou et al. 1991), the EnKF method enjoys much greater success. The importance of spatial covariance information is further supported by the fact that a worse analysis is obtained when the effective radius of the covariance localization is too small (results not shown).

Reliable and dynamically consistent multivariate covariances between the observed quantities and the state variables not directly related to them can be obtained after a few assimilation cycles, even when the ensemble is started from initial guesses made up of an environmental sounding plus random perturbations. Spatial covariance structures are shown to be dynamically consistent. After the initial two to three cycles, useful observational information can be spread in space and to indirectly related variables. Delaying the update of indirectly related variables until after the first few cycles when assimilating reflectivity data, produces the best analysis. Using reflectivity information in clear-air regions is very beneficial in suppressing spurious storms (assuming that the radar network provides a complete spatial coverage). The forecast initiated from the ensemble-mean analysis using  $V_r$  and full coverage reflectivity data is shown to be the best within about 80 min of all three forecasts presented. We should point out here that if the EnKF assimilation system is run in a continuously cycled mode, as an operational system should be, or if the ensemble is initialized in a more physical way, such as using the breeding method (Toth and Kalnay 1997), then the delay in updating indirectly related variables may not be necessary.

The EnKF data assimilation results reported here used 100 ensemble members. We found that 40 ensemble members are enough to produce good analysis results, except that the filter convergence rate is a little slower. With 40 members, the radius of the data influence region needs to be smaller. A radius of 6 km is found to produce the best results in this case.

Snyder and Zhang (2003) noted that the results of their EnKF experiments were subject to some random variability associated with the specific realizations of the initial ensemble and observation errors. In this study, we have repeated some of the experiments with different realizations and we did not notice any signifi-

cant deviation from the results reported here in terms of the error characteristics. The larger ensemble size used here may account for some of the reduced variability.

For larger applications, the analysis algorithm needs to be parallelized for distributed-memory parallel platforms. For our current application, we used shared-memory parallelization via OpenMP for the computation of the background error covariance  $\mathbf{P}^T$ , which is the most expensive part of the algorithm. Four IBM Regatta (model p-690) processors give a speedup of 3.5 for the analysis. The ensemble forecasts were distributed among a number of processors.

Finally, we note that caution should be used when interpreting OSSE results. Both forecast model and forward observation operators are assumed perfect in the current work. The effects of model error need to be studied in the future. Much work is still needed in moving us in the direction of real case and real data. We also mention that a similar set of assimilations using square-root EnKF, which does not perturb the observations (as used in, e.g., Snyder and Zhang 2003), has also been conducted with generally similar conclusions.

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