

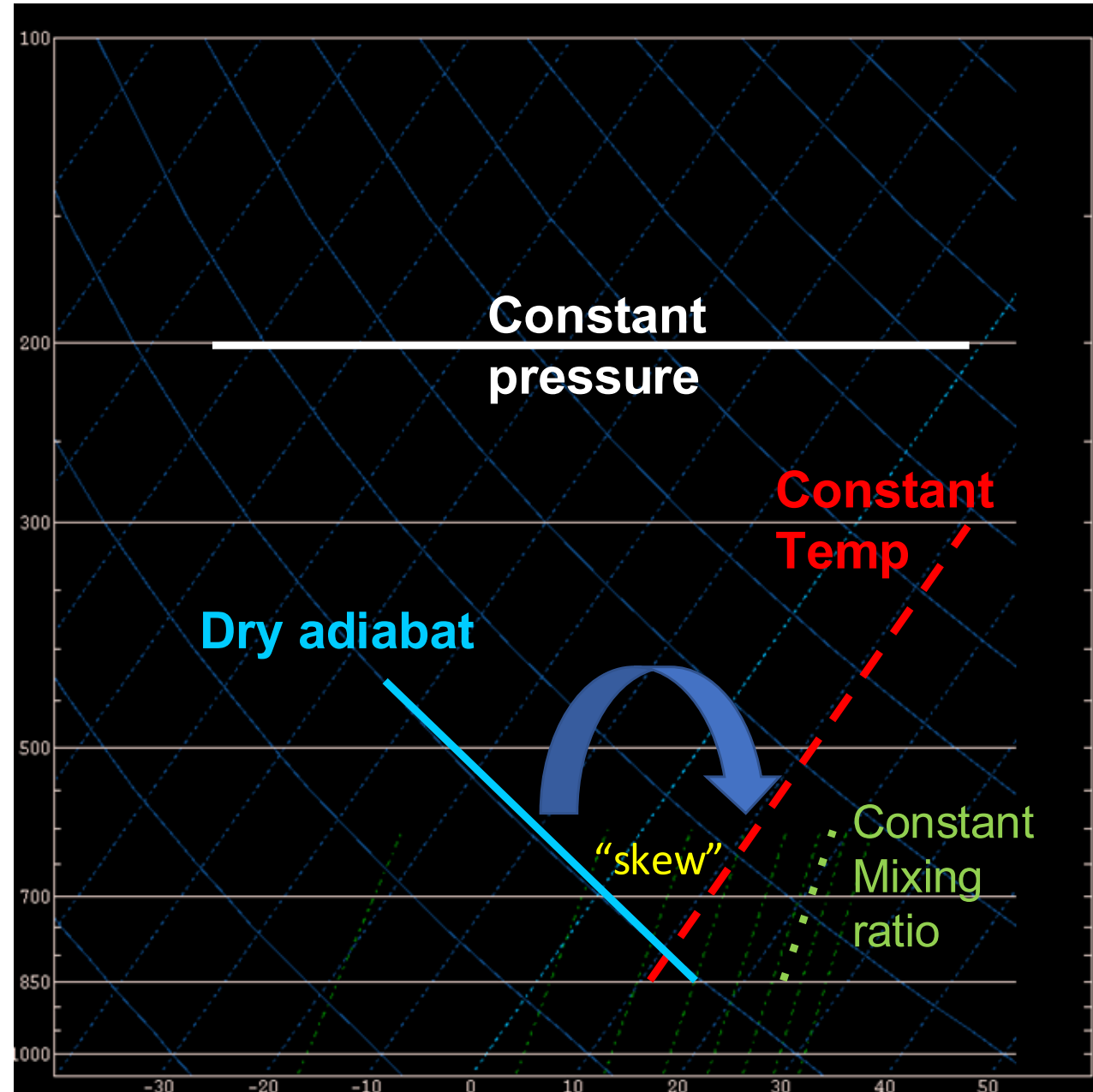
Skew-T Diagram Basics

METR 4403/5403

Material originally prepared by Rich Thompson

Updated by Andrew Lyons, Andrew Moore

Raw SkewT-log P diagram

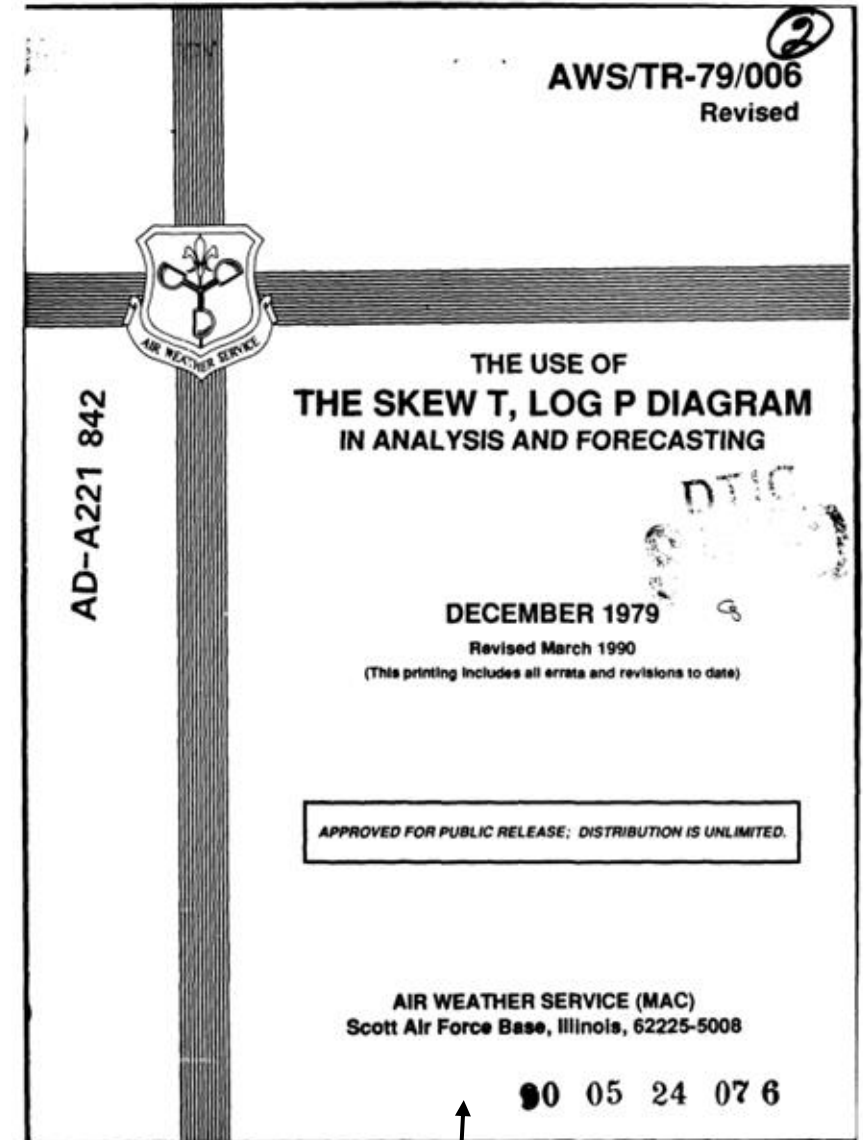


Features of note in SkewT log P

- Temperature is **skew**ed about 90° from the dry adiabats
- **P**ressure decreases as a **log**arithm of height (faster at bottom than top)
- Mixing ratio crosses over temperature lines
 - It's a function of pressure, which is why the same dew point temperature at higher elevation contributes more to buoyancy
- One thing missing is a plot of saturated parcel ascent

Common Sounding Terms

- **LCL** – lifting condensation level
- **LFC** – level of free convection
- **EL** – equilibrium level
- **CAPE** – buoyancy (positive area)
- **CIN** – convective inhibition (negative area)
- Autoconvective Lapse Rate (34.2 C/km)
- Convective Temperature
- Virtual Temperature
- Potential Temperature
- Equivalent Potential Temperature
- Lifted Index

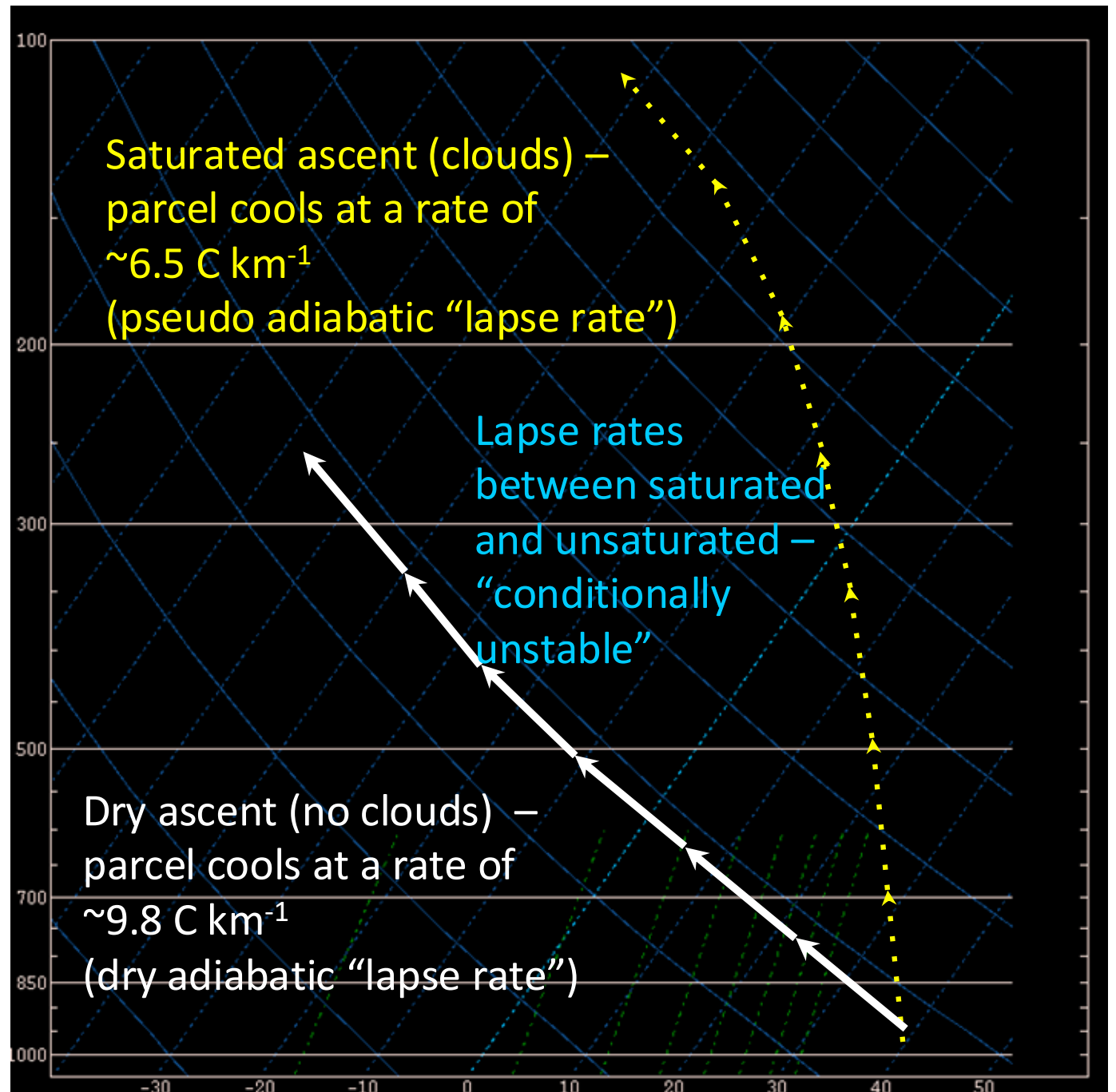


A tremendous resource!

Adiabatic Motion

In parcel theory it is assumed that parcel motions are adiabatic processes - that is parcel exchange no energy/mass with their environment (not true!).

This also means their paths are predictable along lines of constant entropy (isentropes).

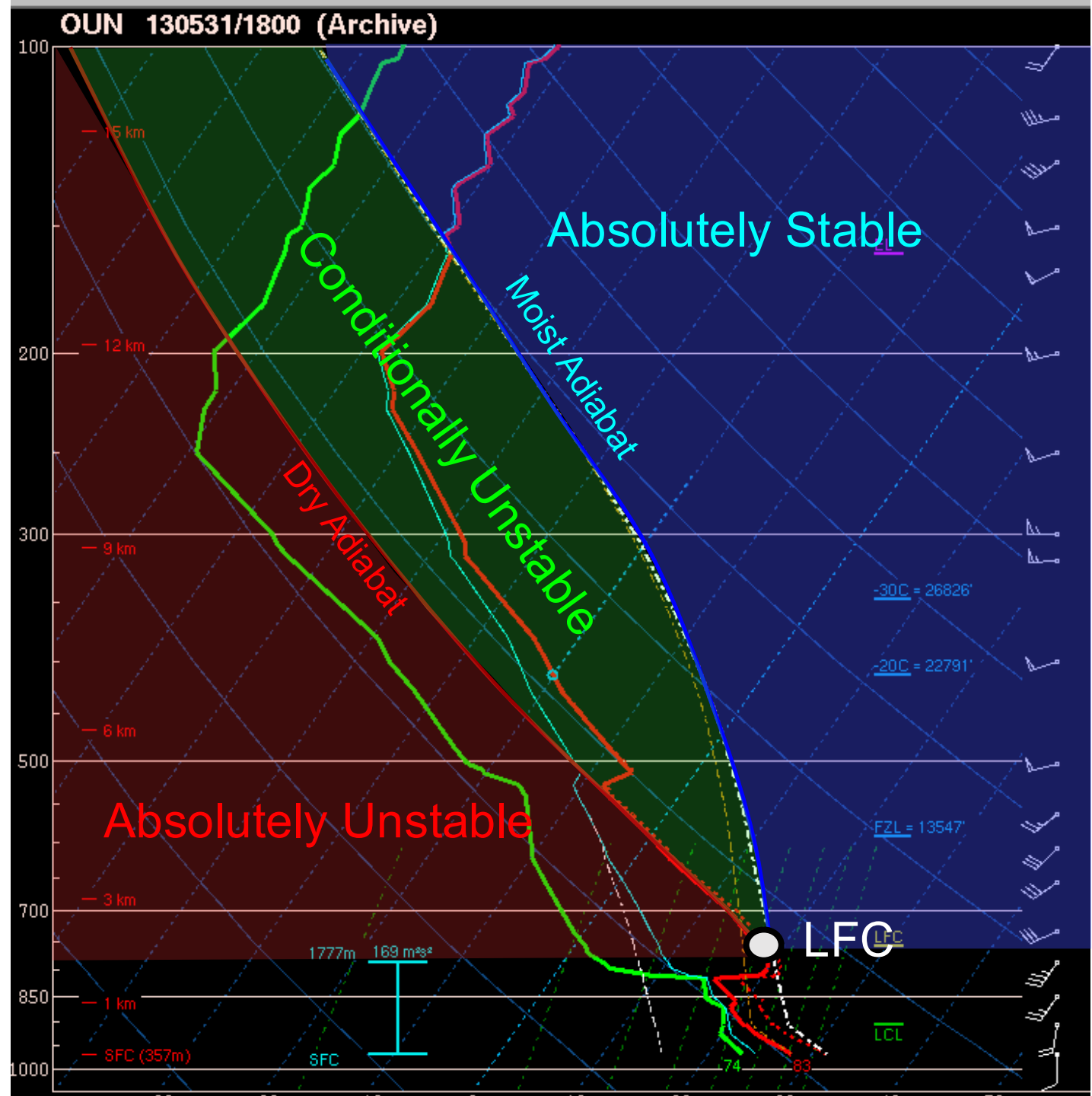


Lapse Rate

A lapse rate is simply the change in temperature over some depth (dT/dz)

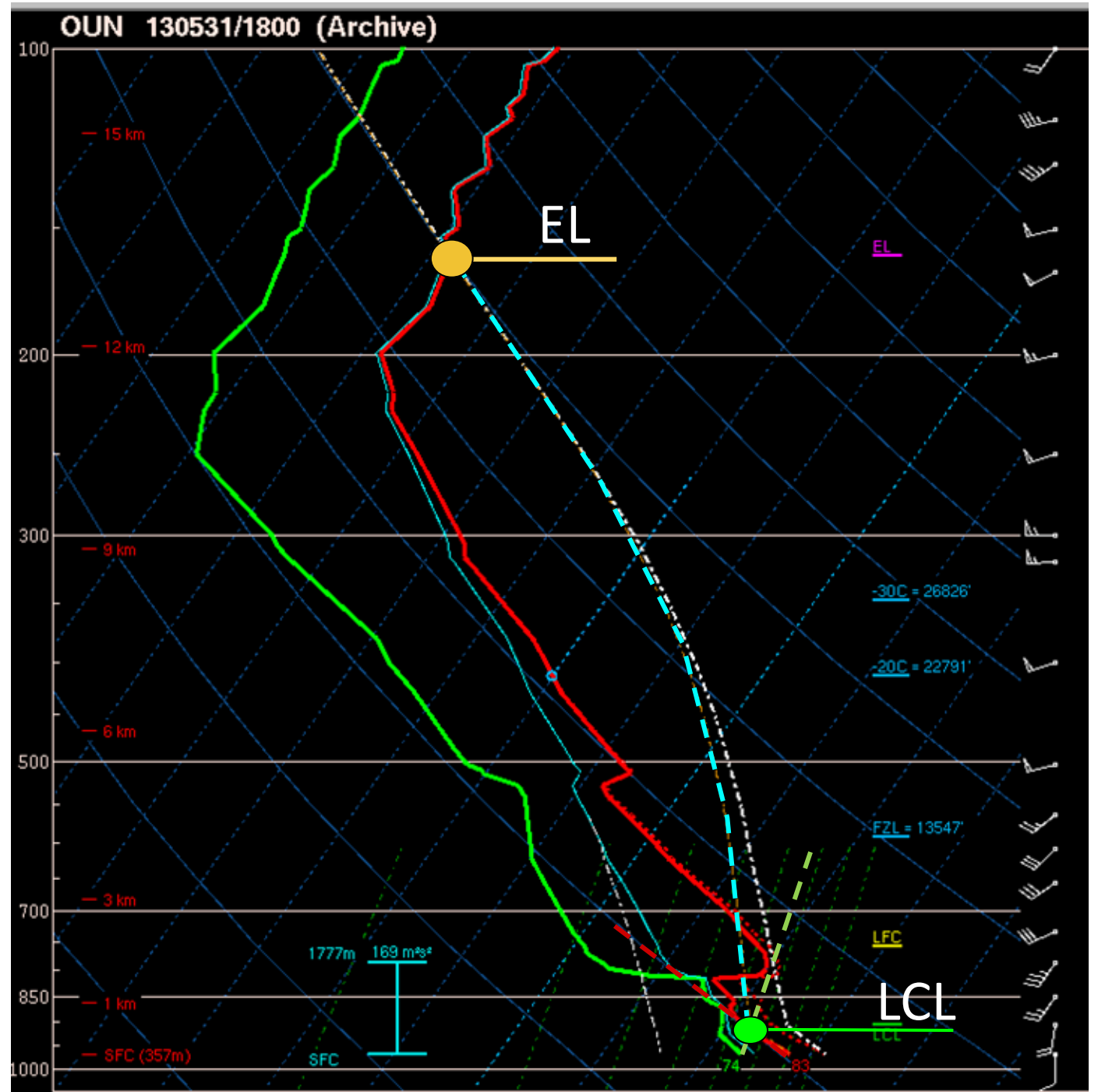
Lapse rates in most T-storm environments will be conditionally unstable...

In other words, between the dry adiabatic lapse rate (9.8 C/km) and the moist adiabatic lapse rate (~6.5 C/km).



Lifting a Parcel

- 1) Choose a parcel (sfc, mixed layer, most-unstable, etc...)
- 1) Find temperature and dewpoint.
- 1) Assume dry adiabatic ascent until you reach **Lifted Condensation Level (LCL)**.
- 1) Assume moist adiabatic ascent until you reach the **Equilibrium Level (EL)**.



Buoyancy Basics

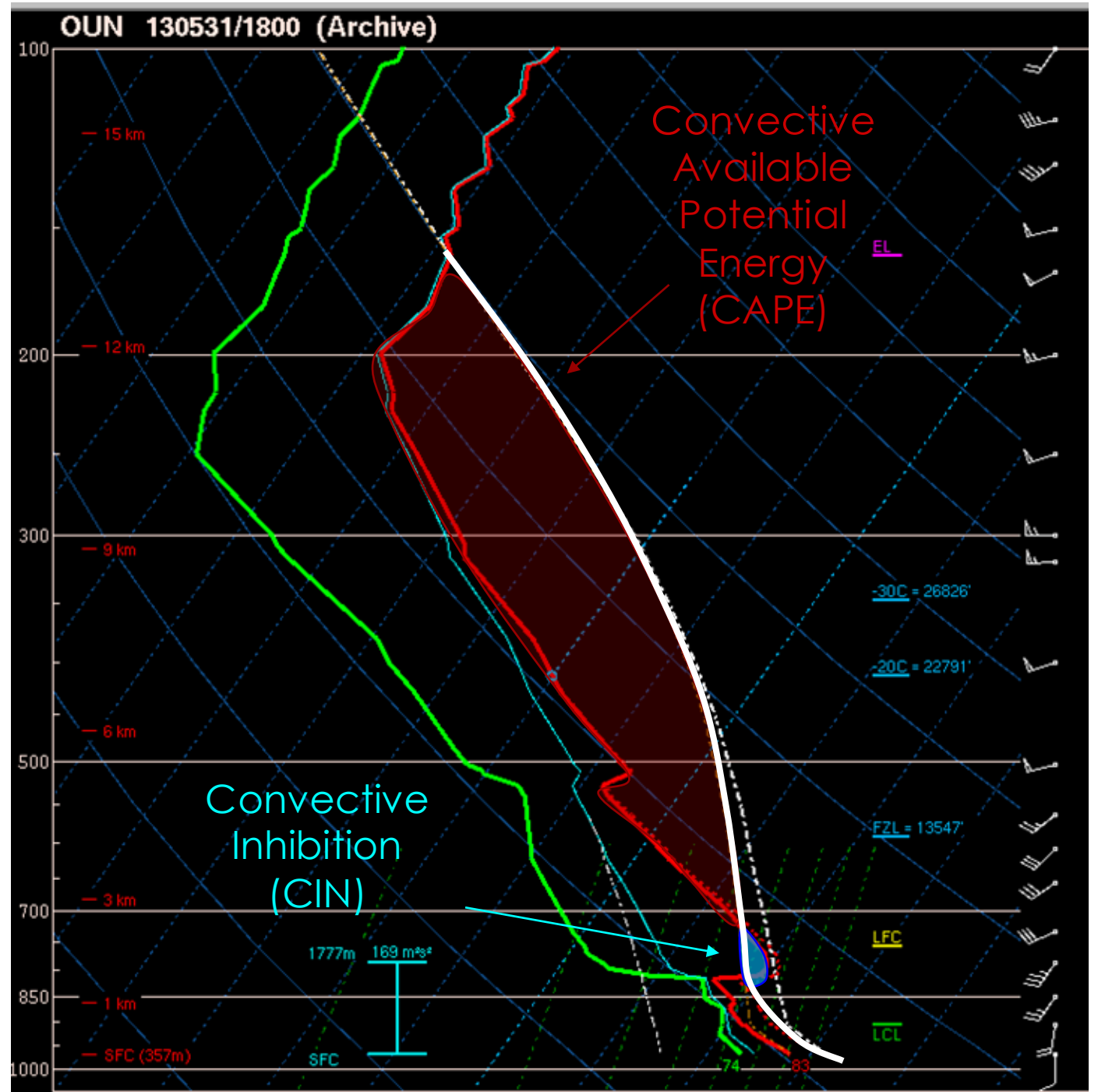
If parcel temperature > ambient temperature:
Buoyancy > 0
Parcel accelerates upwards

If parcel temperature < ambient temperature:
Buoyancy < 0
Parcel accelerates downward

If parcel temperature = ambient temperature:
Buoyancy = 0
Parcel experiences no buoyant forces
(either continues in direction of
motion or remains motionless)

From ideal gas law:

$$B = -g \frac{\rho'}{\bar{\rho}} = g \left(\frac{T_v'}{\bar{T}_v} - \frac{p'}{\bar{p}} \right)$$



Lifted Index

A more simplistic way to quantify buoyancy of a parcel.

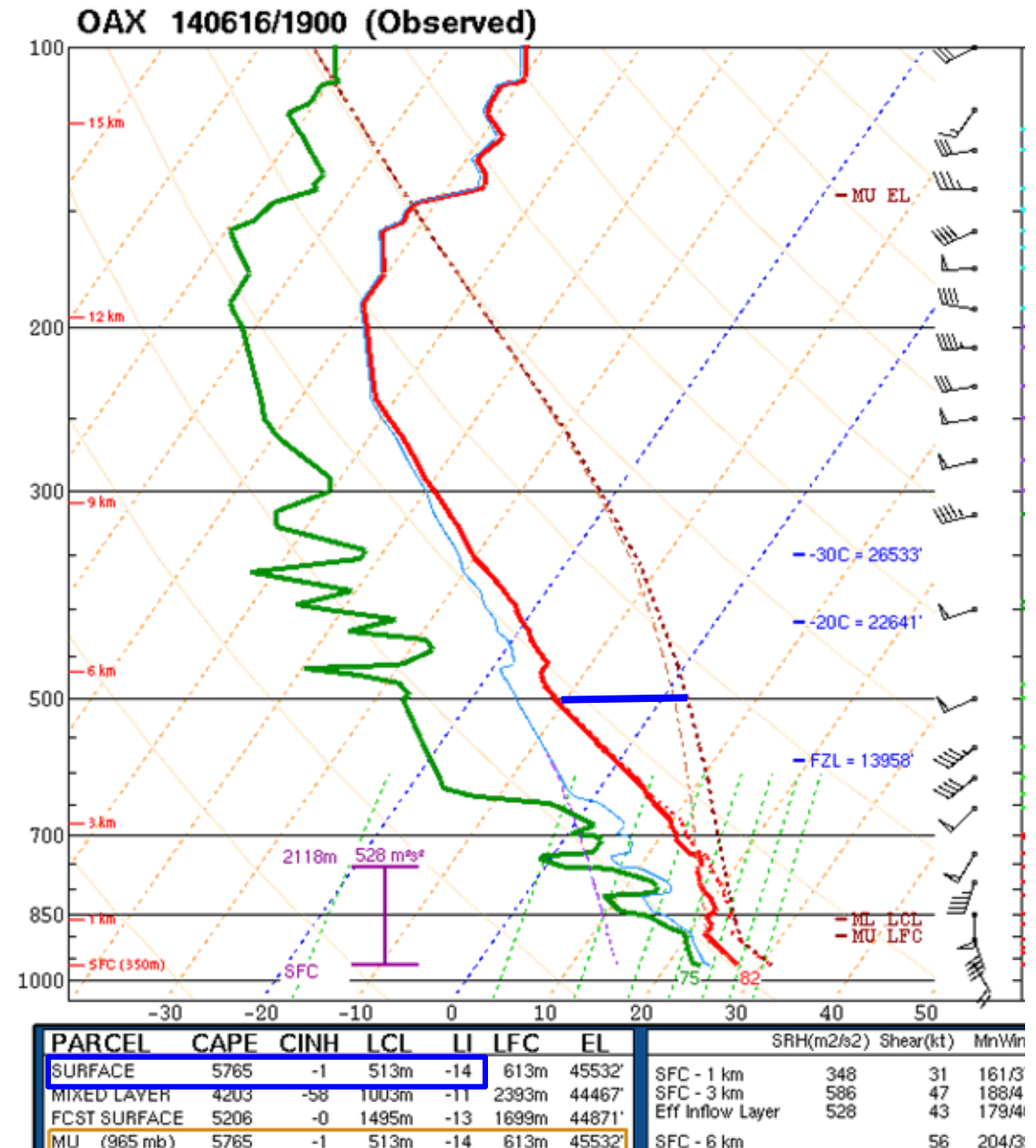
- 1) Lift a parcel from the surface (or whatever level you want)
- 2) Find the temperature of the parcel at 500 mb
- 3) Find the environmental temperature at 500 mb
- 4) $LI = \text{Env Temp } 500 \text{ mb} - \text{Parcel Temp } 500 \text{ mb}$

LI > 0 = Stable!

-1 to -4 = Weakly unstable

-5 to -9 = Very unstable

-10 and lower = Extremely unstable!



Lifted Index

A more simplistic way to quantify buoyancy of a parcel.

Pros:

- Very simple to calculate and interpret!
- Implicitly accounts for lapse rates!

Cons:

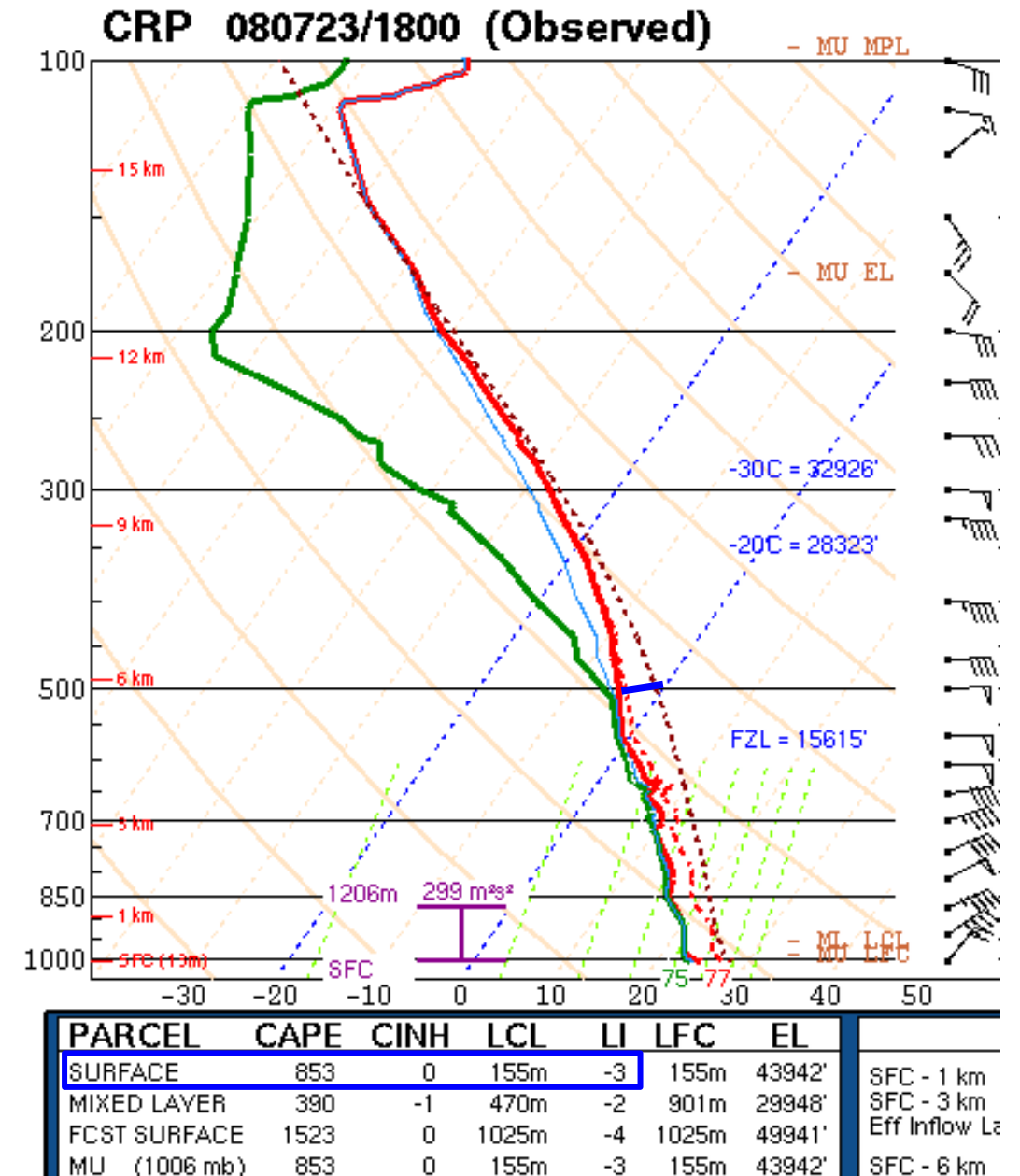
- Very simplistic.
- May miss critical buoyancy (e.g. elevated buoyancy)

$LI > 0$ = Stable!

-1 to -4 = Weakly unstable

-5 to -9 = Very unstable

-10 and lower = Extremely unstable!



Downdraft CAPE (DCAPE)

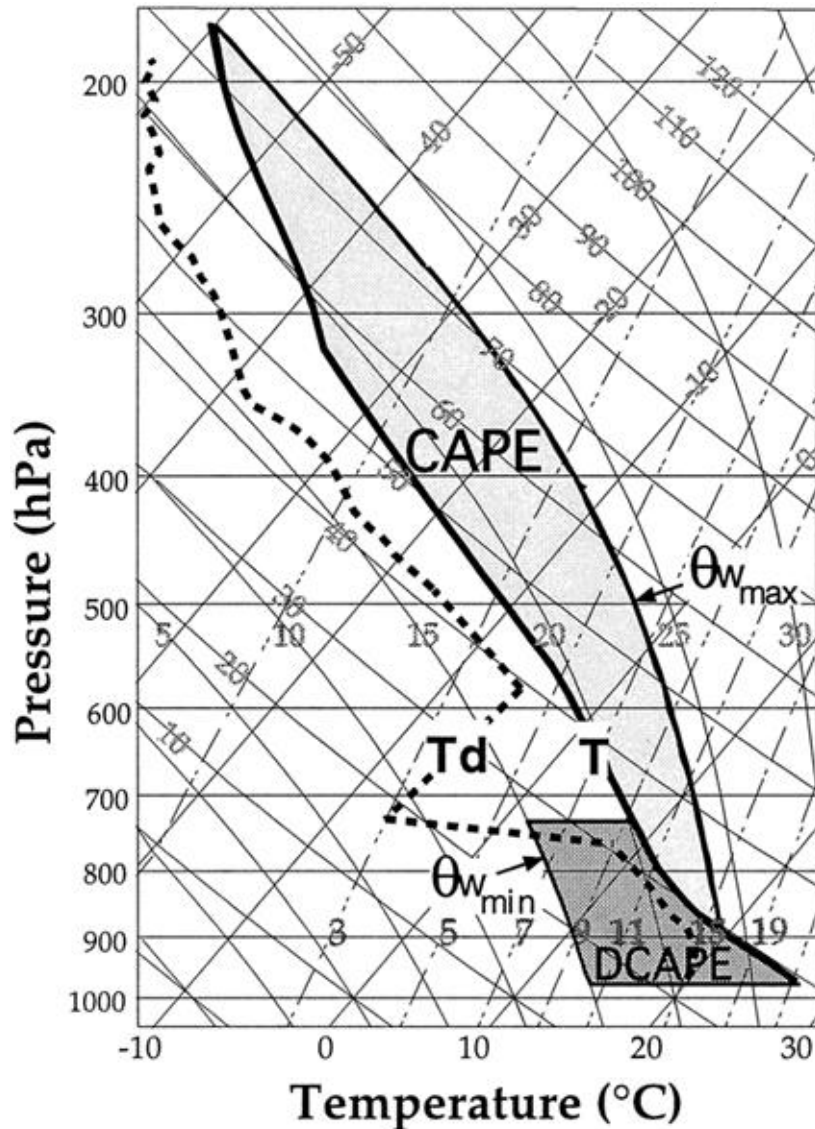


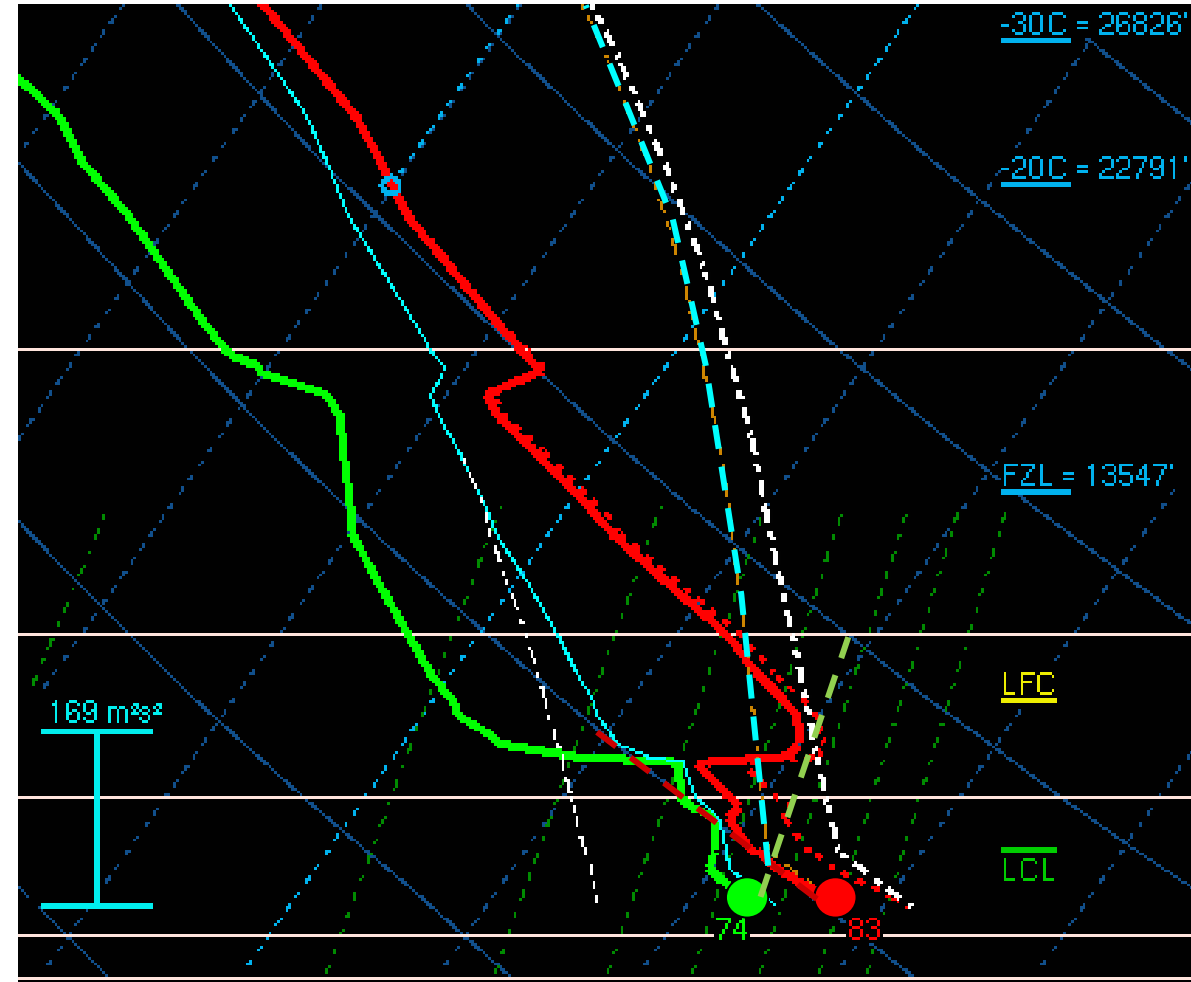
Fig. 1 Gilmore and Wicker 1998

- Estimates the negative buoyancy a downdraft parcel could have.
- This gives you an estimation of potential downdraft strength.
- Assumes you know where the downdraft is originating from! (Other parcel theory assumptions apply.)
- Because of this, it often doesn't show up as a strong discriminator for severe wind.

Parcel Selection - Which is Best?

Surface-Based (SB) Parcel

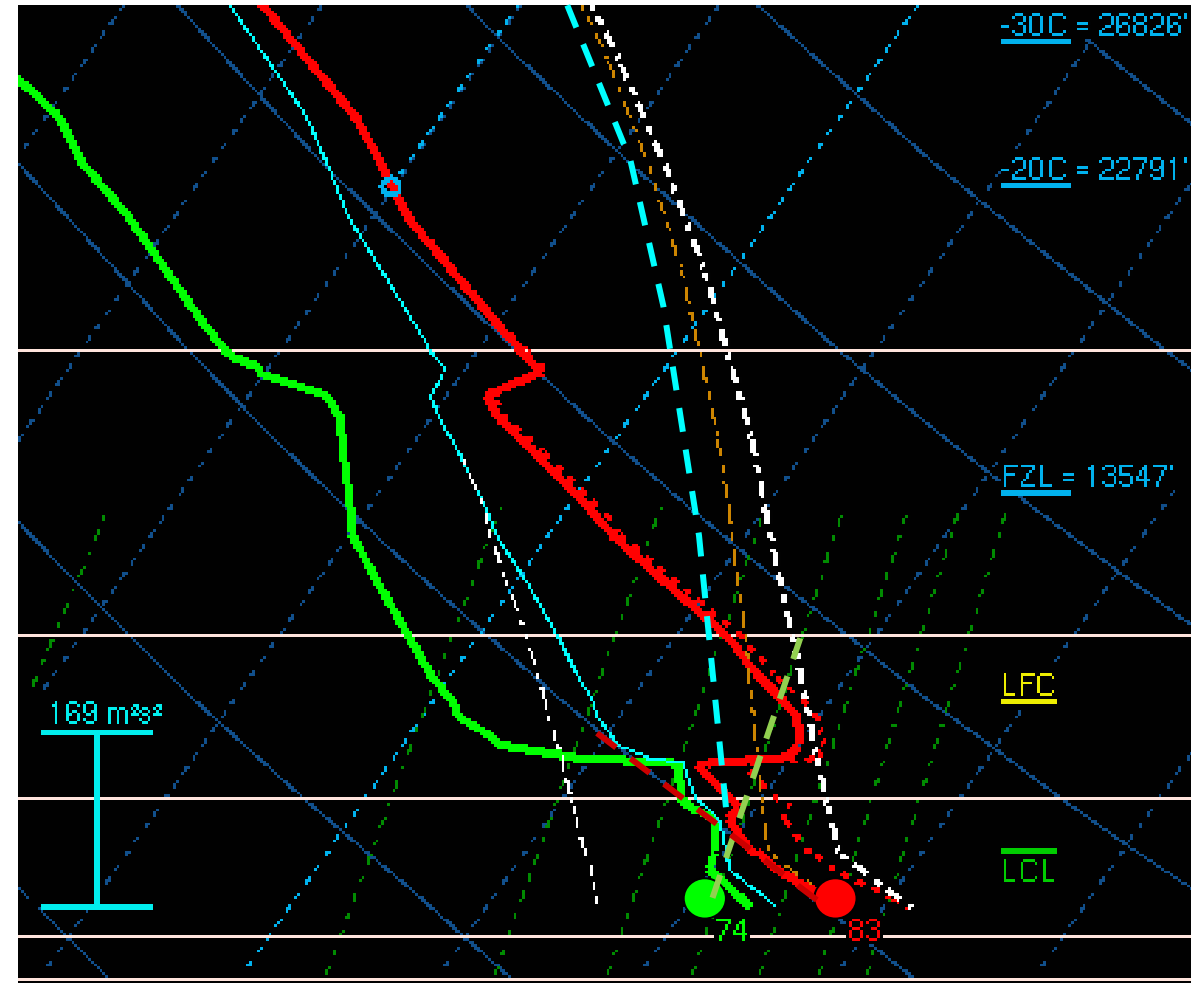
- Lift a parcel from the surface pressure using the surface temperature and dewpoint.
- Easy to calculate!
- Often unrepresentative: too unstable with too little inhibition. Does not account for elevated convection (more later).



Parcel Selection - Which is Best?

Mixed-Layer (ML) Parcel

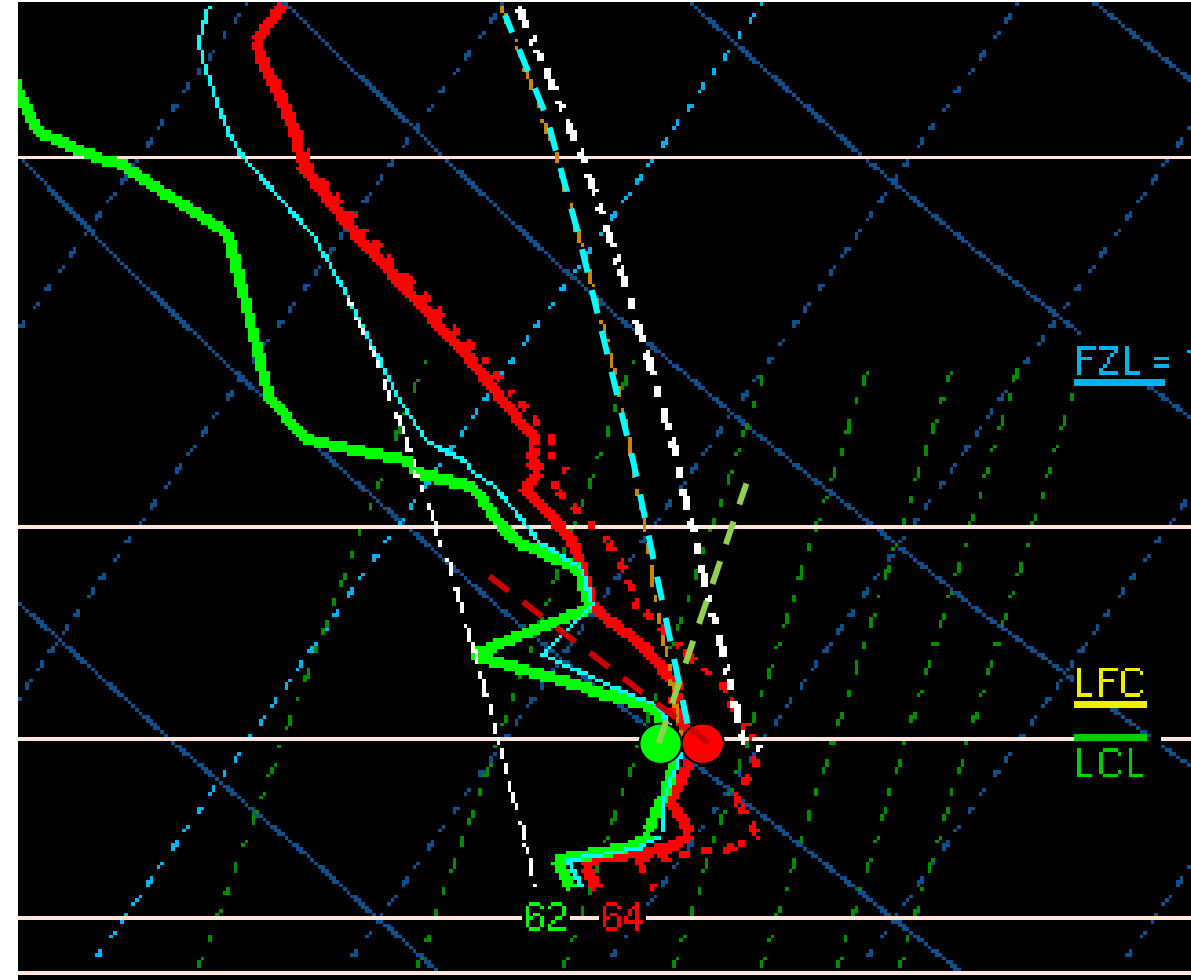
- Find the average temperature, & dewpoint from the lowest 100 mb. Lift this parcel from the surface.
- Found to be a good representation of parcel buoyancy on most typical severe weather days.
- Often features less CAPE and more CIN compared to other parcels.



Parcel Selection - Which is Best?

Most-Unstable (MU) Parcel

- Find the highest Theta-e value in the lowest 400 mb (typically). Use this level's temperature, dewpoint, and pressure level to lift a parcel.*
- Essential for identifying elevated T-storm environments.
- Often overestimates CAPE and underestimates CIN in non-elevated T-storm environments.
- The SB Parcel is often the MU Parcel when if there is a convective boundary layer in place.

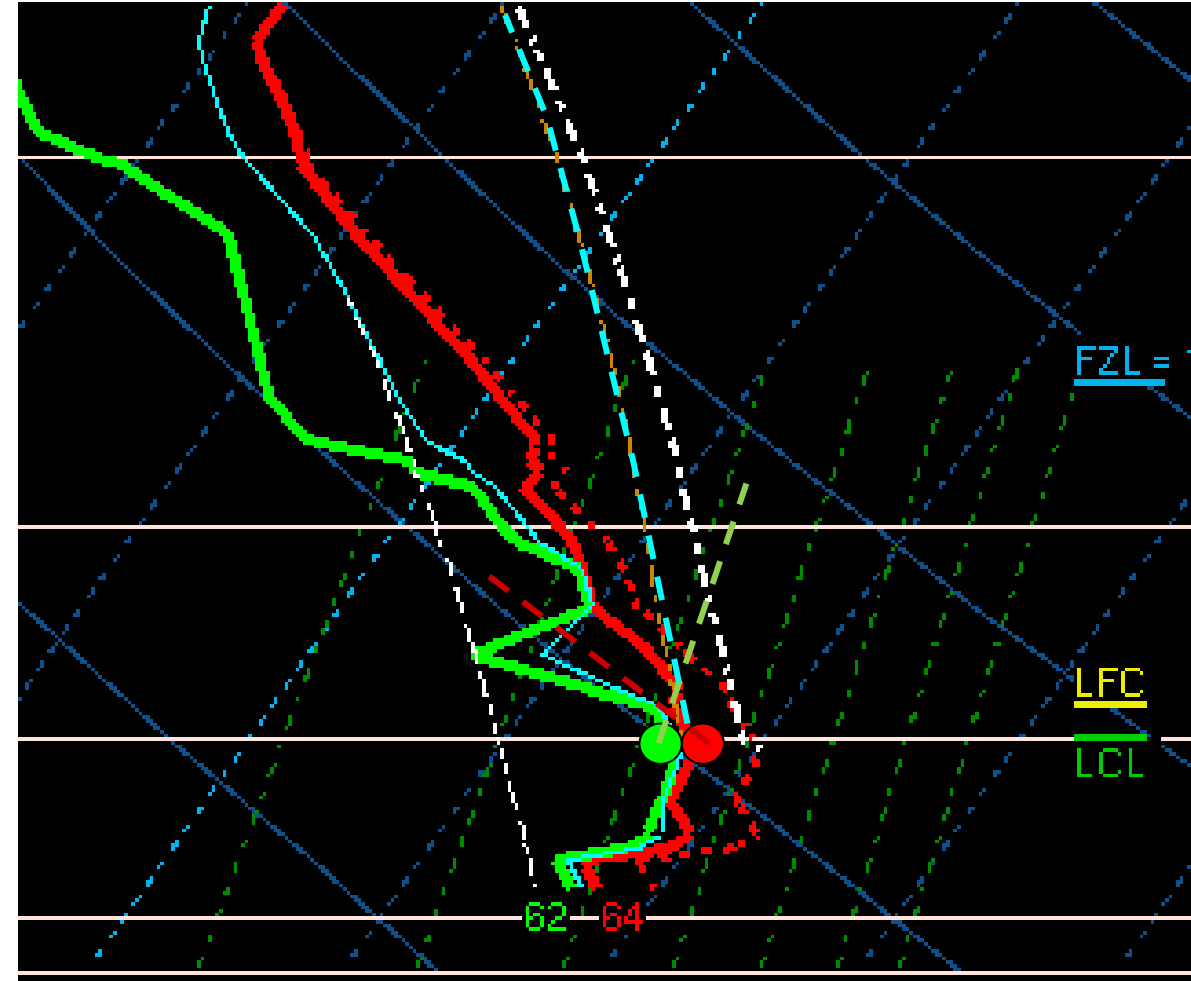


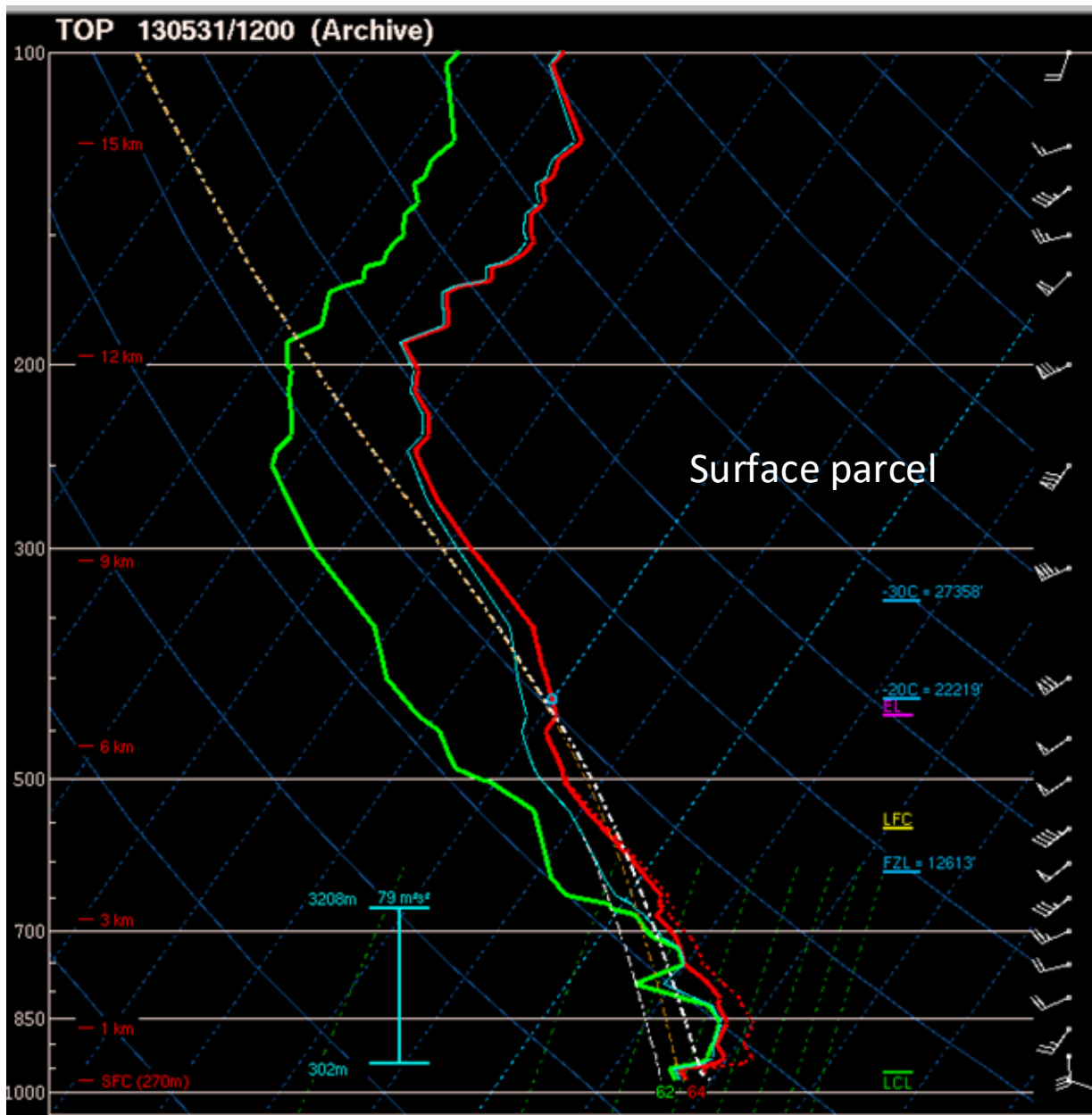
*This is not the only method!

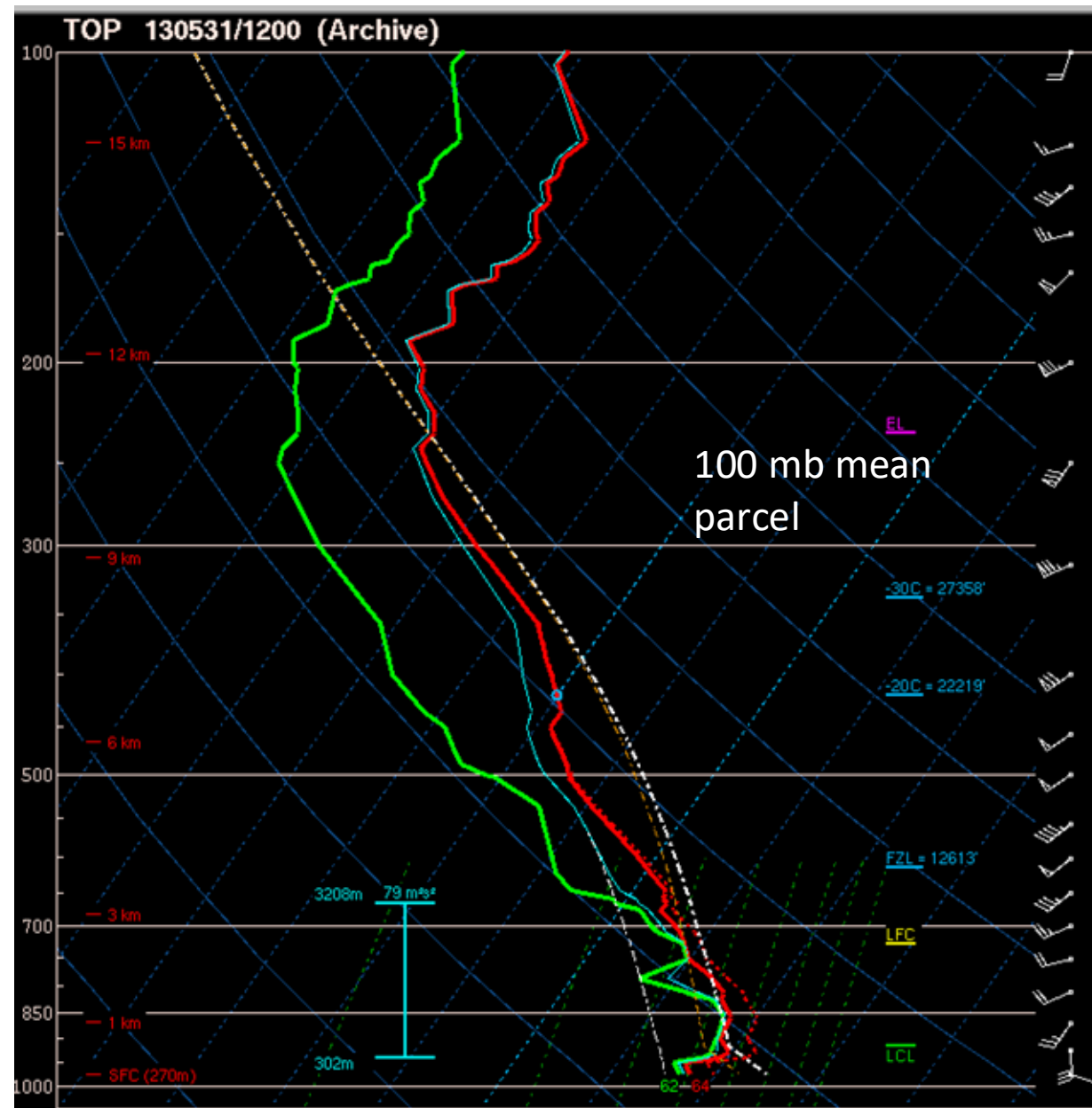
Parcel Selection - Which is Best?

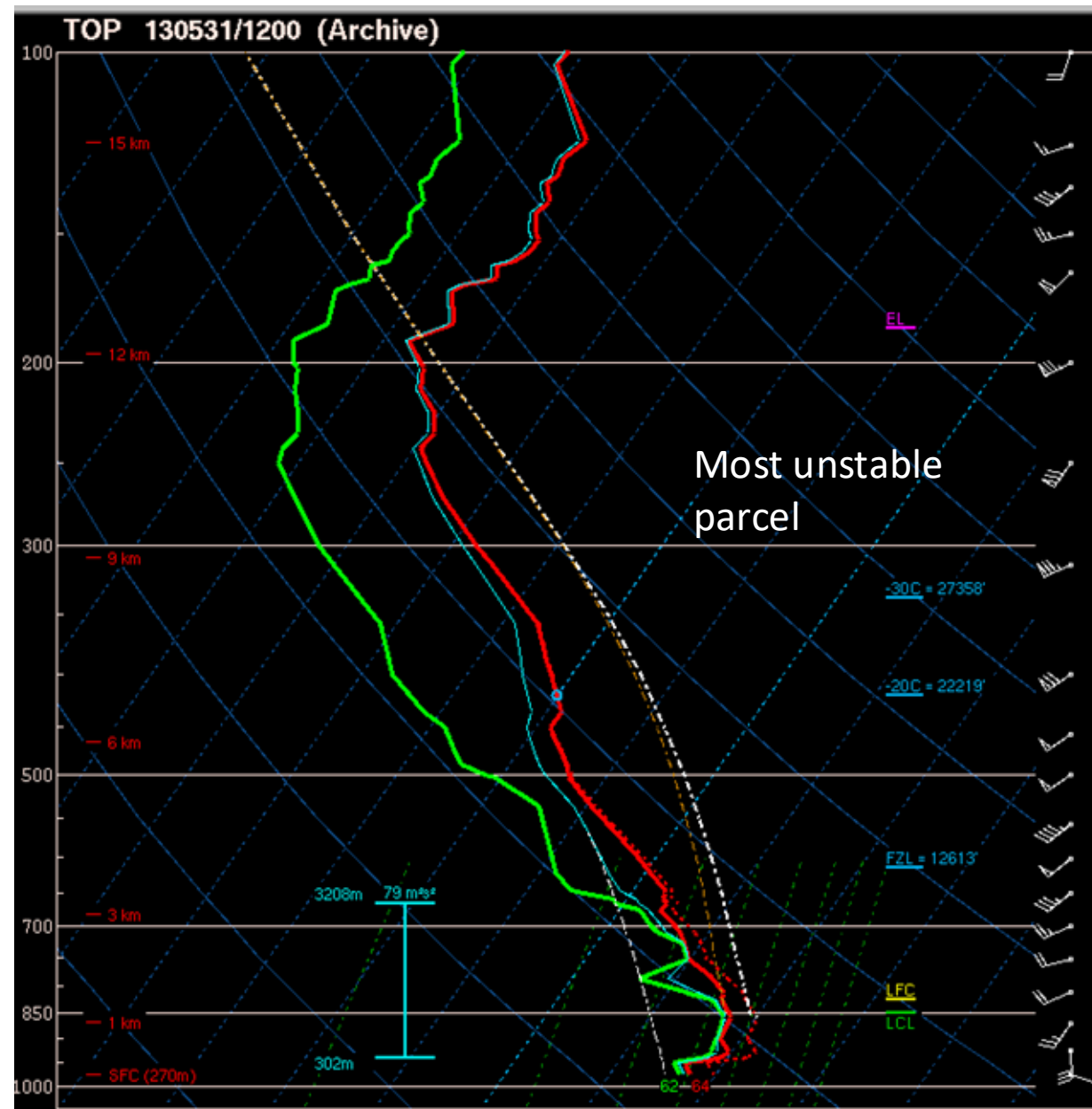
Least Inhibited (LI) Parcel

- Lift a series of parcels, find the parcel with the lowest amount of inhibition.
- This is often, but not always, the MU Parcel.
- Not particularly useful for severe convection, but can be helpful for identifying or explaining areas of weak thunderstorms.









What do we assume in parcel theory?

- No mixing with environment (not true)
 - “entrainment” usually reduces updraft strength from expectations based on CAPE alone
- Hydrometeor falls out instantly (not true)
 - Suspended rain particles reduces updraft strength. That’s why we say “pseudo” adiabatic for saturated parcel ascent
- Neglects downward pressure perturbation pressure
 - Acts to hinder the upward motion of parcels.
- Parcel vertical motion is due to buoyancy alone
 - We don’t explicitly incorporate environmental ascent (e.g. mesoscale, synoptic ascent, etc...)

Vertical PGF

- Wider thermal has larger PGF compared to narrow thermal (more air needs to be moved out of the way)
- As thermal becomes wider the scenario approaches hydrostatic where PGF offsets buoyancy ($dw/dt=0$)
- In theory, narrow thermals more favorable for convective initiation

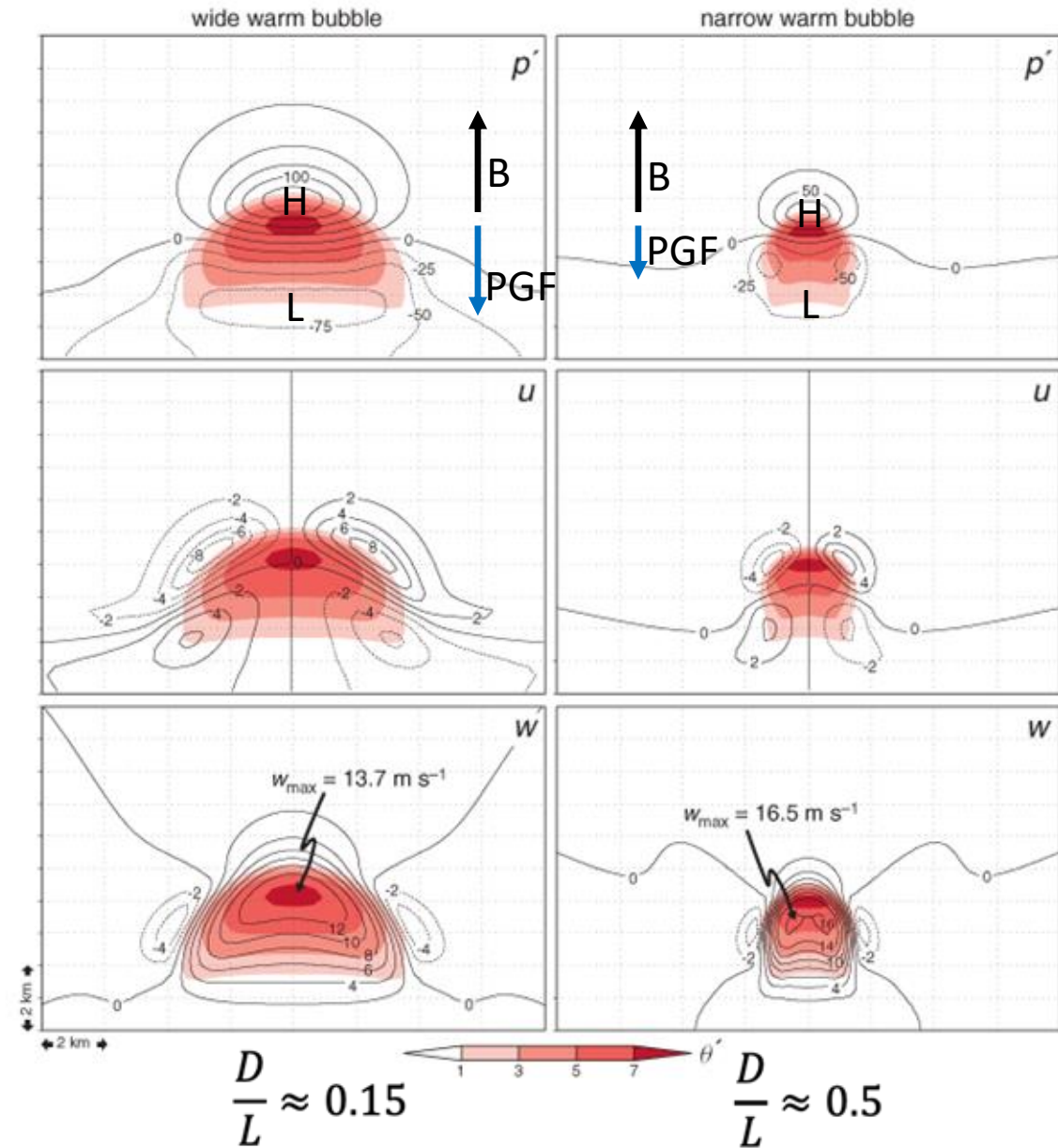
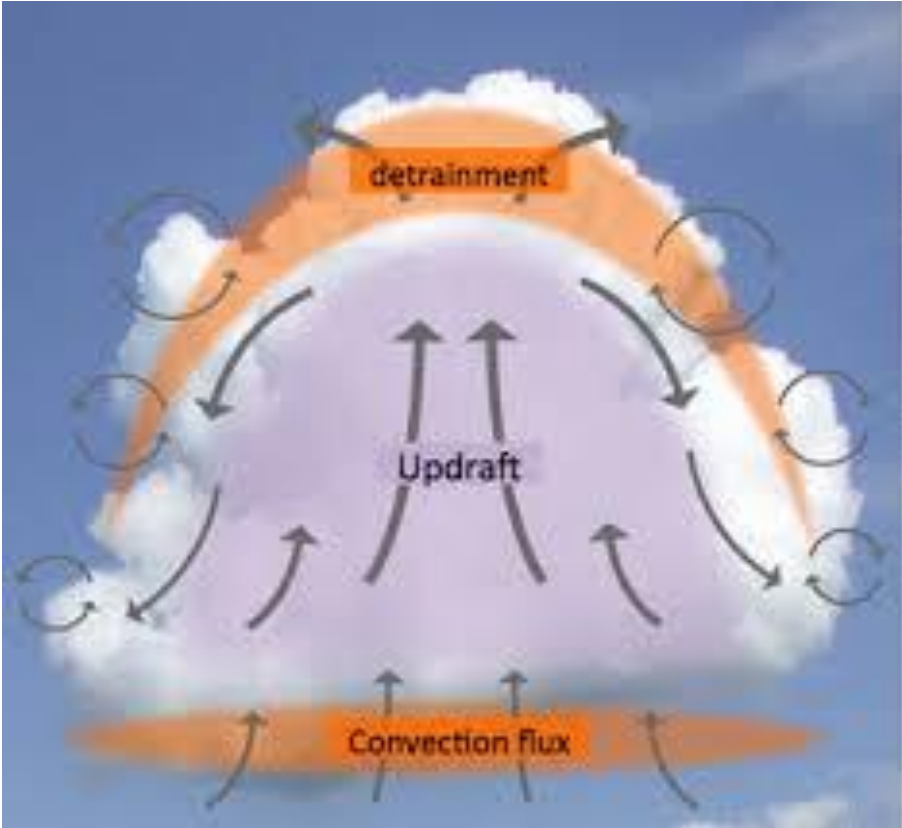


Figure 3.1

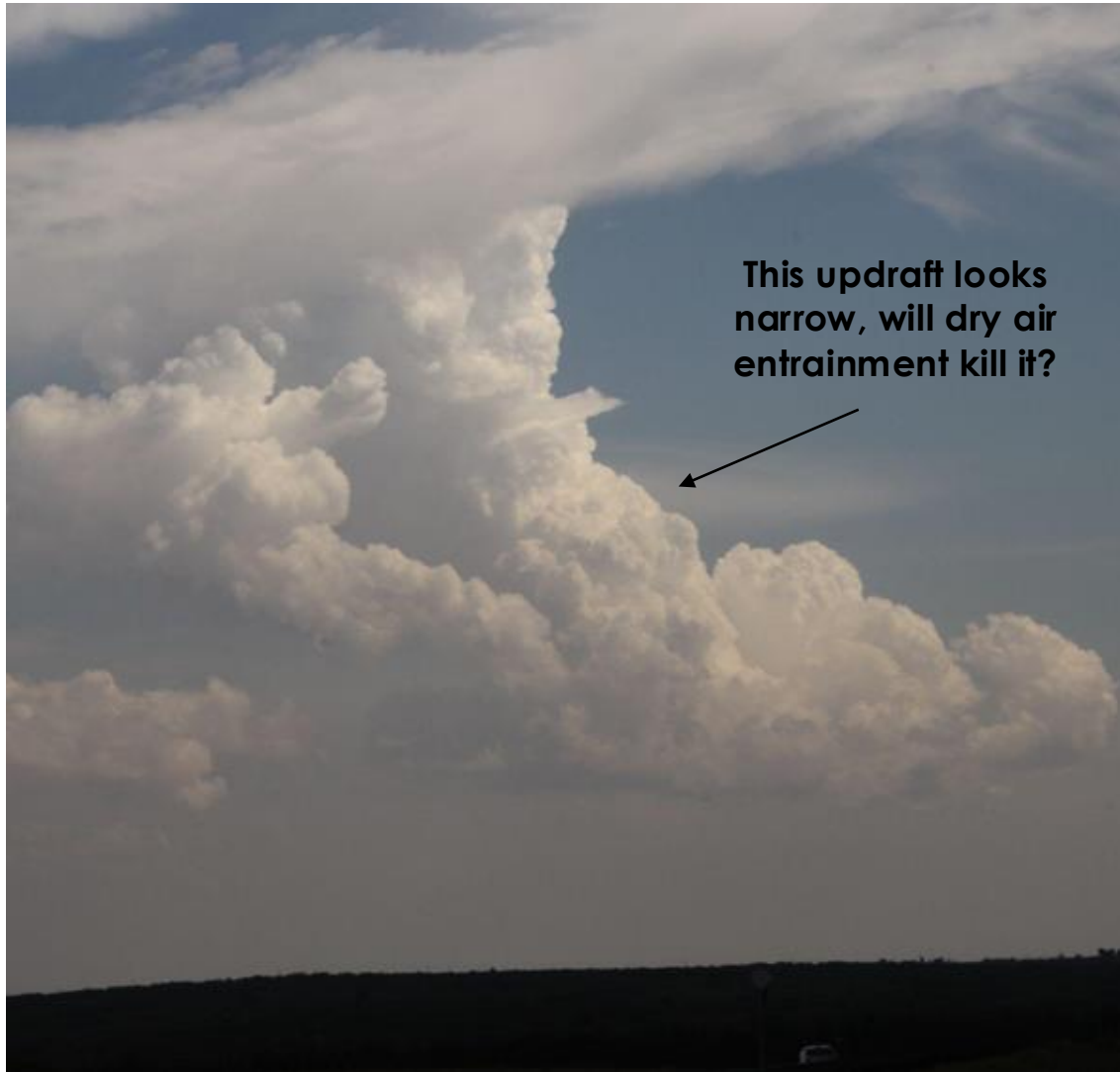
Dry Air Entrainment & E-CAPE

Mixing by two mechanisms:



- 1) The condensed updraft is very moist (RH near 100%), the environment is relatively dry. Moisture flux from updraft to the environment to restore thermodynamic equilibrium.
- 1) Differential vertical motion across the updraft (dw/dx and dw/dy) causes mechanical mixing on the cloud exterior.

Dry Air Entrainment & E-CAPE



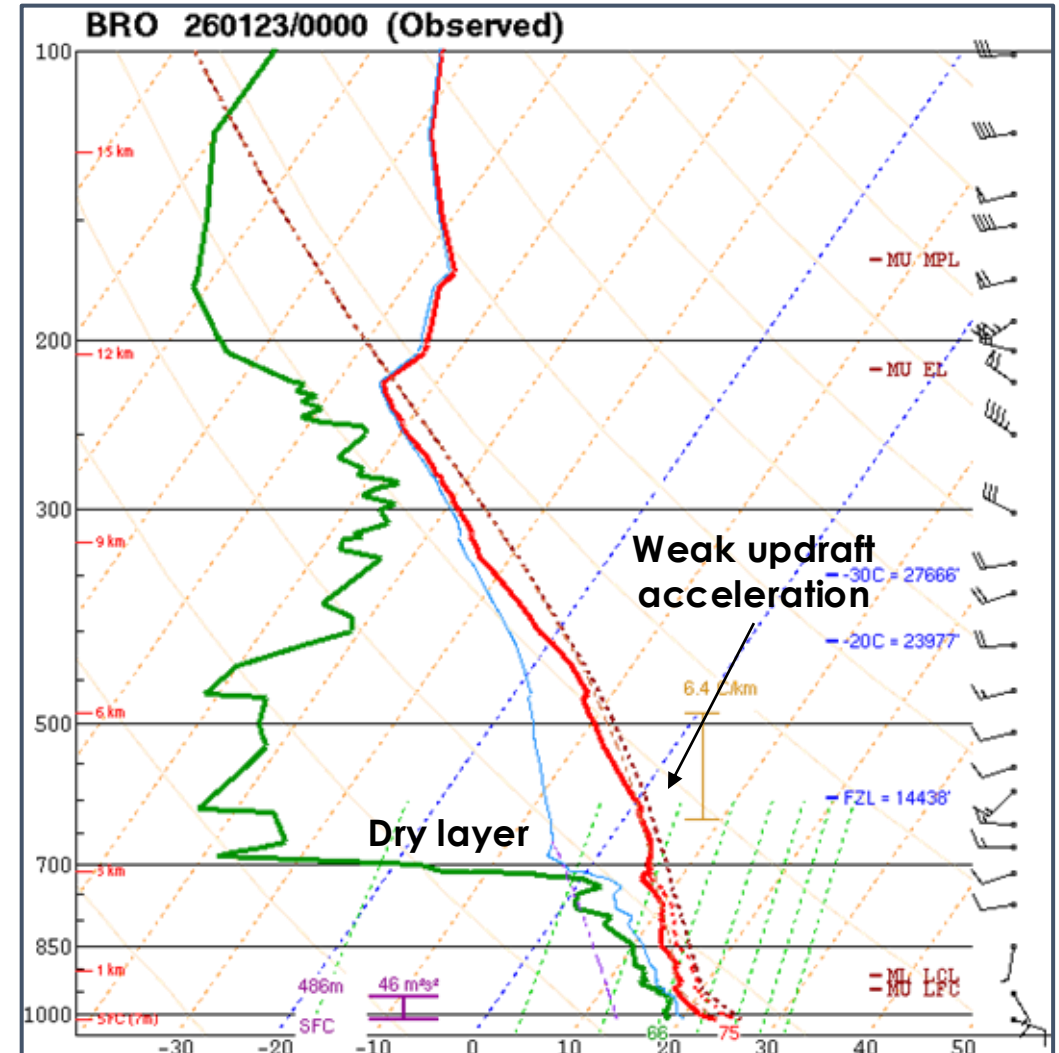
Dry Air Entrainment & E-CAPE

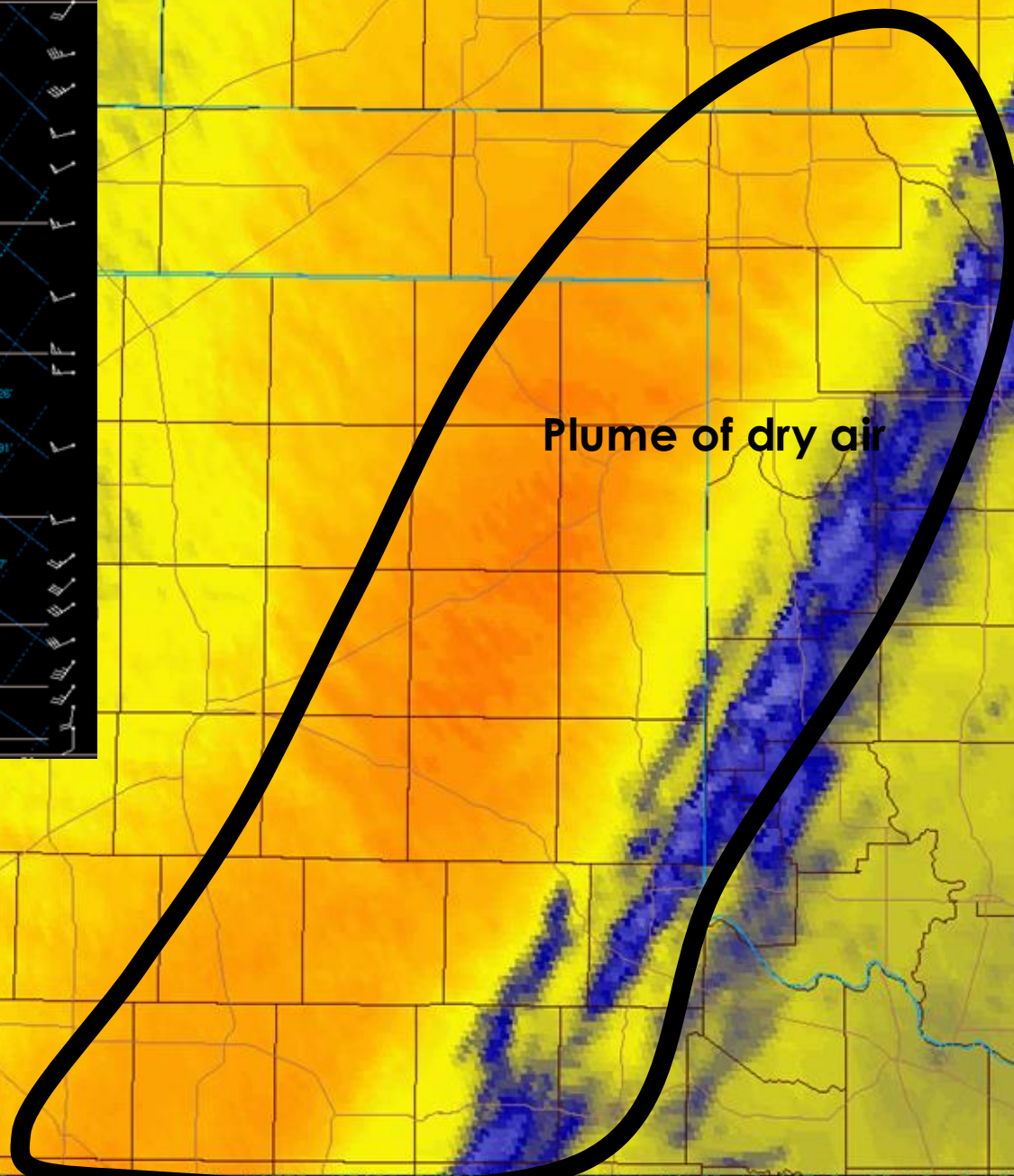
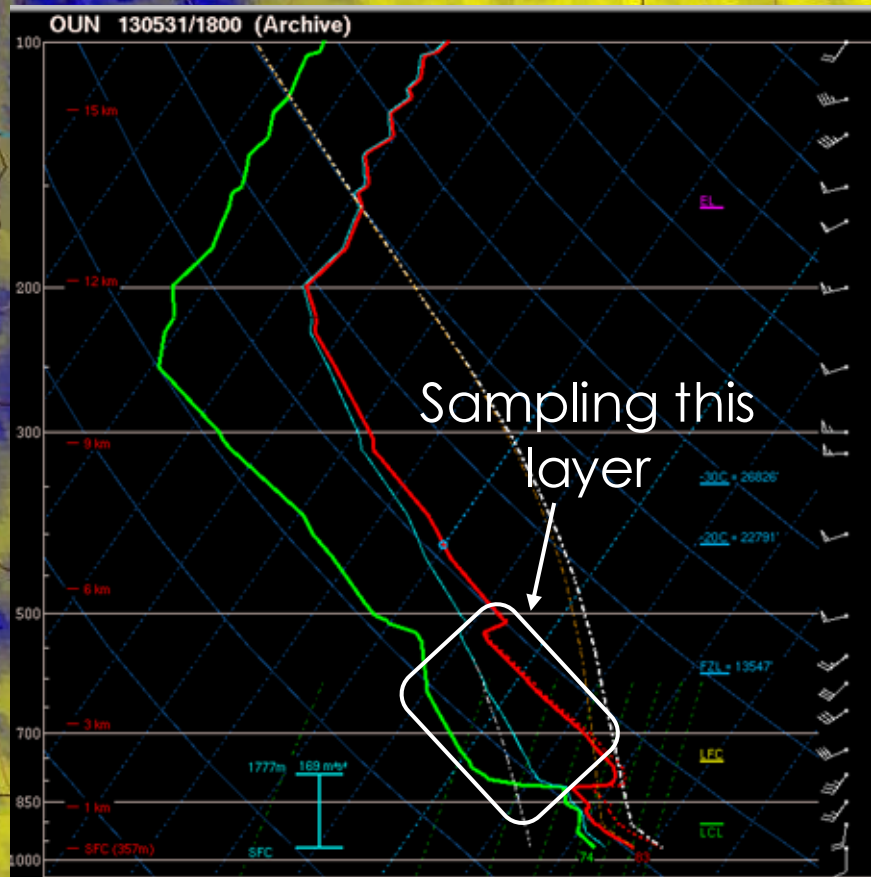
Dry air entrainment occurs all of the time!

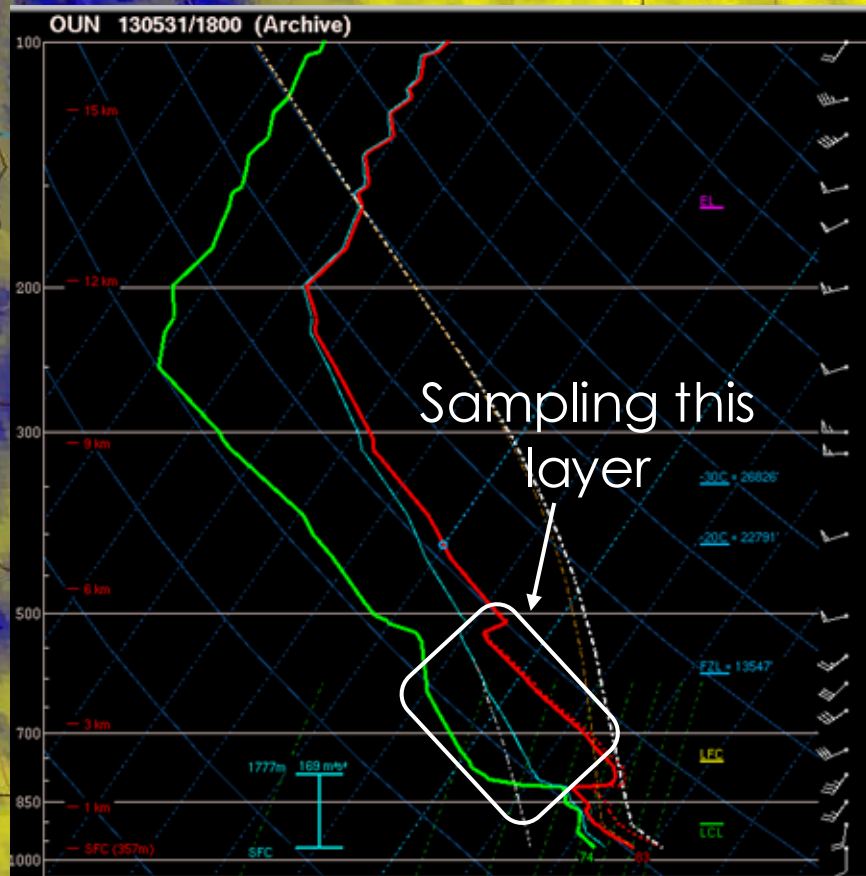
How do we know when it could be a problem?

Thermodynamically: look for dry layers coincident with very narrow buoyancy profile (i.e. weak CAPE).

Mechanical lift: In weak-lift regimes, T-storms are dependent on their own thermodynamic buoyancy with no help from environmental ascent.







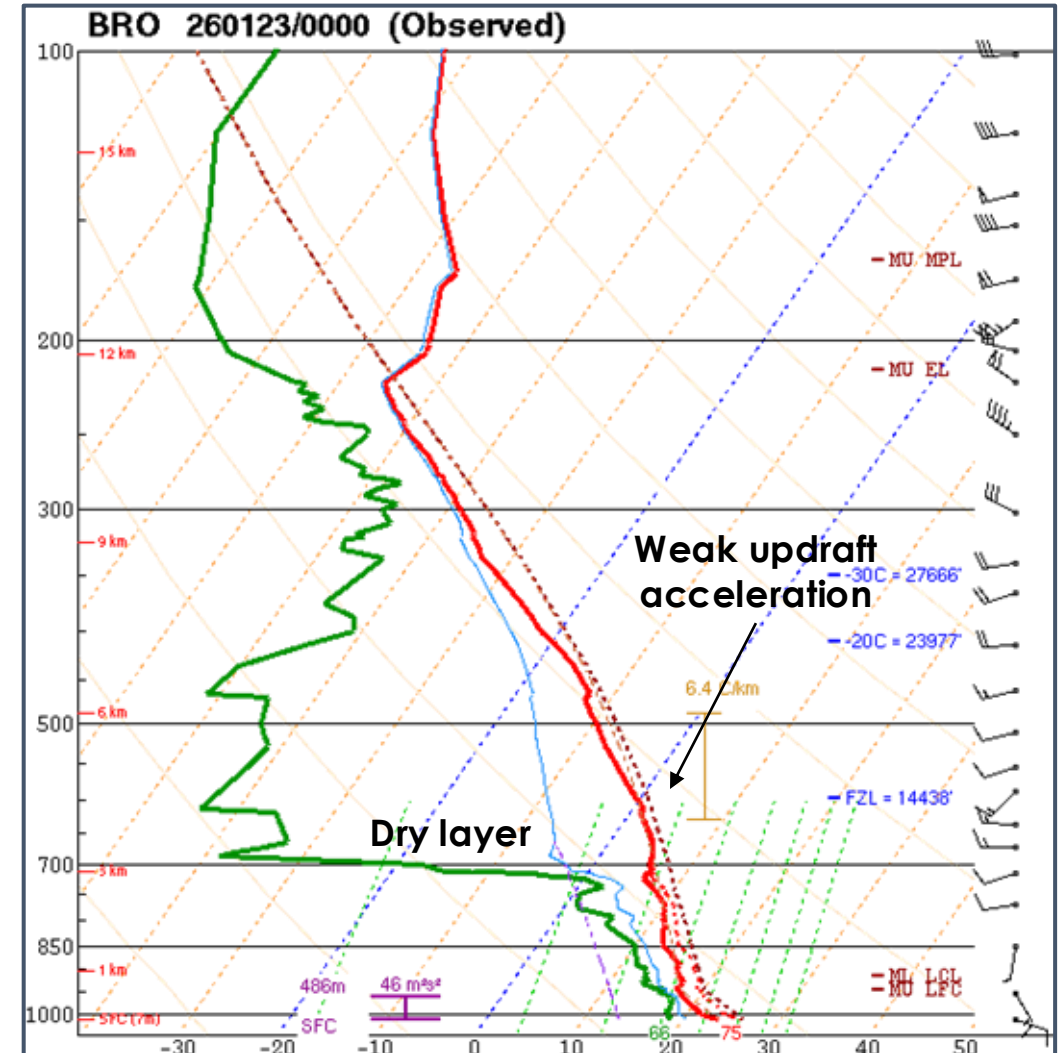
Failed Convective Initiation

So how can we account for this?

$$\text{ECAPE} = \frac{-1 - \frac{2\psi}{v_{\text{SR}}^2} \text{NCAPE} + \sqrt{\left(1 + \frac{2\psi}{v_{\text{SR}}^2} \text{NCAPE}\right)^2 + \frac{8\psi}{v_{\text{SR}}^2} \text{CAPE}}}{4 \frac{\psi}{v_{\text{SR}}^2}}.$$

- Accounts for dry air entrainment!
- Reduces CAPE in dry environments
- Increase CAPE in moist environments.

- Computationally expensive (changing)
- Not as intuitive to determine from sounding.



Dry Air Entrainment & E-CAPE

Ultimately, why and when does this matter?

$$w_{max} = \sqrt{2 * CAPE}$$

$$CAPE = \int_{z_f}^{z_n} g \left(\frac{T_{v,parcel} - T_{v,env}}{T_{v,env}} \right) dz$$

$$ECAPE = \frac{-1 - \frac{2\psi}{V_{SR}^2} NCAPE + \sqrt{\left(1 + \frac{2\psi}{V_{SR}^2} NCAPE\right)^2 + \frac{8\psi}{V_{SR}^2} CAPE}}{4 \frac{\psi}{V_{SR}^2}}.$$

Which CAPE you use an influence how you interpret updraft intensity.

But be weary, they're all still just estimates!

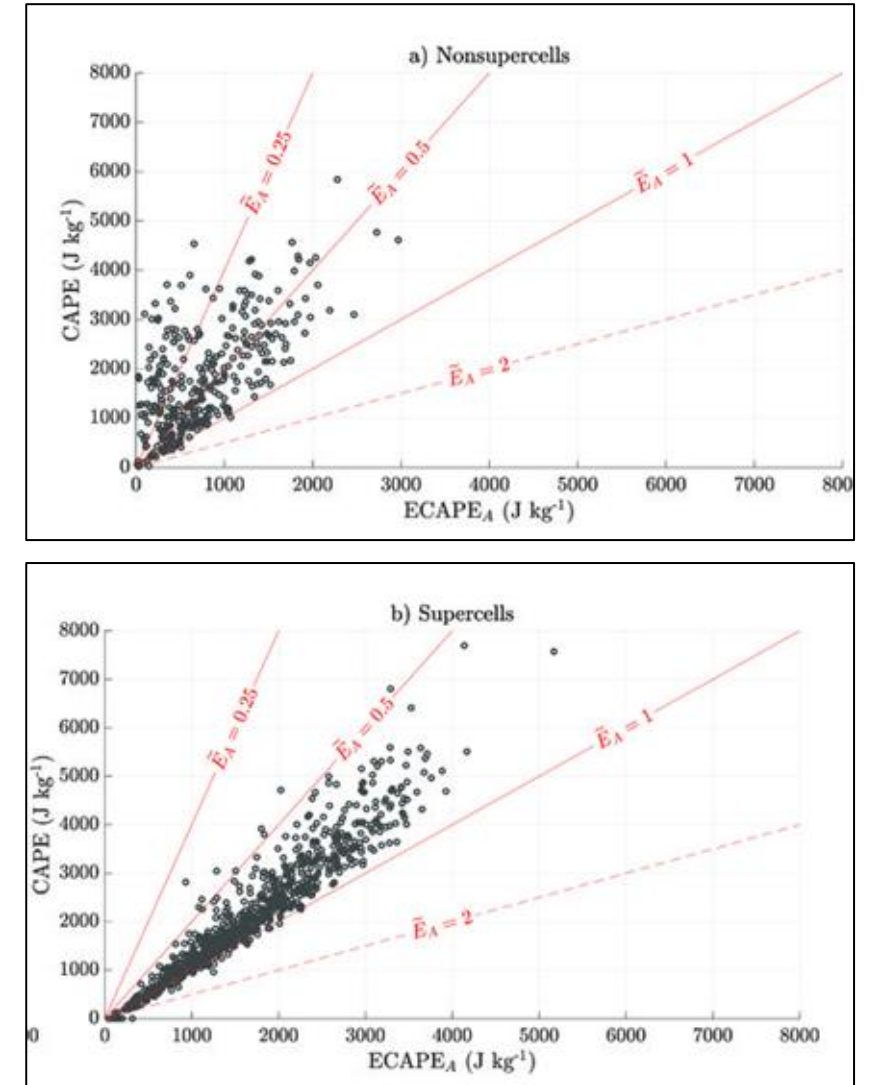
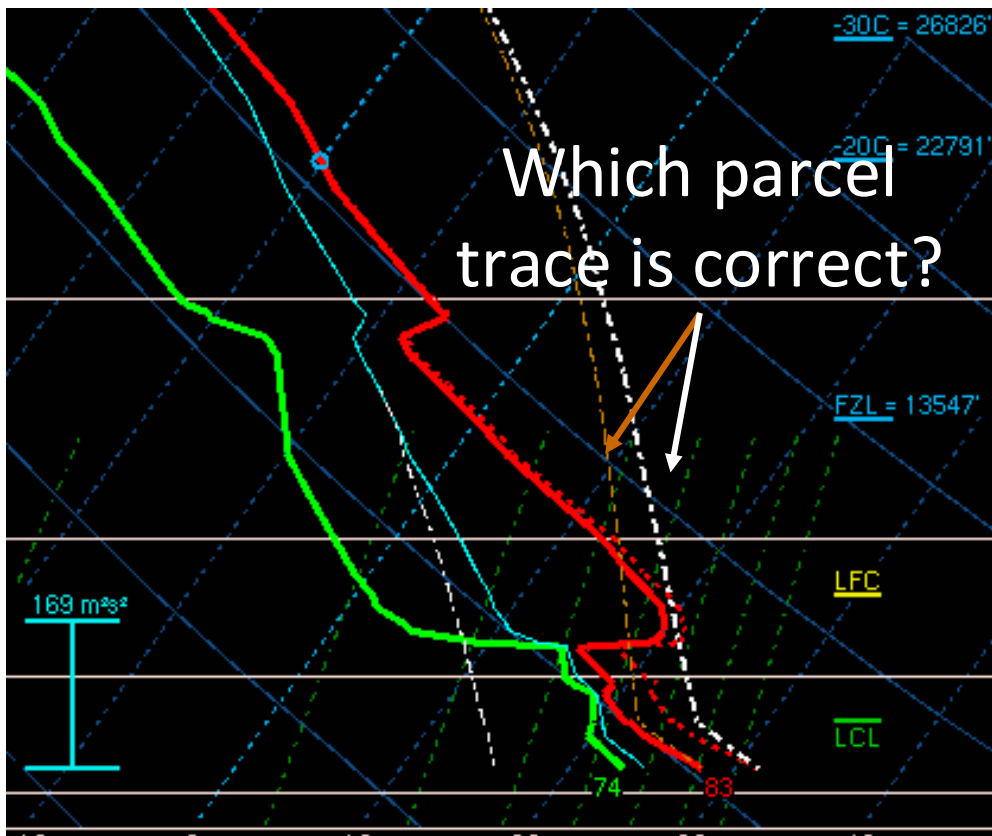
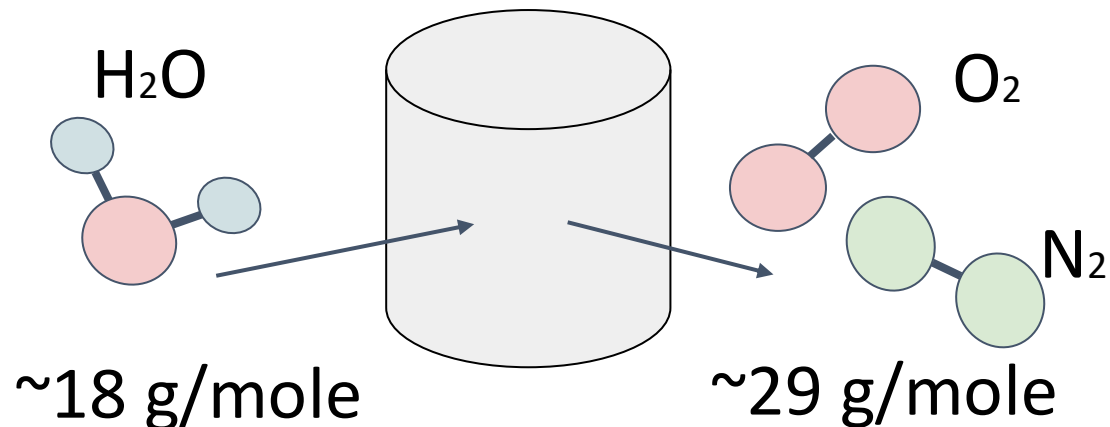


Fig 10 from Peters et al 2023



Conservation of mass in a parcel



Virtual Temperature Correction

Accounts for the reduction in density a parcel experiences as the proportion of water vapor in the parcel increases.

$$T_v = \frac{T + 273.15}{1 - 0.379 \times \left(\frac{6.11 \times 10^{\left(\frac{7.5 \times T_d}{237.3 + T_d} \right)}}{P_{sta}} \right)}$$

$$\text{CAPE} = \int_{z_f}^{z_n} g \left(\frac{T_{v,\text{parcel}} - T_{v,\text{env}}}{T_{v,\text{env}}} \right) dz$$

In effect, this makes our parcel trace more representative of reality by:

- Increasing CAPE
- Reducing CIN



Matters most in moist,
low-CAPE environments

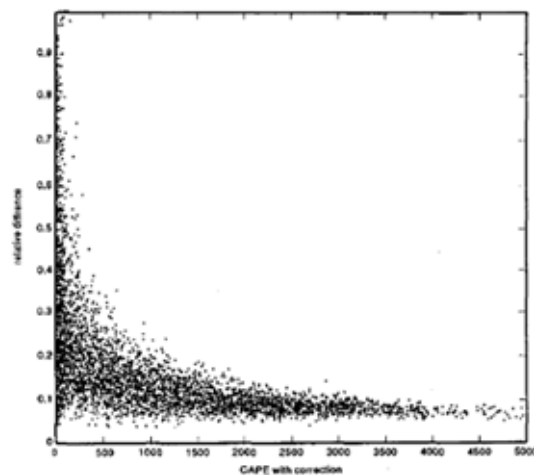
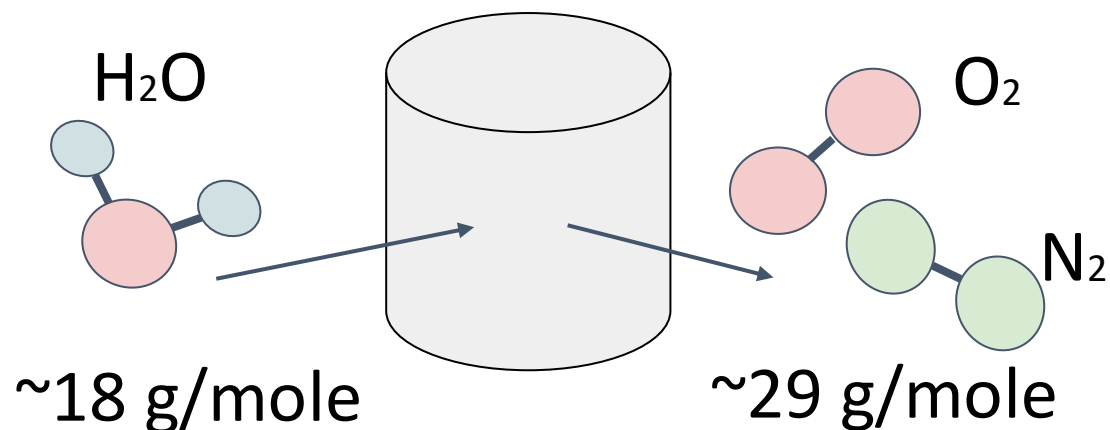


FIG. 4. Plot of the relative difference in the CAPE with and without the virtual correction for the 1992 positive CAPE soundings (as in Fig. 2) versus CAPE (with correction).

Conservation of mass in a parcel



NOTES AND CORRESPONDENCE

The Effect of Neglecting the Virtual Temperature Correction on CAPE Calculations

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NOAA/Environmental Research Laboratories, National Severe Storms Laboratory, Norman, Oklahoma

3 March 1994 and 22 June 1994

ABSTRACT

A simple theoretical analysis of the impact of neglecting the virtual correction on calculation of CAPE is made. This theory suggests that while ignoring the virtual correction does not introduce much error for large CAPE values, the relative error can become substantial for small CAPE. A test of the theory is done by finding the error made by ignoring the virtual correction to CAPE for all the soundings in 1992 having positive CAPE (when the correction is made). Results of this empirical test confirm that the relative error made in ignoring the correction increases with decreasing CAPE. A number of other "corrections" to CAPE might be considered. In a discussion of the issues associated with the results of the analysis, it is recommended that CAPE calculations should include the virtual correction but that other complications should be avoided for most purposes, especially when making comparisons of CAPE values. A standardized CAPE calculation also is recommended.

1. Introduction

This note addresses the calculation of convective available potential energy (CAPE). CAPE is a quantity most closely associated with the environment in which deep convection might occur, and has become widely accepted as a *forecasting* parameter with the advent of computer programs that calculate CAPE from operational soundings or model forecasts. Recently, it has come to our attention that the algorithms for computing CAPE are not all the same. In particular, some schemes do not include the virtual temperature correction in the calculations.

It is well known that the *virtual* temperature T_v is the proper temperature to use in the equation of state $p = \rho R T_v$ in order that the gas constant R be truly constant. Otherwise, the addition of moisture changes the "constant," with the change depending on the amount of moisture. Use of the virtual correction to temperature T such that

$$T_v = T(1 + \epsilon q), \quad (1)$$

where $\epsilon = 0.608$ when the mixing ratio q is expressed in g g^{-1} , allows the use of the gas constant for *dry* air, $R = 2.87 \times 10^2 \text{ m}^2 \text{ s}^{-2} \text{ K}^{-1}$, in the equation of state. The virtual correction is always positive because adding

water vapor to a parcel makes it less dense, which can be considered equivalent to warming the parcel.

Since CAPE concerns the *difference* in density between a rising parcel and its environment, and since an accurate calculation of density requires the virtual temperature, it should be obvious that the virtual correction is necessary when estimating CAPE. To assess the impact of ignoring the virtual correction, an analysis of the contribution from this error follows in section 2. In section 3, the application of CAPE estimates is discussed and some recommendations are made.

2. Theoretical analysis of the error

We begin with logarithmic differencing of the equation of state,

$$\frac{\delta p}{\rho} = \frac{\delta p}{p} - \frac{\delta T_v}{T_v}, \quad (2)$$

where the difference operator $\delta(\)$ is between the parcel and its environment:

$$\delta(\) = (\)_{\text{parcel}} - (\)_{\text{env.}}$$

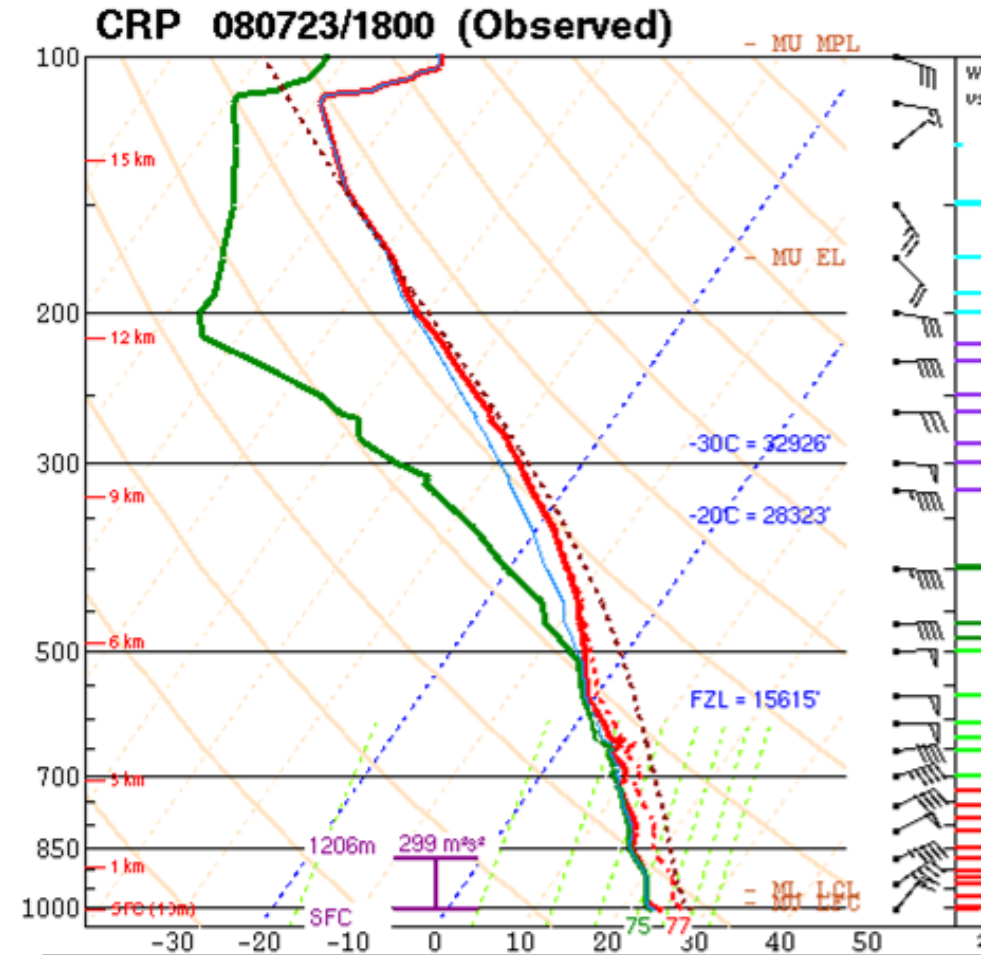
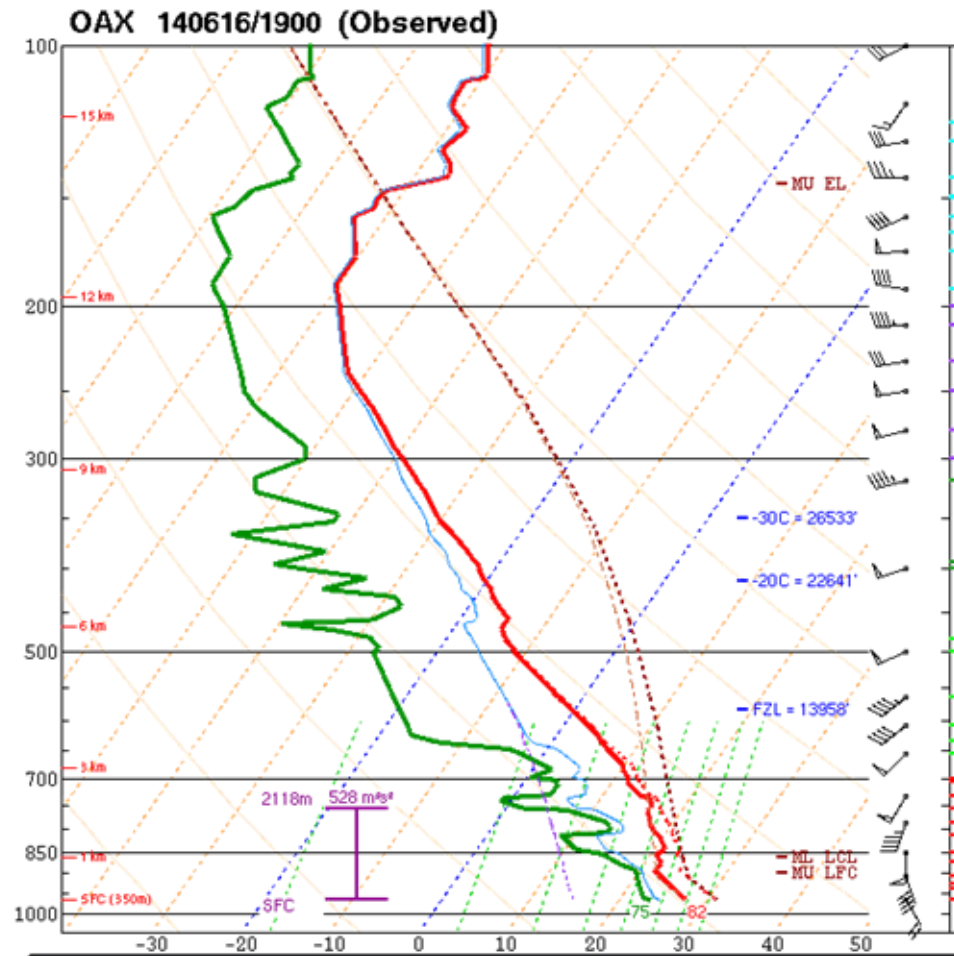
The standard assumption in parcel theory is to ignore the contribution to differences in density due to differences in *pressure* between the parcel and the environment. If this standard assumption is made and (1) is logarithmically differenced, substitution into (2) gives

$$\begin{aligned} \frac{\delta p}{\rho} &\approx -\frac{\delta T_v}{T_v}, \\ &= -\left[\frac{\delta T}{T} + \frac{\epsilon \delta q}{(1 + \epsilon q)} \right]. \end{aligned} \quad (3)$$

* Additional affiliation: Cooperative Institute for Mesoscale Meteorological Studies, Norman, Oklahoma.

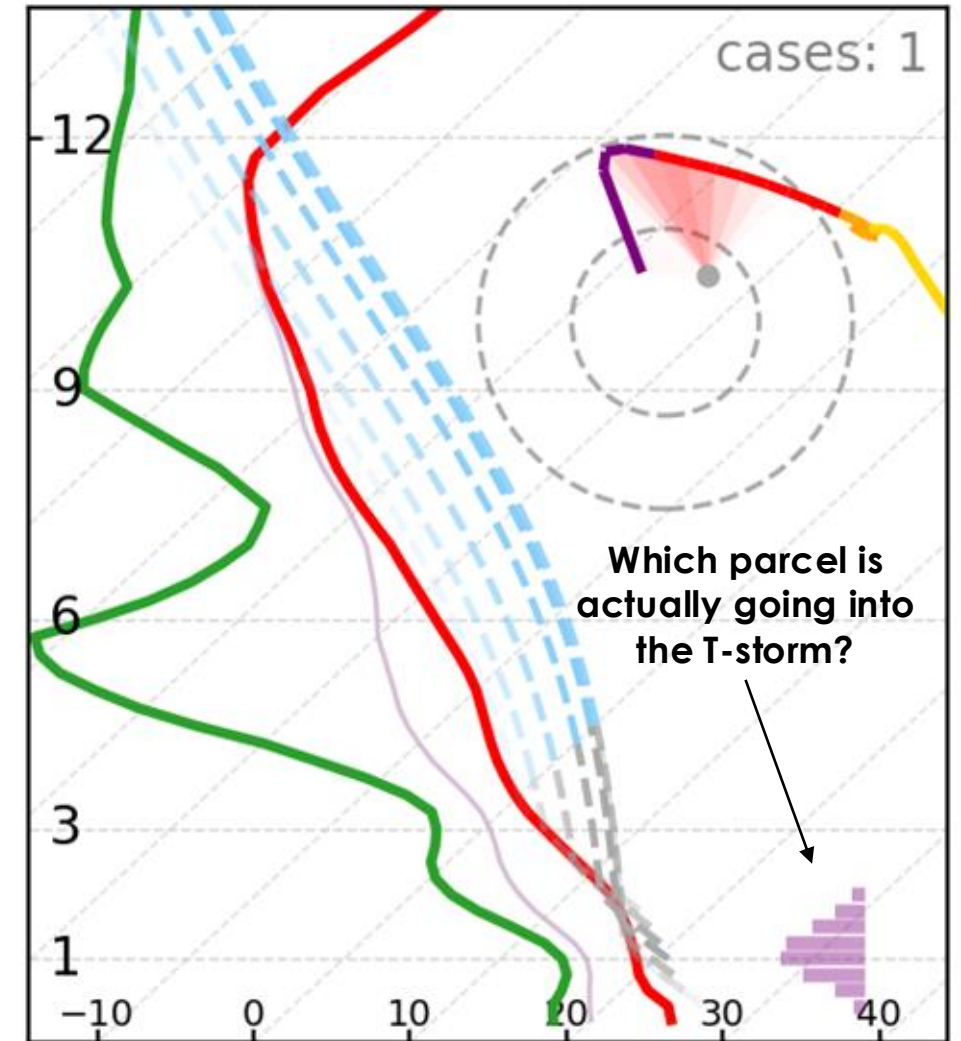
Corresponding author address: Dr. Charles A. Doswell III, National Severe Storms Laboratory, 1313 Halley Circle, Norman, OK 73069.

In which sounding will the virtual temperature correction matter more?



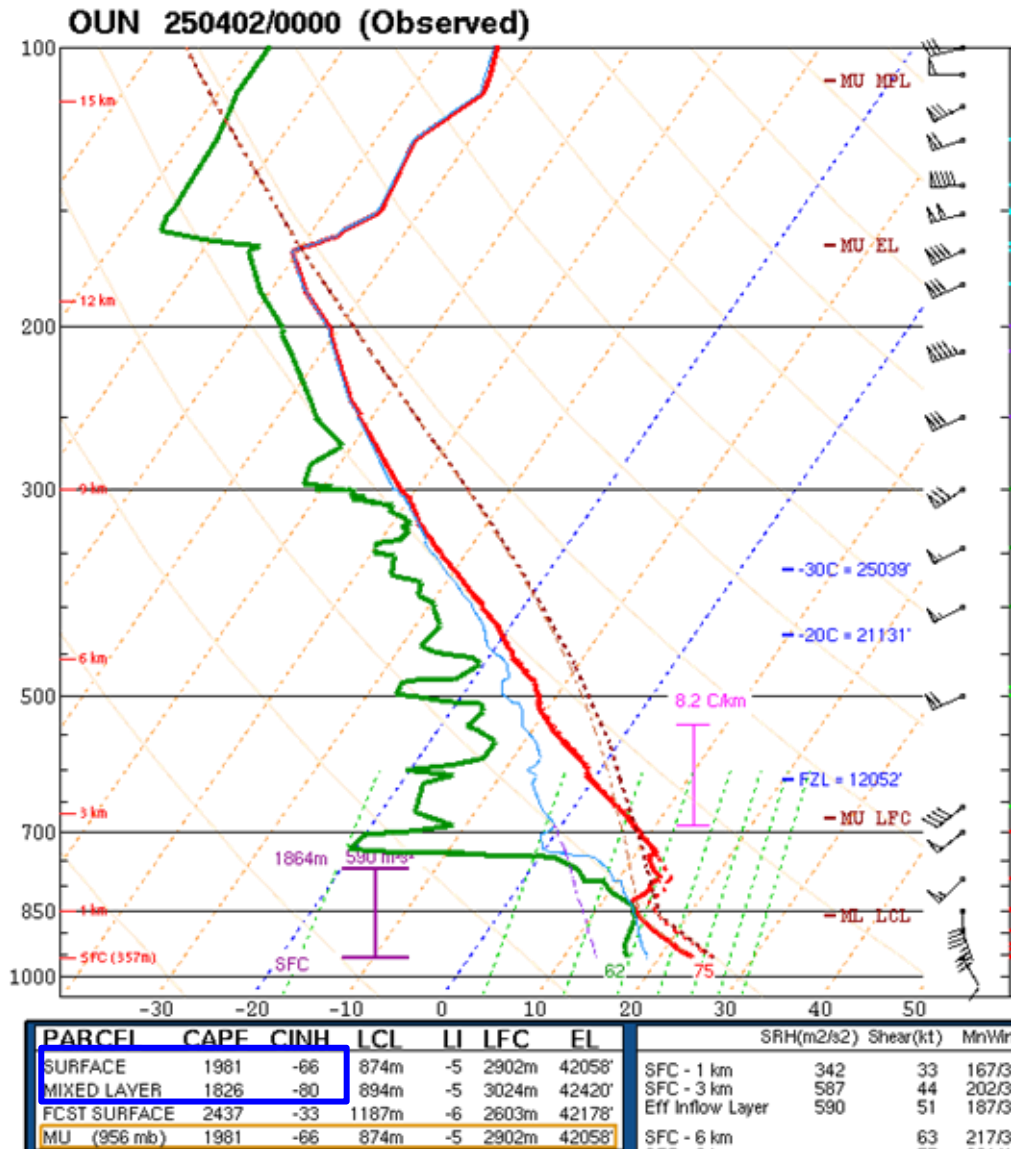
At the end of the day...

- Parcel selection matters!
 - Influences your interpretation of the environment.
- Know when to use the right parcel and when to make adjustments.
- Realize that we're working with an imperfect model of the atmosphere. Treat thermodynamic parameters as estimates!



Courtesy of Dr. Cameron Nixon

What is feeding the storm?



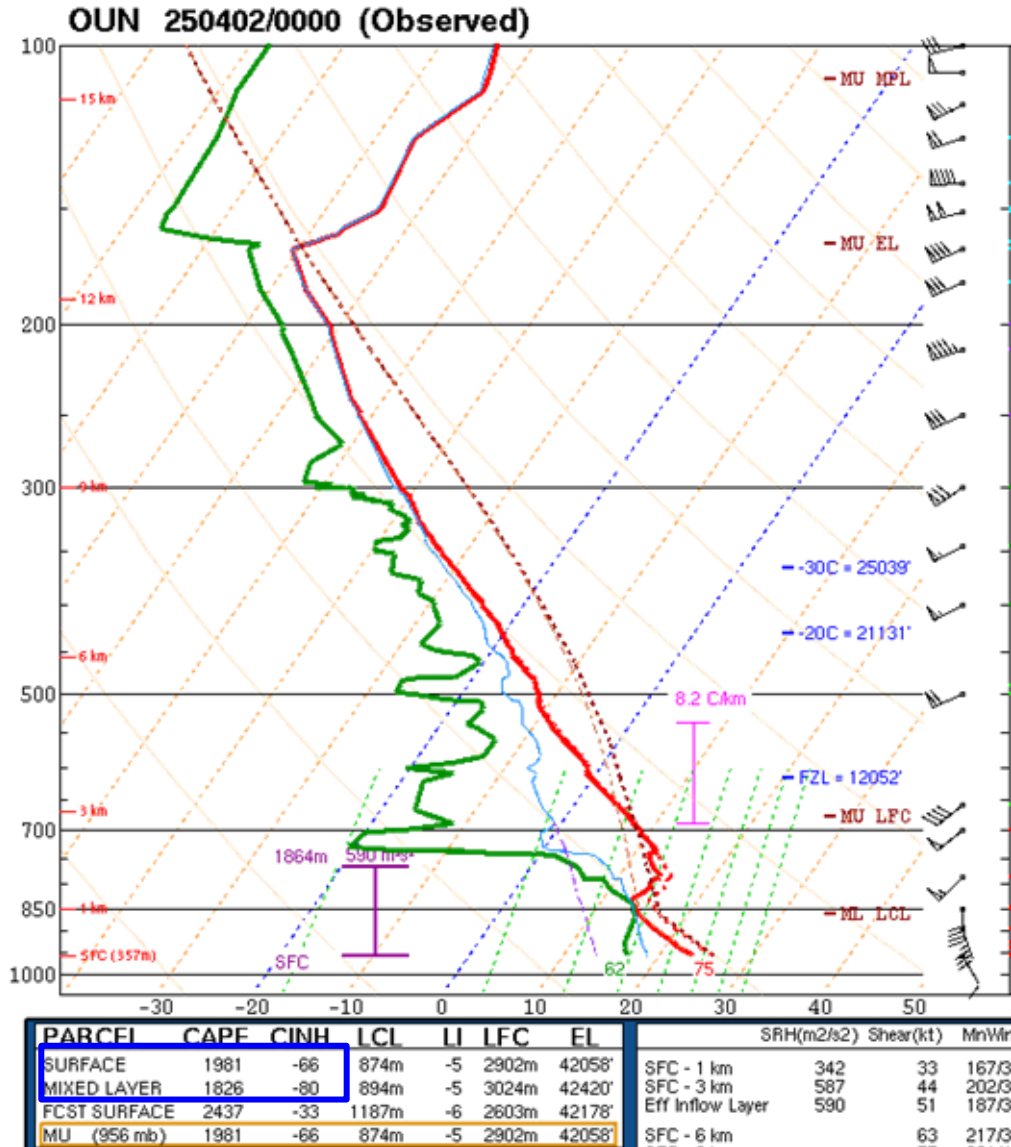
Is this storm surface-based?

Storm motion suggested it was not.

(more on that later)

No discernable rising scud.

What is feeding the storm?



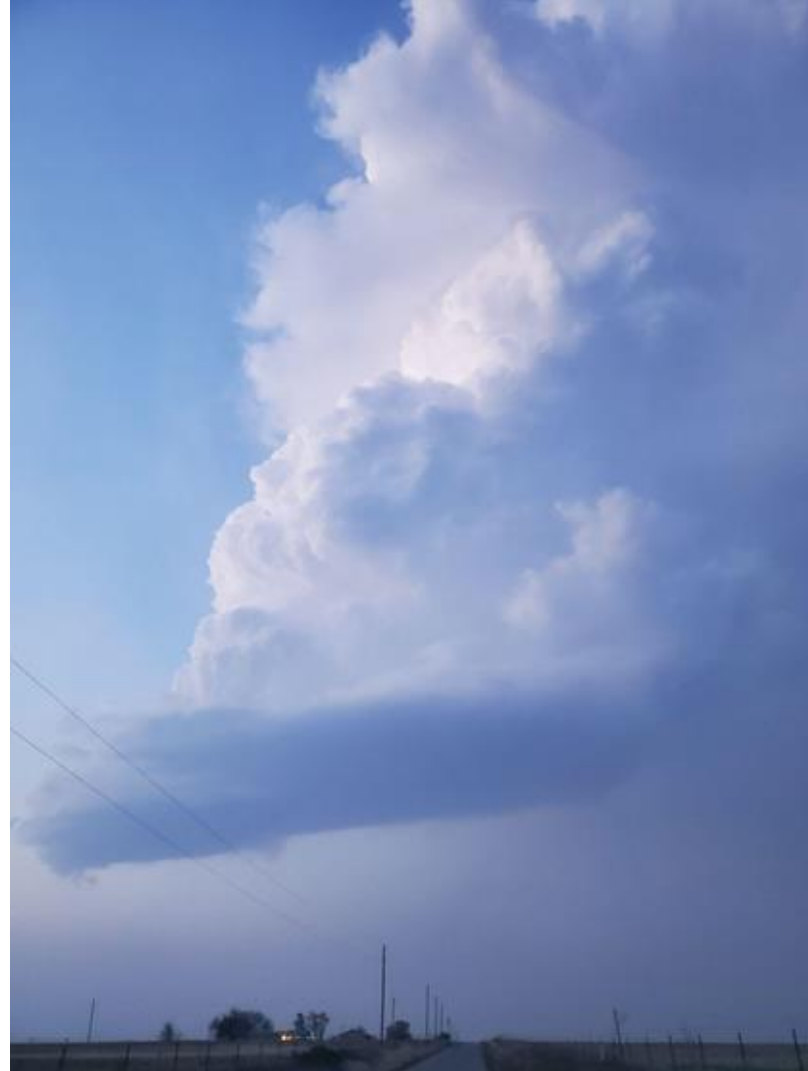
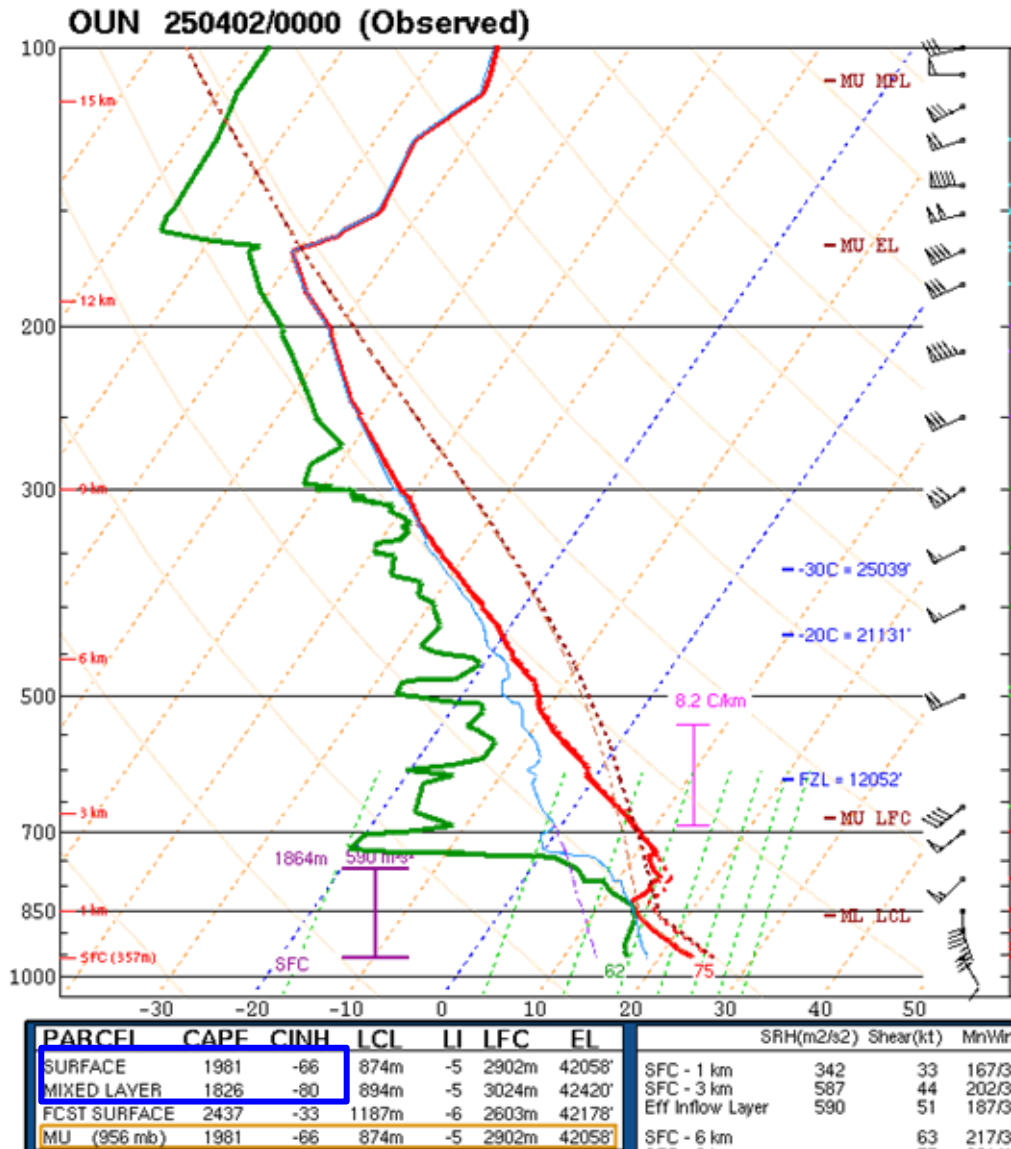
Is this storm surface-based?

Increasing rising scud into a lowering cloud base.

Notable updraft pulses.

Suggested the storm was ingesting near-surface parcels!

What is feeding the storm?



Is this storm surface-based?

Rising scud diminishes.

Weak updraft pulses.

Cloud based climbs up and elongates.

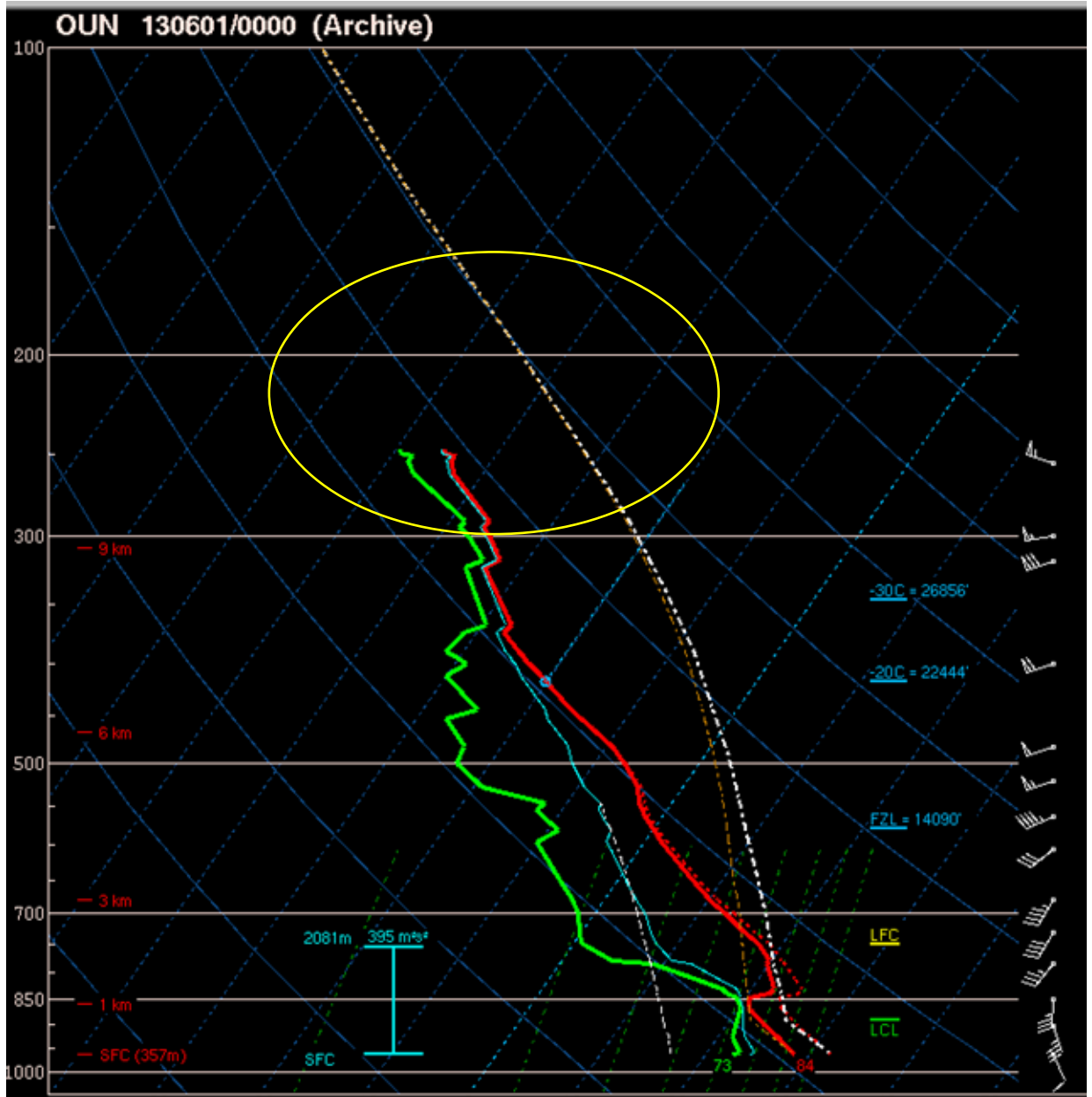
Storm begins accelerating away from us.

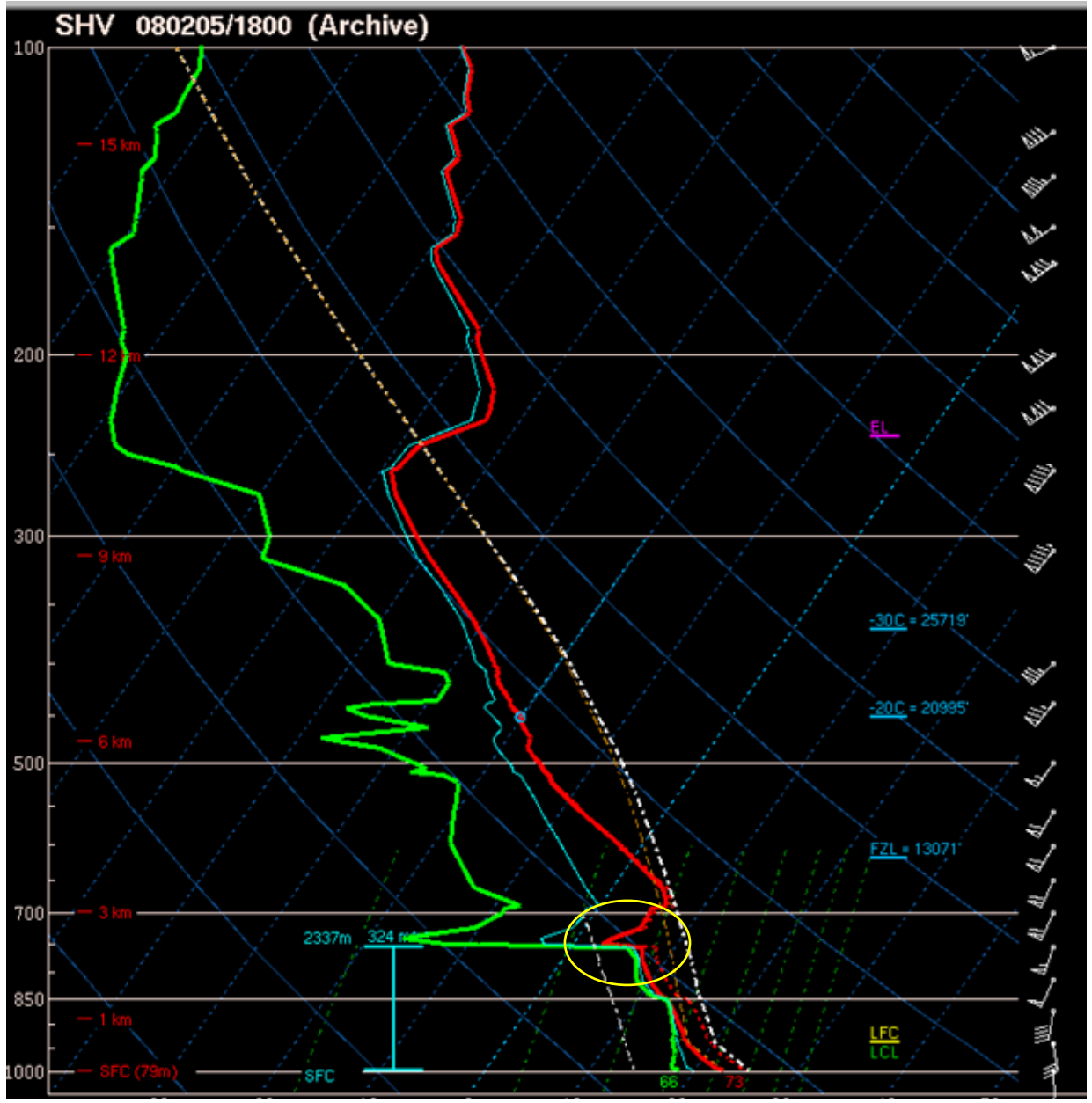
Storm dies within 20 minutes.

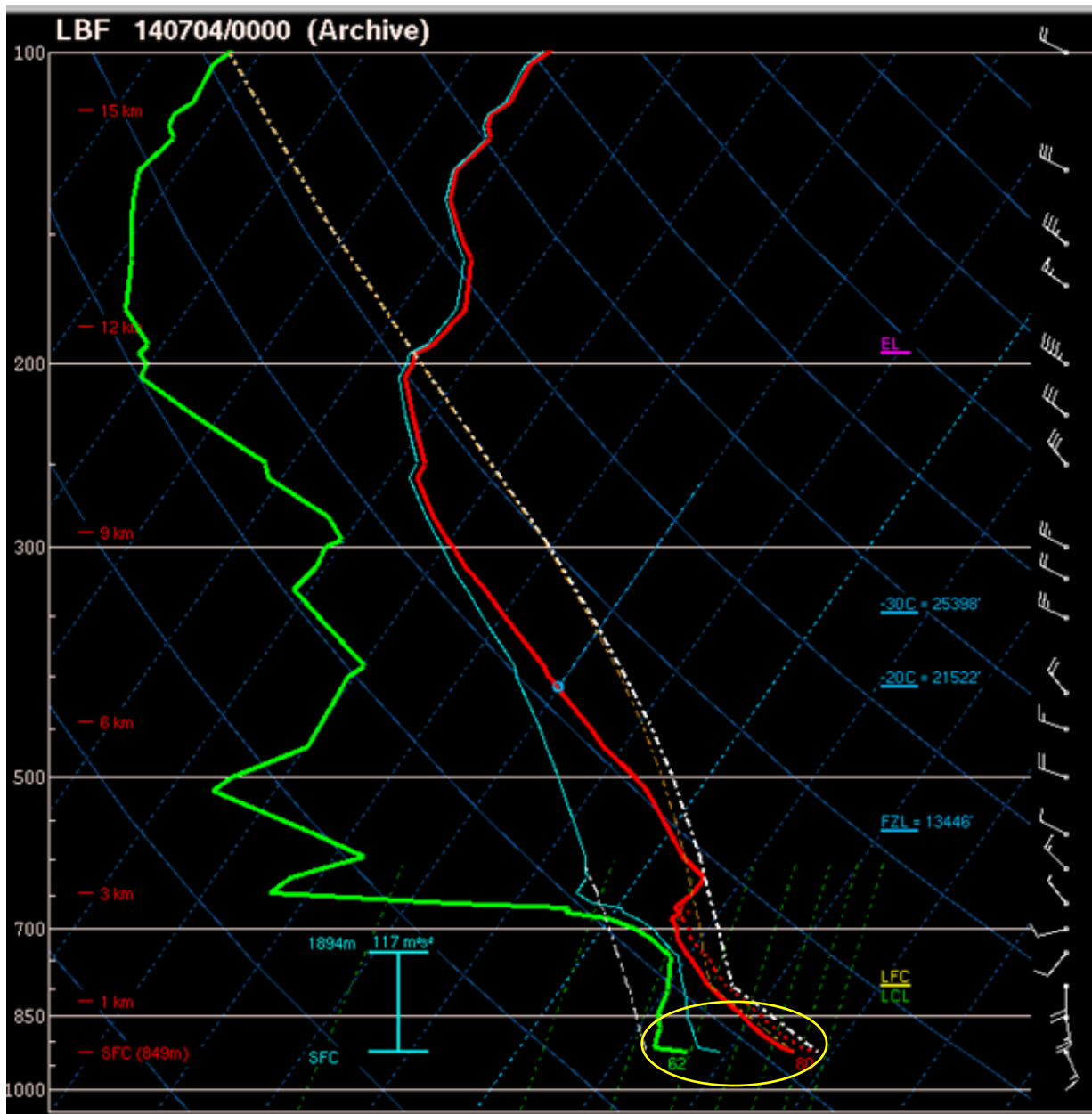
Was the storm elevated the whole time? Storm behavior suggested it was!

Quality of Observations Aloft?



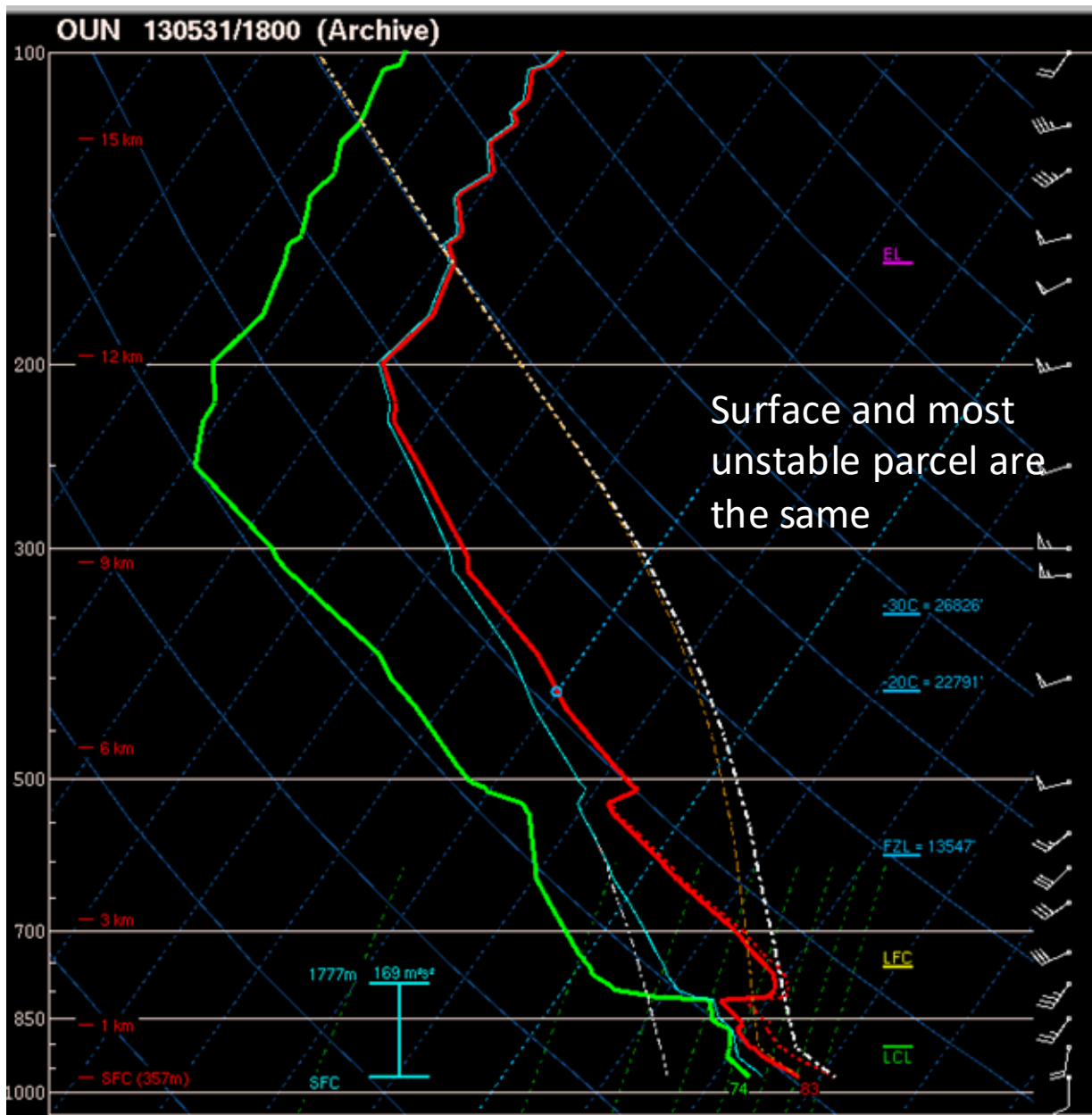


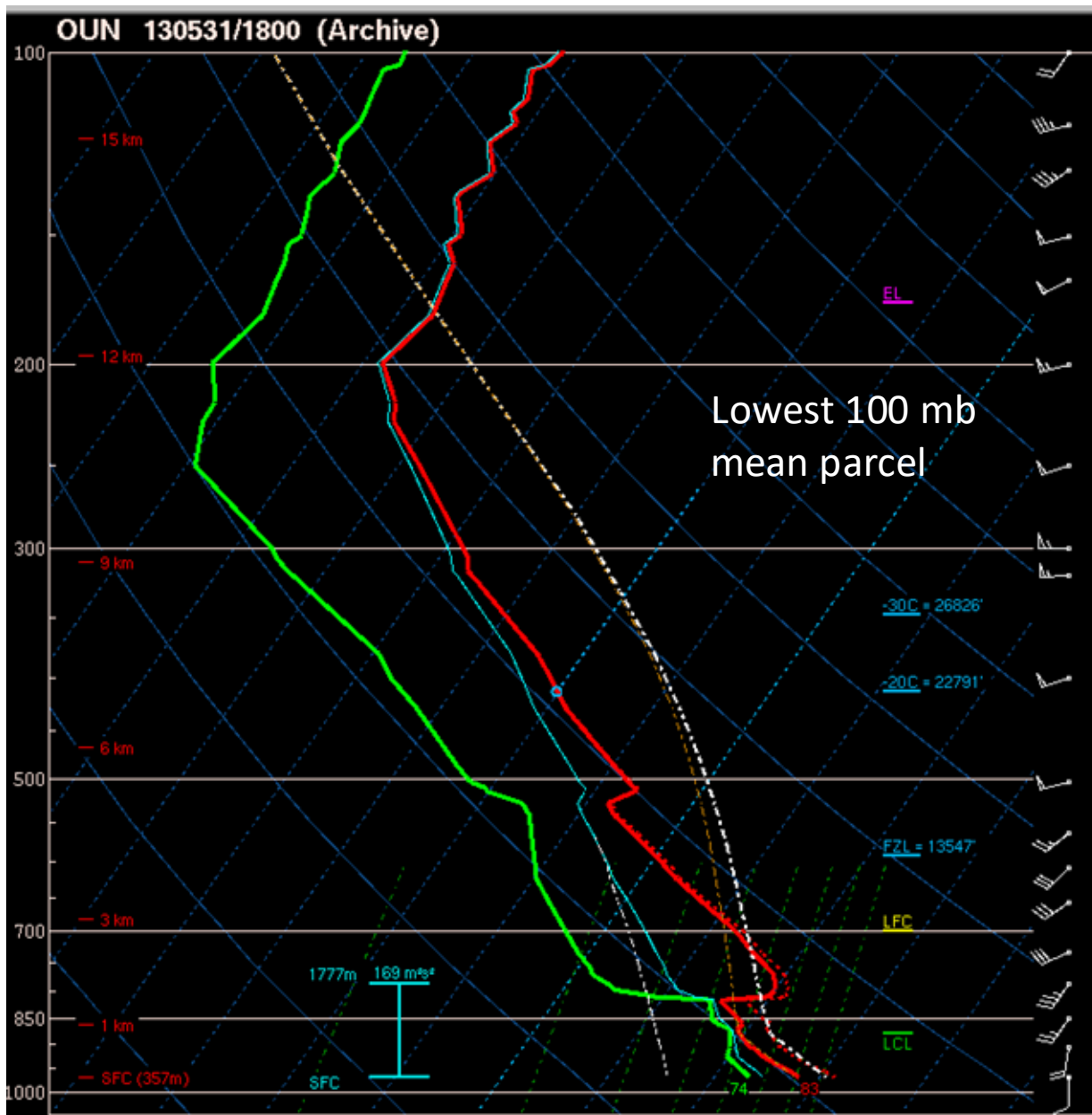




Understand the Data and Processes!

- Understanding the processes gives you a sound way to interpret weather data, and recognize errors
- If you don't know what you're using, how do you know if you're using it correctly?
 - Must consider data quality
- Focus on observations!



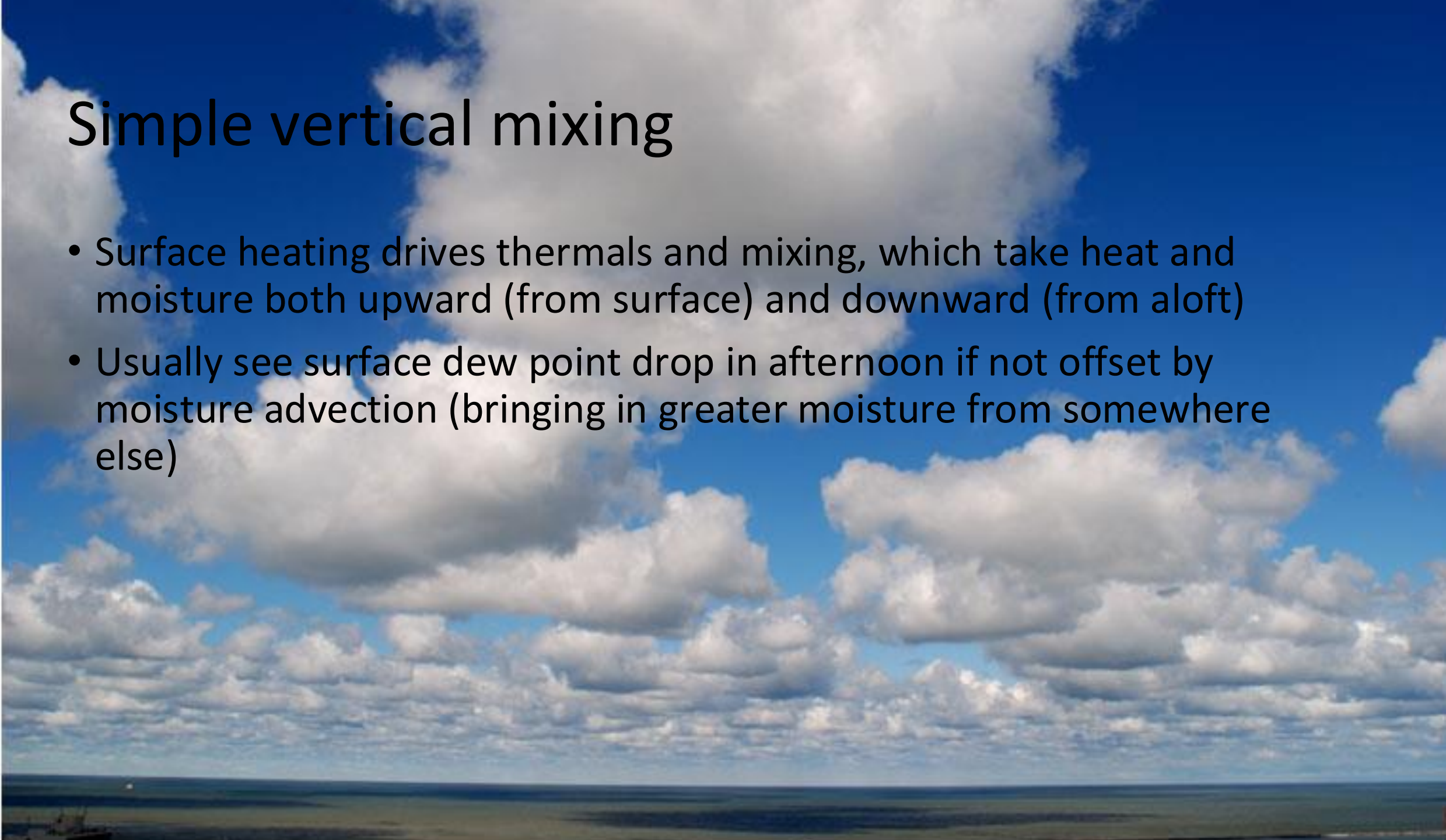


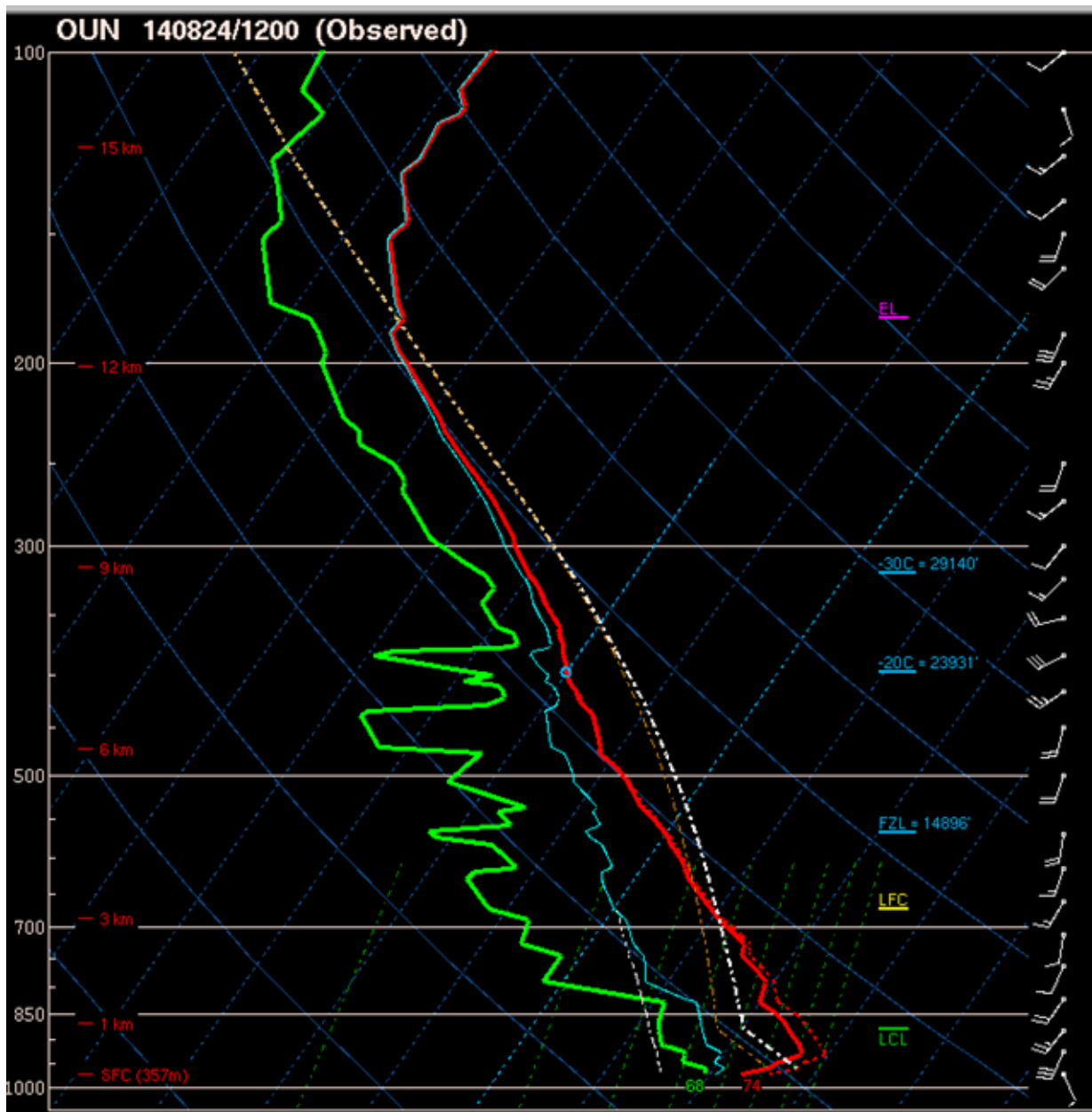
Always keep in mind what we don't know:

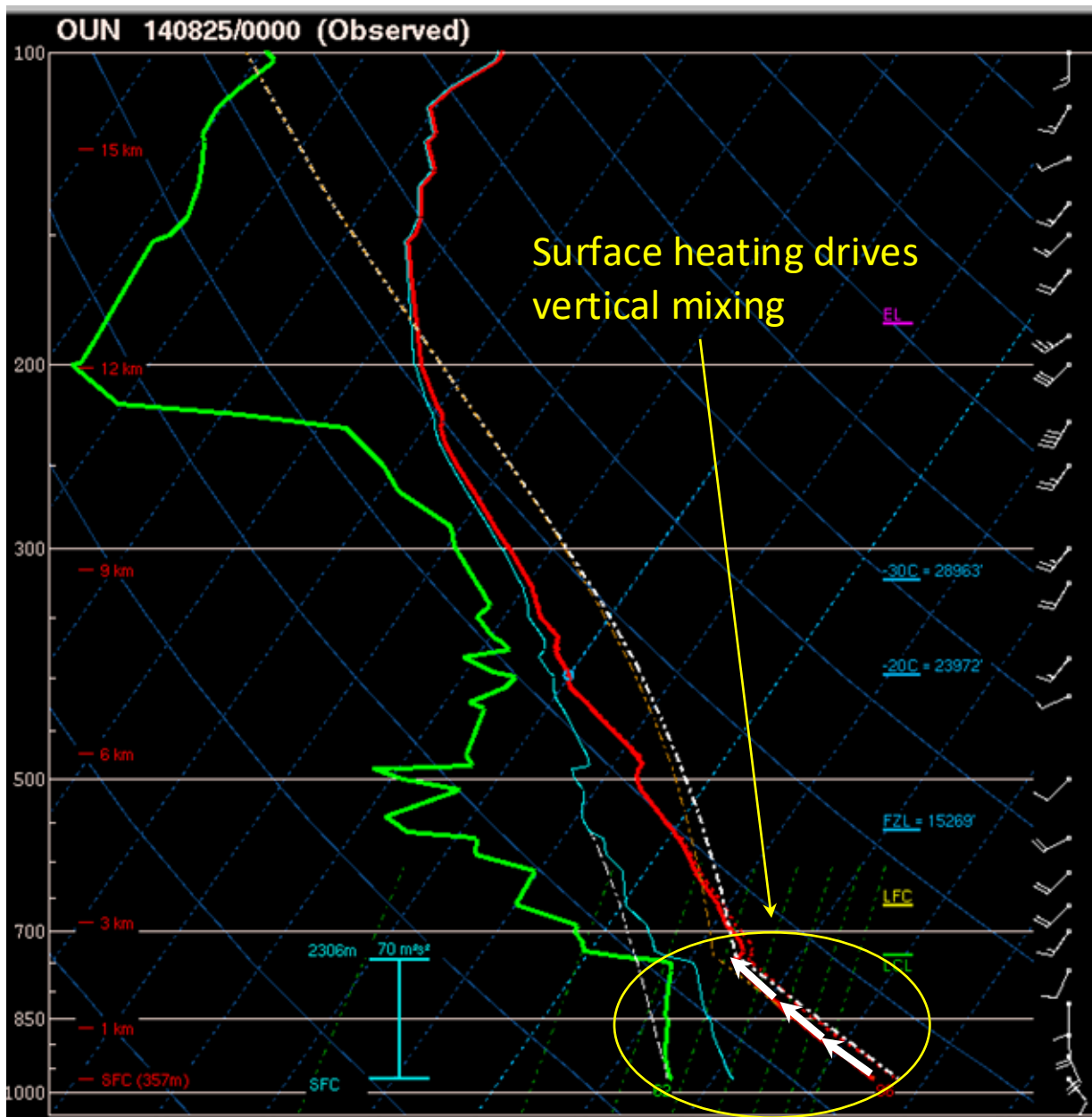
- Uncertainty in observations
 - “Good” measurements?
 - Do they represent what we're trying to forecast?
- Unknown details with lifted parcels
 - What is right layer to view?
 - What assumptions are valid, and which might be terribly wrong?
- Lots of room for error, but the concepts are useful!

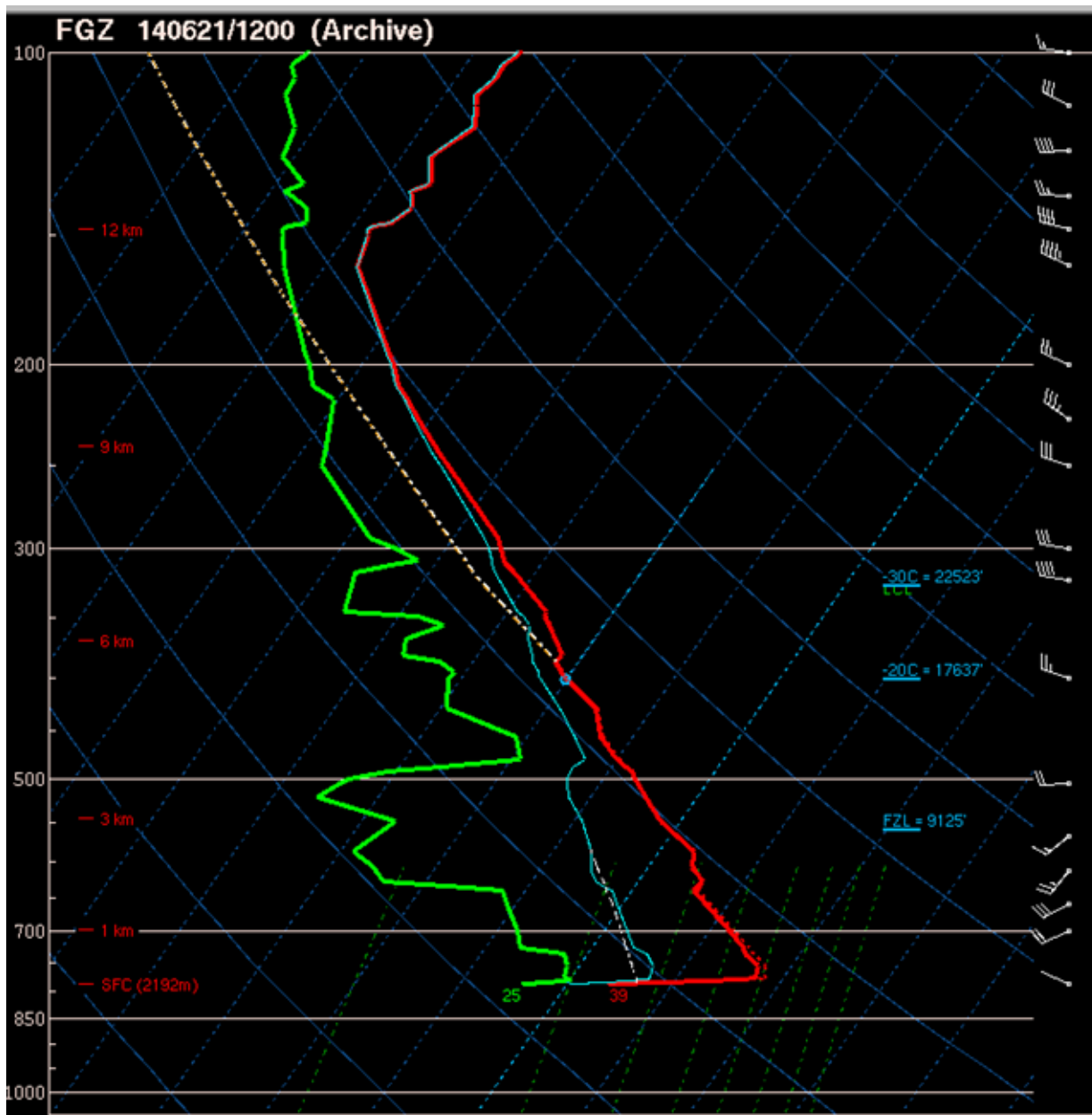
Simple vertical mixing

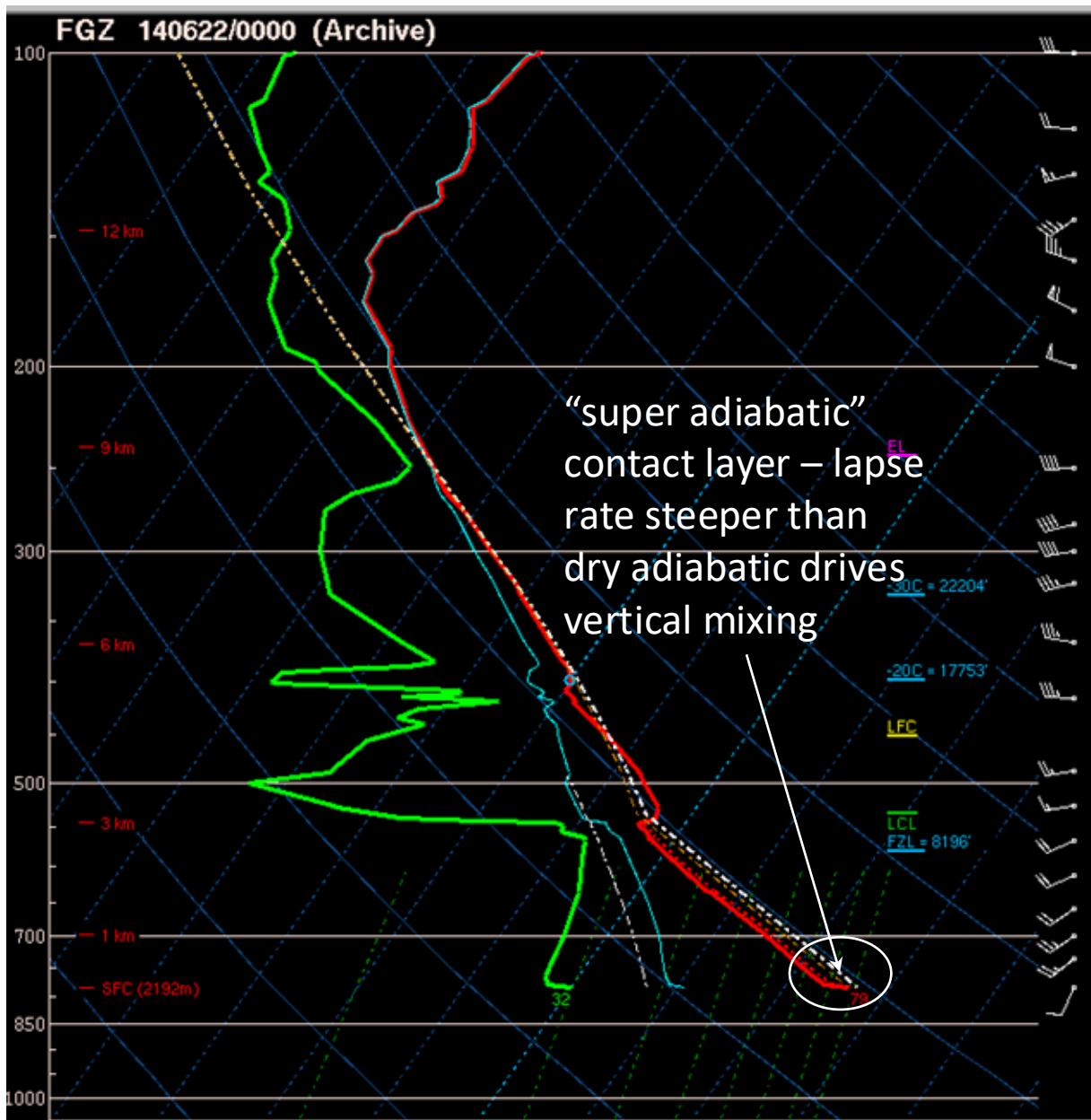
- Surface heating drives thermals and mixing, which take heat and moisture both upward (from surface) and downward (from aloft)
- Usually see surface dew point drop in afternoon if not offset by moisture advection (bringing in greater moisture from somewhere else)





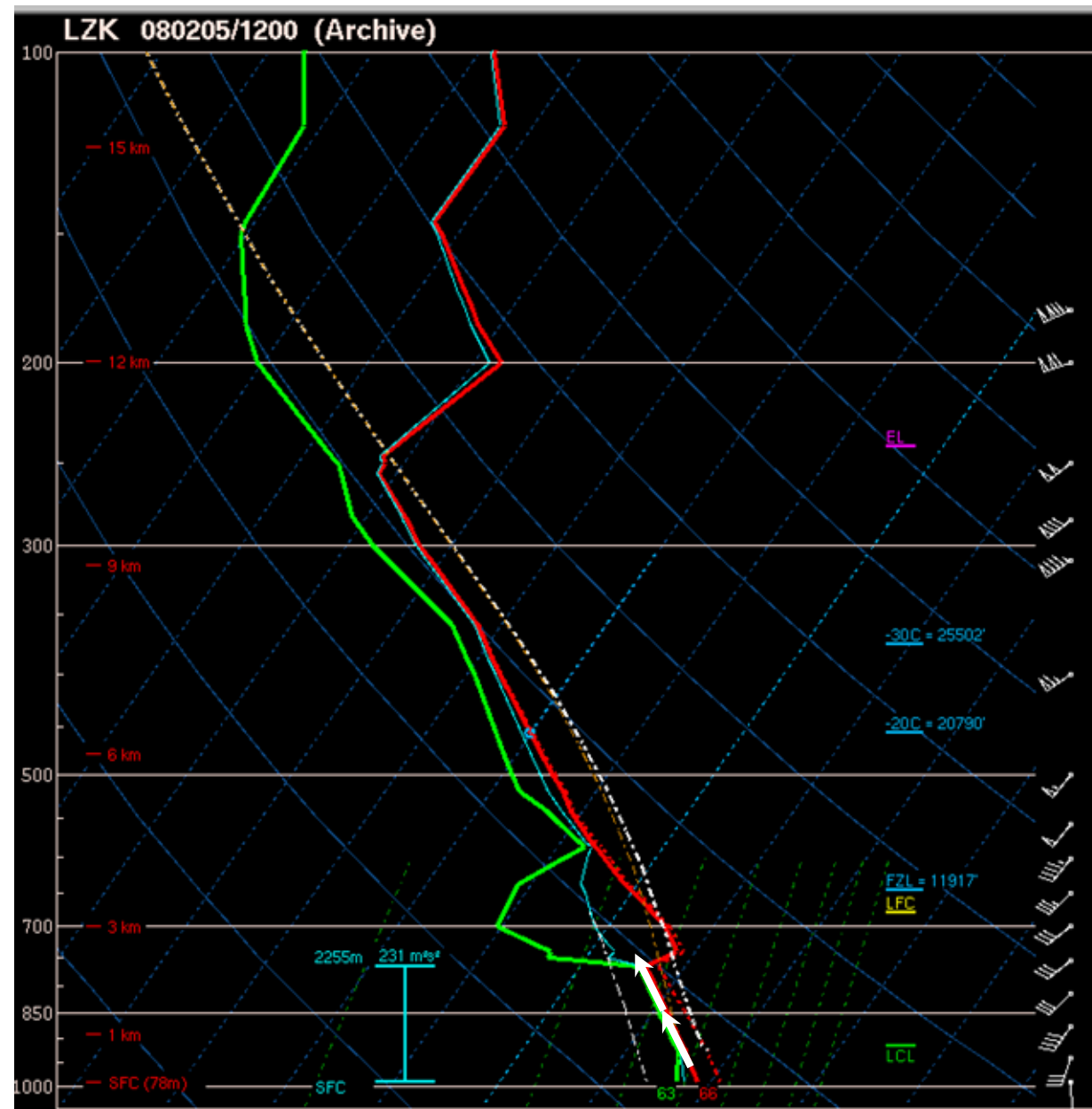


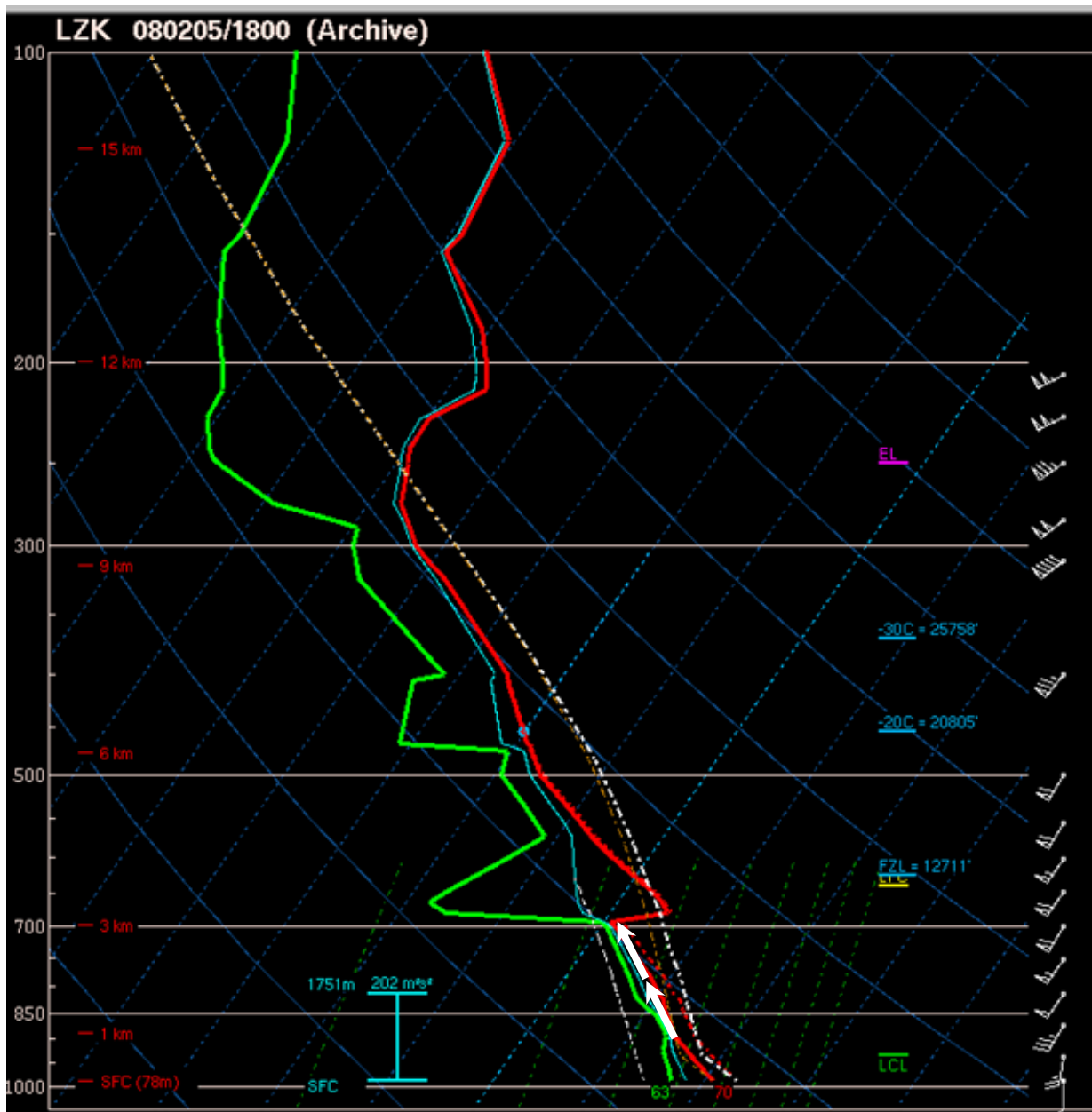


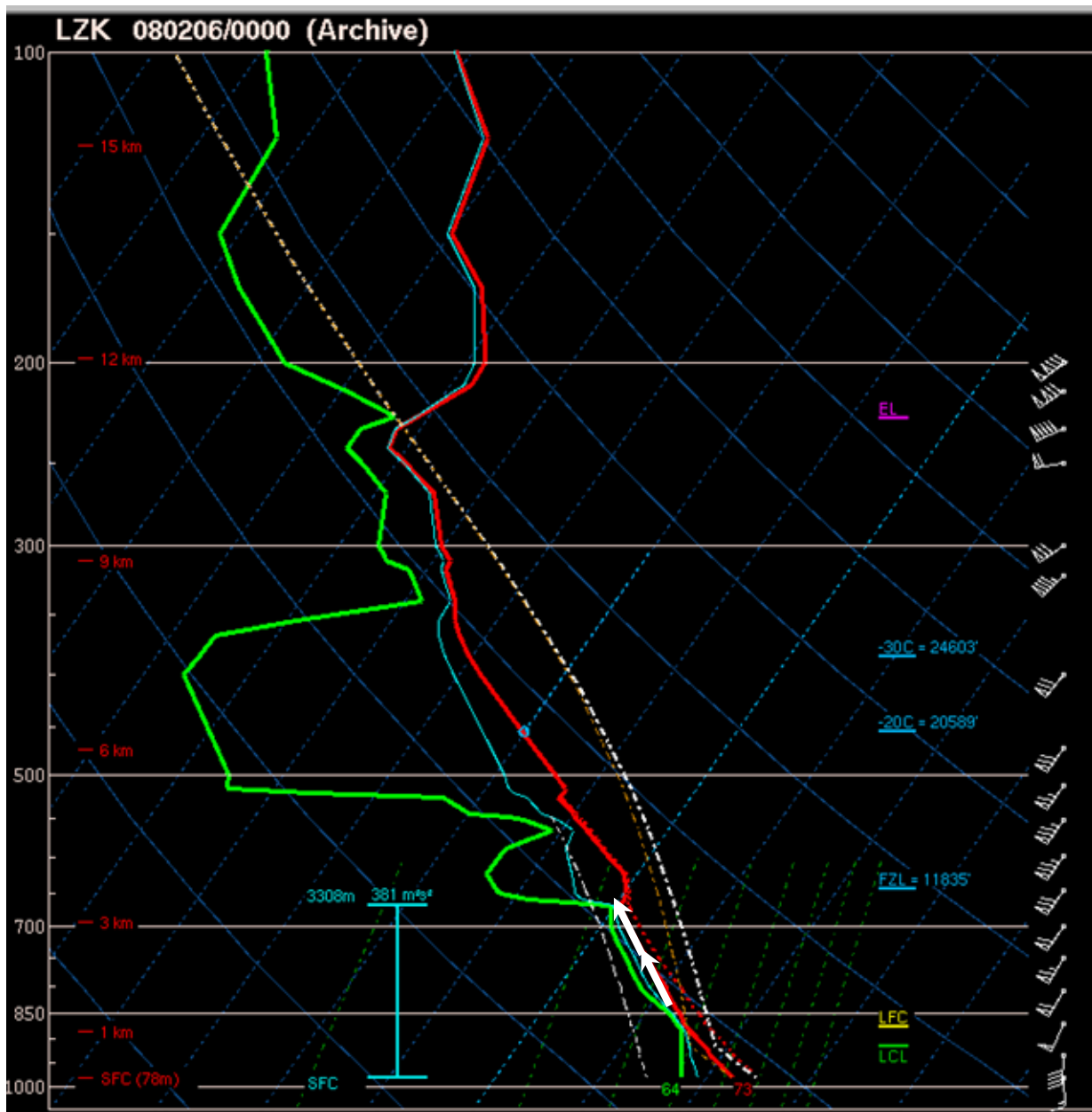


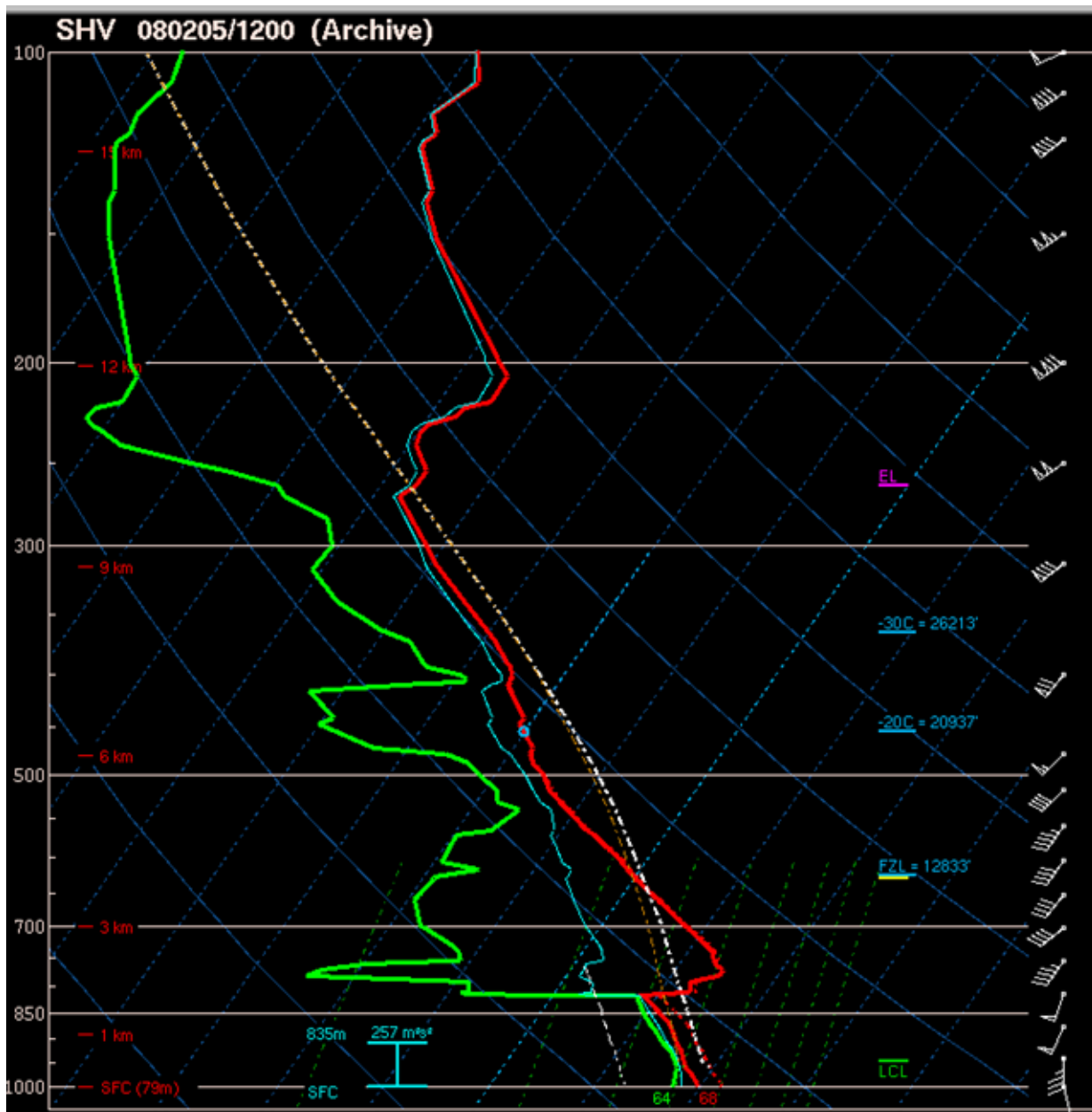
Impact of ascent and moisture advection

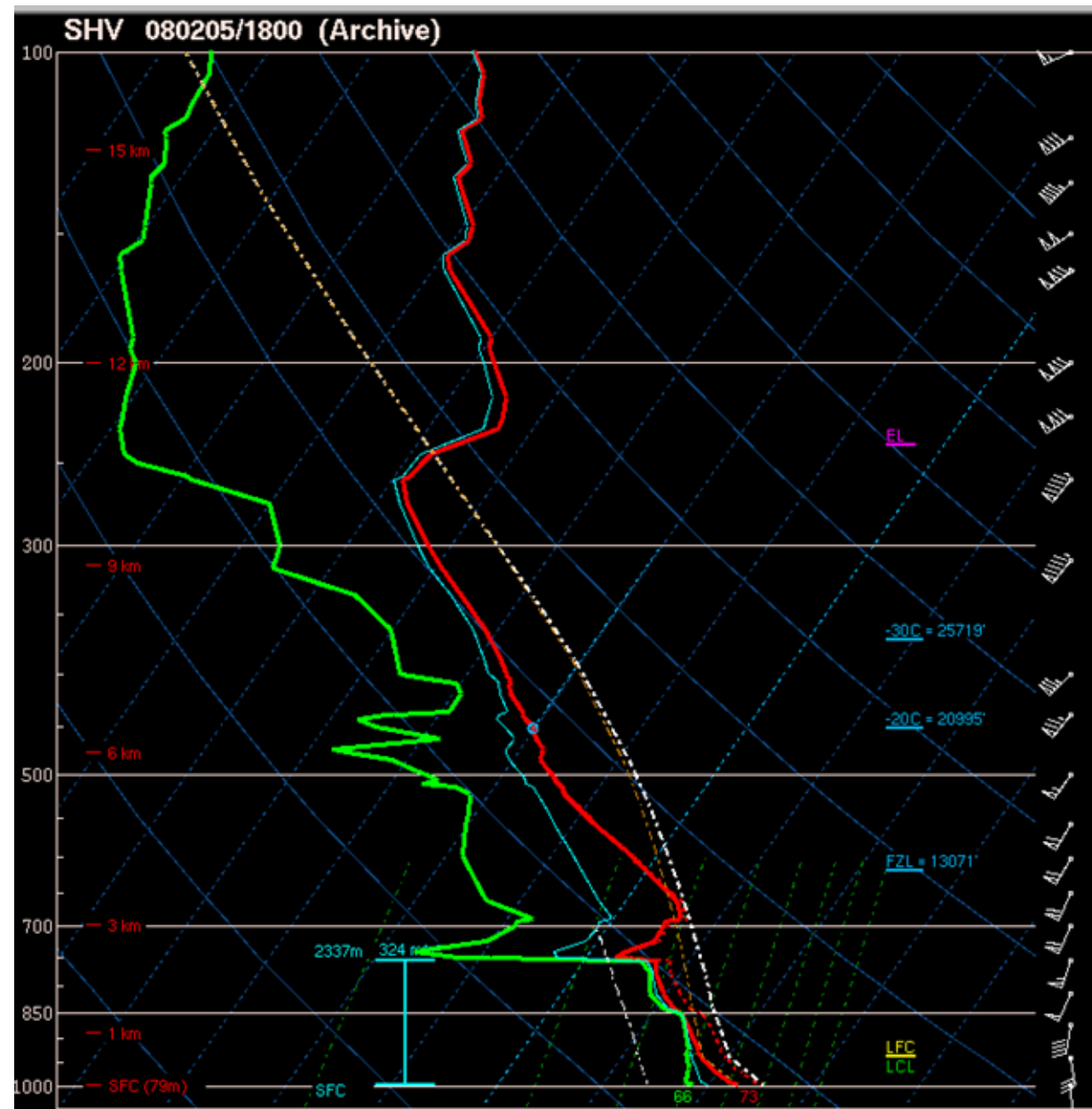
- See moist layer deepen faster than you would expect with just surface heating and mixing
- “Deep” moist layer and horizontal moisture advection both combat vertical mixing driven by surface heating
 - Can see moist layer deepen while dew points increase near surface

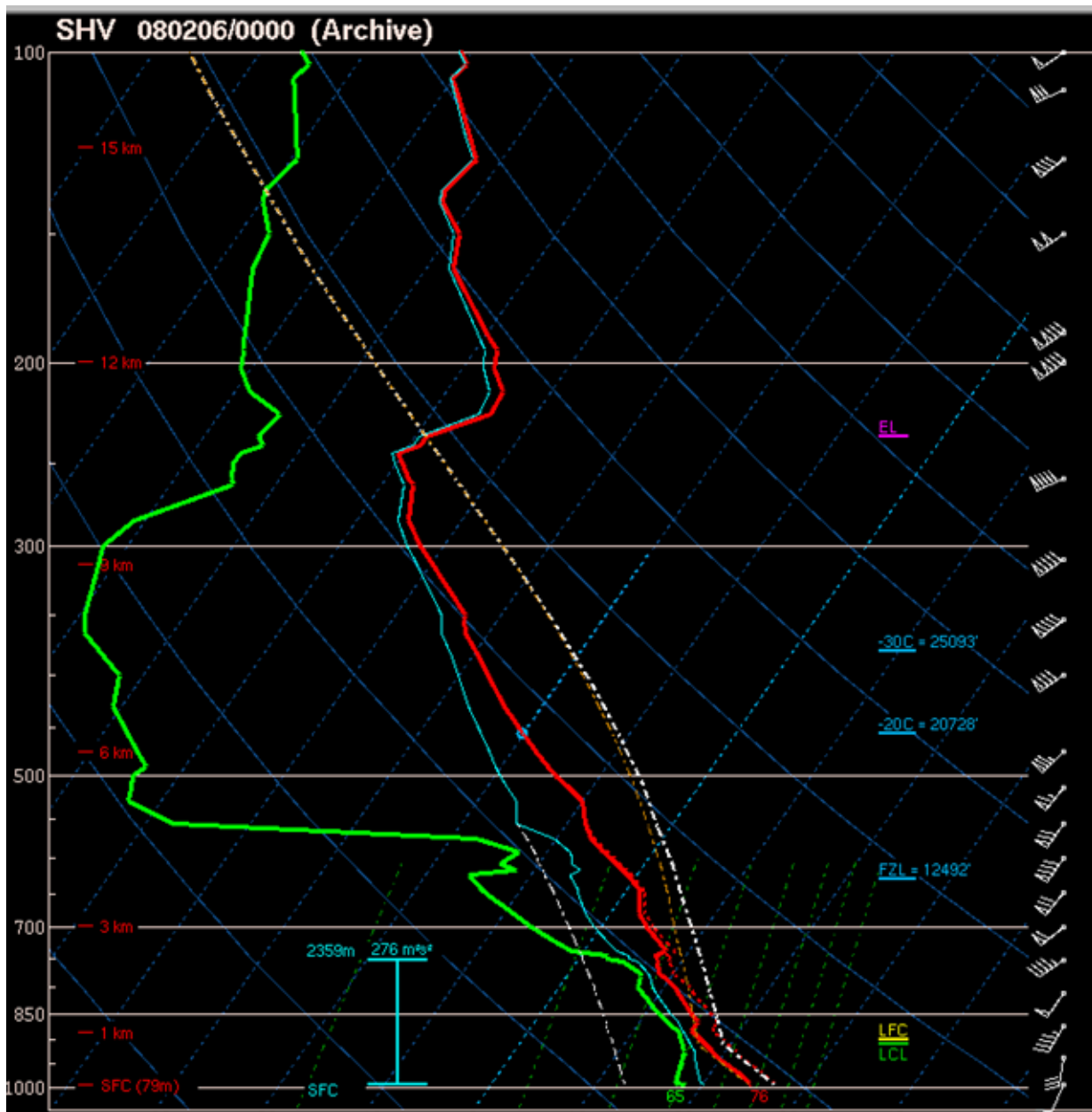












Sounding diagrams are used for...

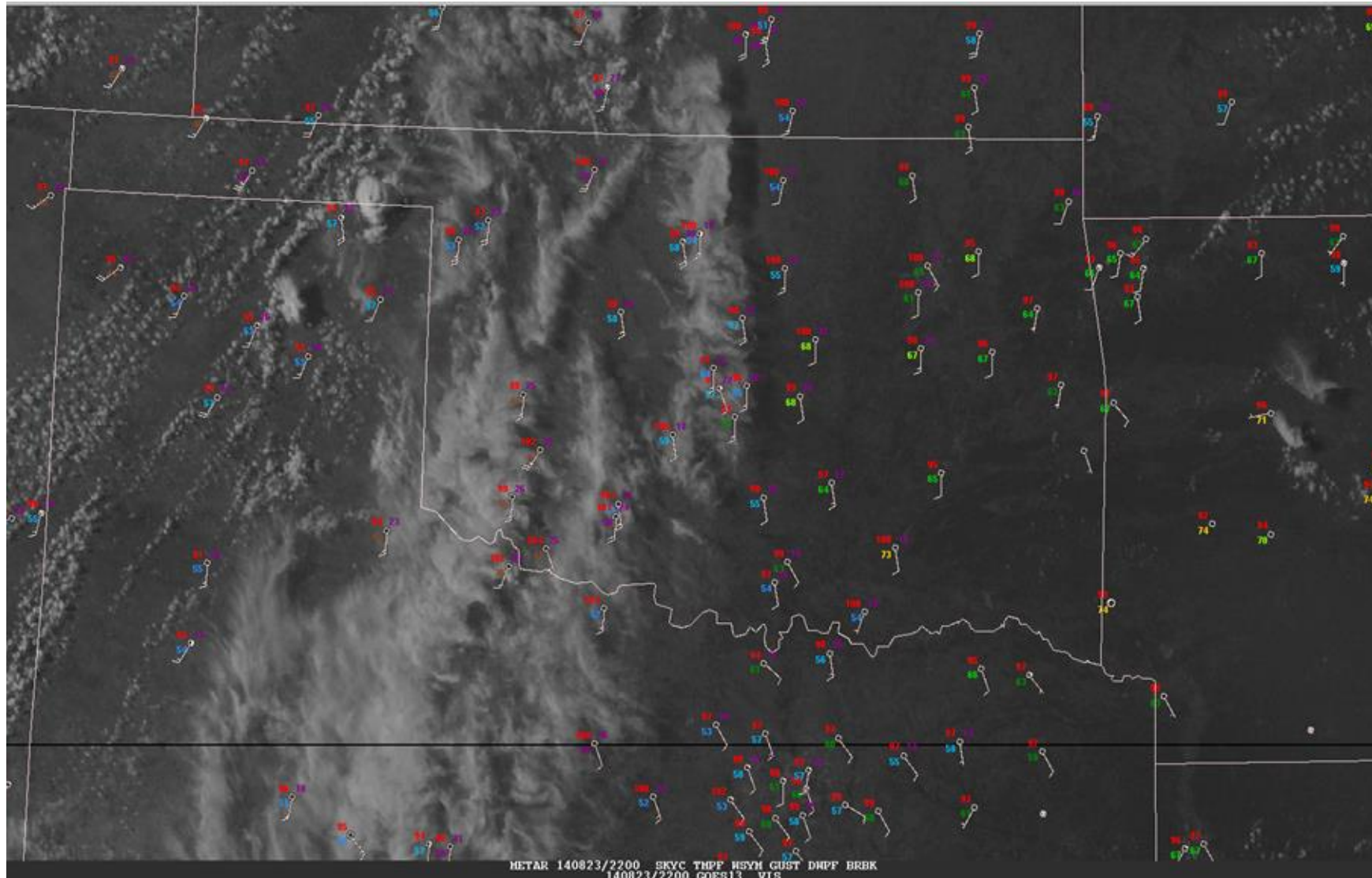
- Moisture and temperature profiles
- Estimates of CAPE, CIN, Lifted Index, etc.
 - Will storms form?
- Vertical wind shear (material on hodographs to come!)
 - What kind of storms will form?
- Many of your favorite thunderstorm parameters are based in these diagrams, and subject to the same errors and concerns!

Quality of Surface Observations?

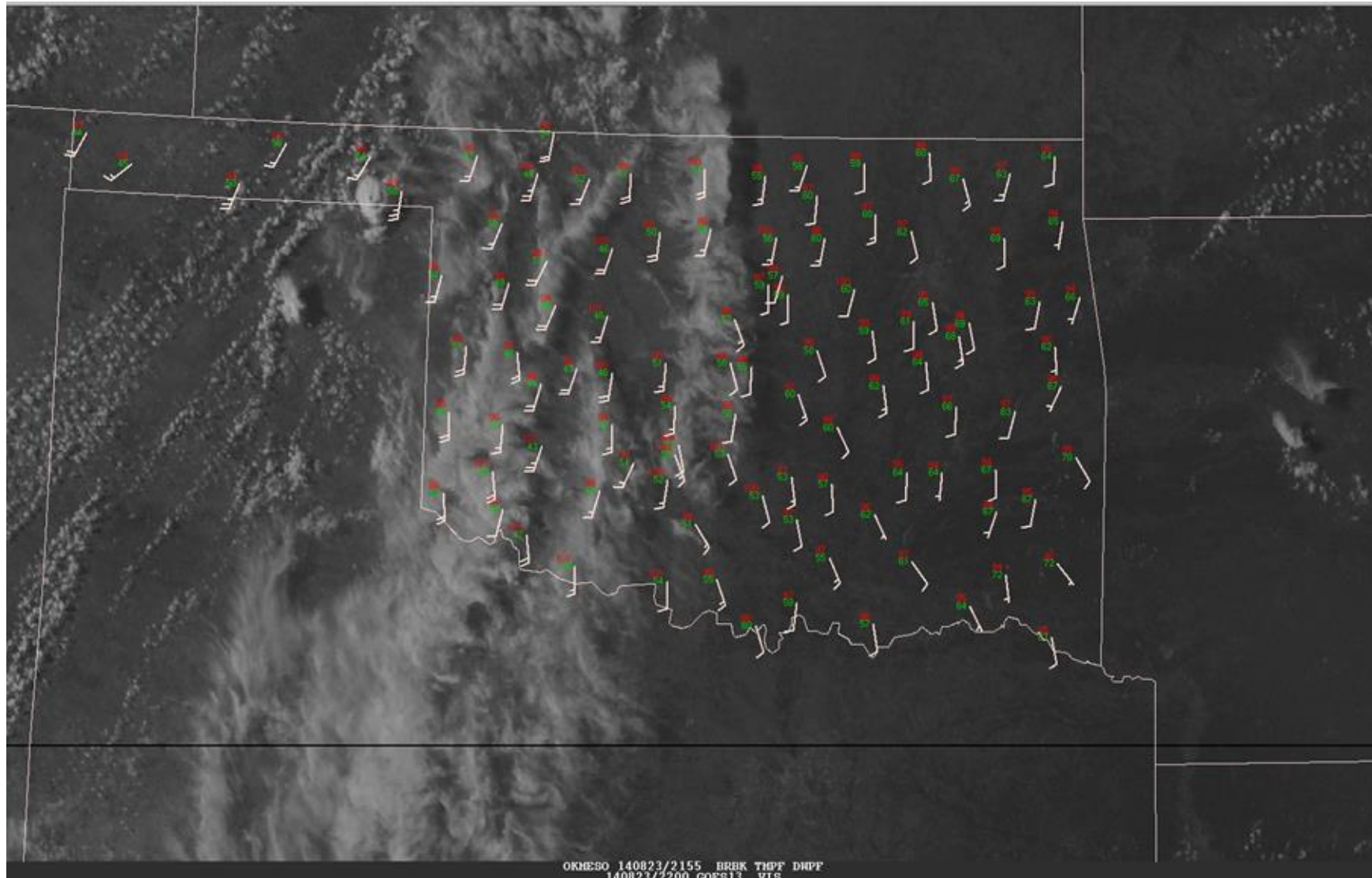


Courtesy of Oklahoma Mesonet

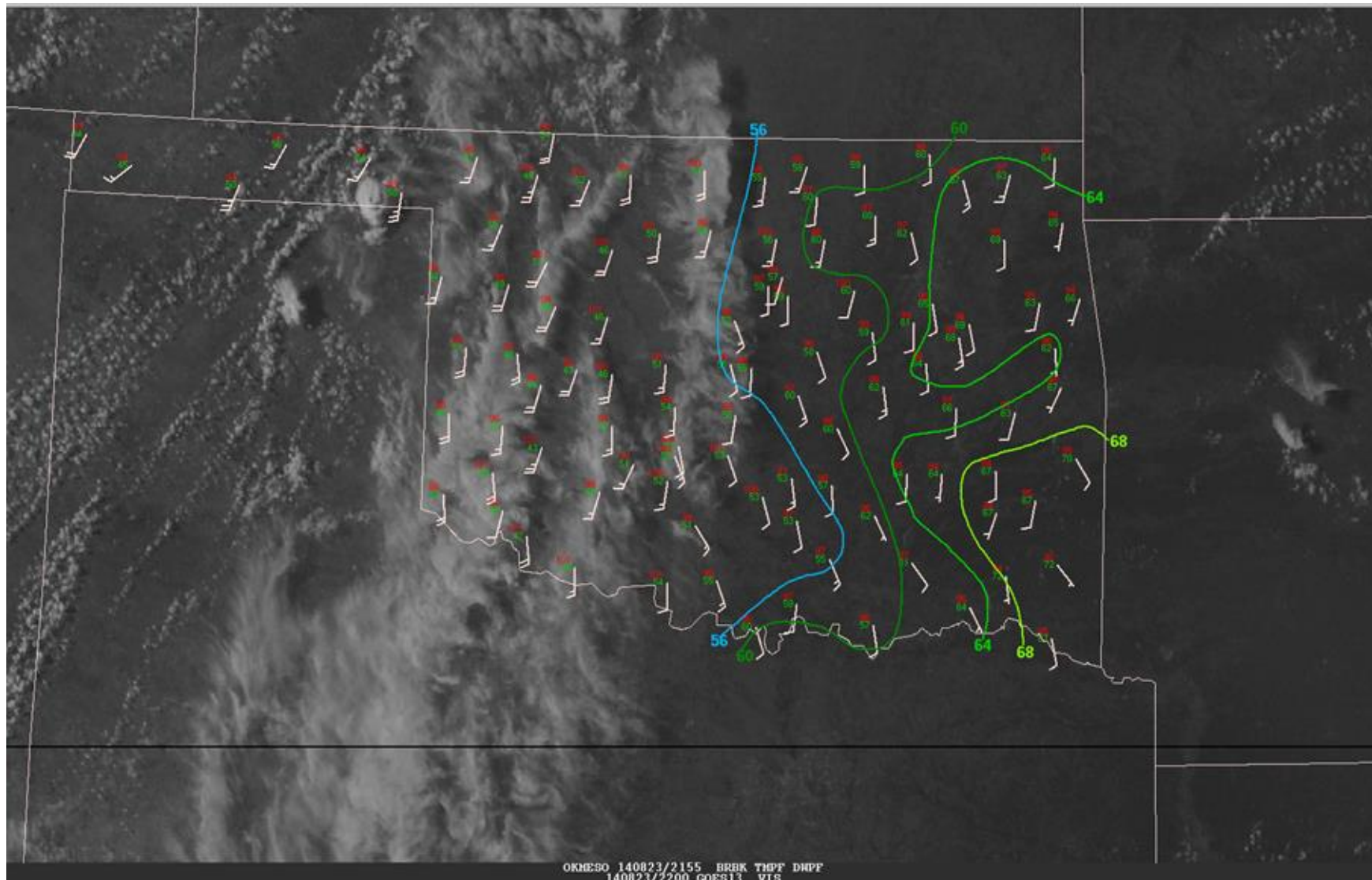
Standard surface observations



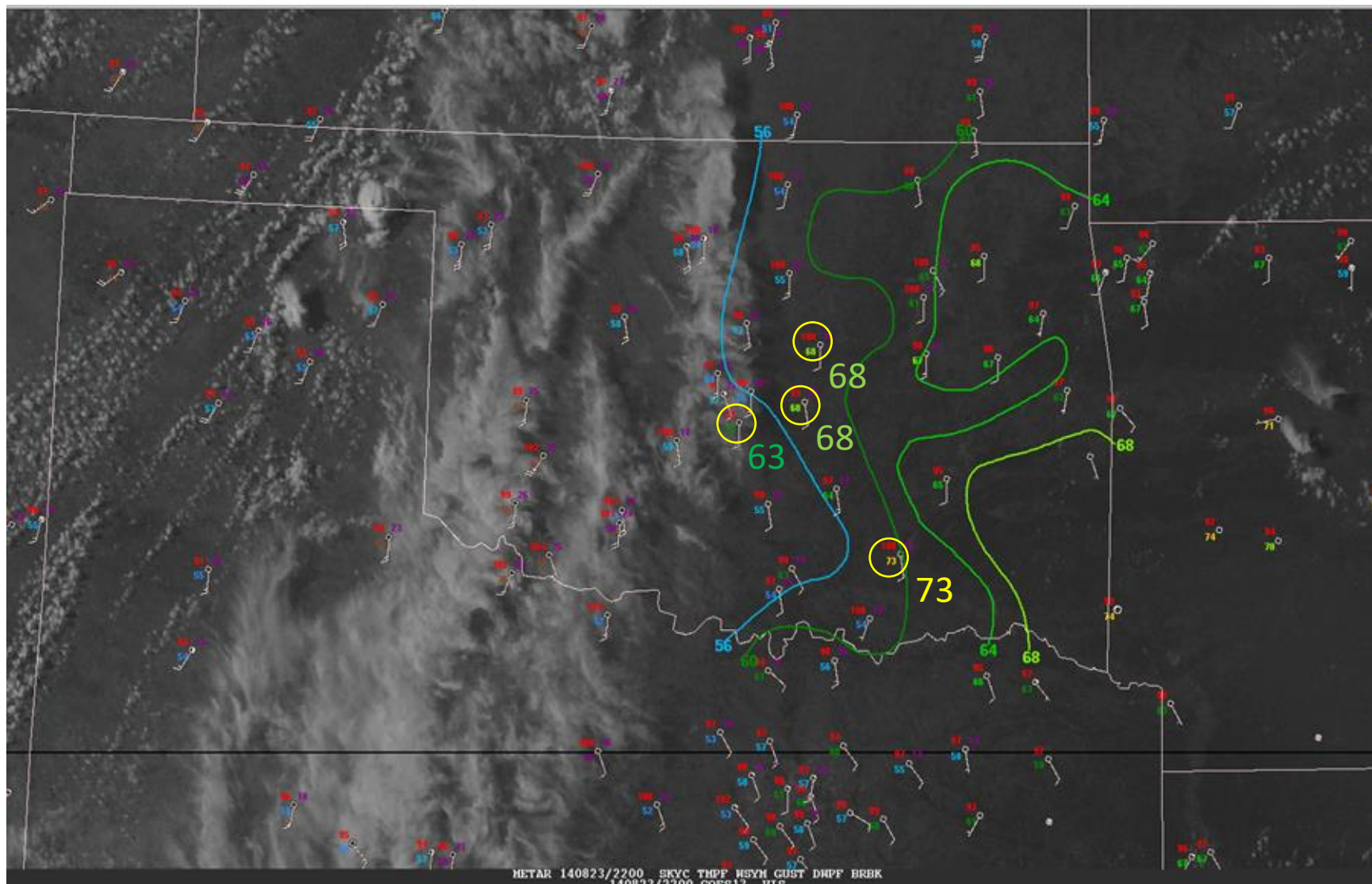
OK mesonet observations at the same time



Dew point analysis for OK mesonet observations



What do these sites have in common?



Parcel Theory

Material prepared by Tom Galarneau

Buoyancy

- Buoyancy is the upward force arising from the displacement of a fluid by another fluid or object (Archimedes' Principle)
 - The upward force is equal to the weight of the displaced fluid
 - Buoyancy is the key force for convection! (Supercells are more complicated...)

- Vertical momentum equation for convective scales goes as:

$$\frac{dw}{dt} = -\frac{1}{\rho} \frac{\partial p'}{\partial z} - g \frac{\rho'}{\rho} = -\frac{1}{\rho} \frac{\partial p'}{\partial z} + B \quad B = -g \frac{\rho'}{\rho} = \text{buoyancy}$$

If $\rho' > 0$, parcel is more dense than environment. $\therefore B < 0 \rightarrow \frac{dw}{dt} < 0$

If $\rho' < 0$, parcel is less dense than environment. $\therefore B > 0 \rightarrow \frac{dw}{dt} > 0$

- B controls the parcel acceleration. So, rising parcels can continue to rise for some time after becoming negatively buoyant (like overshooting top!)

Buoyancy

- Write buoyancy in terms of temperature since we measure that

Using ideal gas law: $B = -g \frac{\rho'}{\bar{\rho}} = g \left(\frac{T_v'}{\bar{T}_v} - \frac{p'}{\bar{p}} \right)$

For small mach number: $B = \left| \frac{p'}{\bar{p}} \right| \ll \left| \frac{T_v'}{\bar{T}_v} \right|$ $\therefore B = g \frac{T_v'}{\bar{T}_v} = g \frac{\theta_v'}{\bar{\theta}_v}$

- Reference state temperature is environment (temperature line on sounding)

$$\therefore B = g \left(\frac{T_{vp} - T_{venv}}{T_{venv}} \right)$$

T_{vp} is virtual temperature of air parcel

T_{venv} is virtual temperature of ambient environment

If $T_{vp} < T_{venv}$, parcel is colder than environment. $\therefore B < 0 \rightarrow \frac{dw}{dt} < 0$

If $T_{vp} > T_{venv}$, parcel is warmer than environment. $\therefore B > 0 \rightarrow \frac{dw}{dt} > 0$

Parcel theory

- We need to be able to determine whether a lifted parcel has buoyancy
- Convective available potential energy (CAPE) tells us the kinetic energy a parcel may gain due to buoyant acceleration

$$CAPE = \int_{LFC}^{EL} B \, dz$$

Vertical integration of buoyancy from LFC to EL.

Caveats: CAPE>0 does not guarantee convection.
Not all parcels have an LFC.

- Convective inhibition (CIN) tells is the work done by a parcel against stable stratification to reach its LFC

$$CIN = - \int_0^{LFC} B \, dz$$

Vertical integration of buoyancy from ground to EL.

Need to overcome CIN to trigger convection.

Theoretical Maximum Updraft Speed

- Parcel theory can be used to estimate w_{\max} from buoyancy alone
- Manipulate vertical momentum equation ($\frac{dw}{dt} = B$) for parcel theory

$$w_{\max} = \sqrt{2 * CAPE}$$

1000 J kg⁻¹ CAPE → 45 m s⁻¹ updraft (??)

STORM UVV (m/s)	
40 or less	Regular updraft
41 to 60	Strong updraft
61 to 80	Very strong updraft
81 or greater	Extreme updraft

- Theoretical updraft speeds based on CAPE seem large – what factors counteract buoyant accelerations for air parcels?

One can relate CIN to a vertical velocity, w_{lift} , or the estimated amount of lifting required to overcome the negative area by the following expression:

$$W_{\text{lift}} = \sqrt{2 * CIN}$$

Summary

- **Parcel theory overestimates updraft speed**
 - Vertical PGF limits updraft speed; significant for wide updrafts
 - Entrainment limits updraft speed; significant for narrow/tilted updrafts
 - Hydrometeor loading also limits updraft speed