Evolution of Lapse Rate, CAPE, and CIN



Figure 7.3

Soundings from Pittsburgh, PA, at 1200 UTC 31 May 1985 (blue) and 0000 UTC 1 June 1985 (black). Between 1200 and 0000 UTC, the mean tropospheric lapse rate has undergone significant changes, probably as the result of a number of large-scale processes acting in unison (e.g., insolation, lapse rate advection/differential temperature advection, stretching effect, etc.). The low-level moisture also increased by several g kg⁻¹ during the same 12 h period, primarily as a result of moisture advection. The increase in lapse rate and low-level moisture between 1200 and 0000 UTC led to the development of large CAPE (the lifted index decreased from +3 to -7; the lifted index is the temperature difference between the environmental 500 mb temperature and the temperature of an air parcel that has been lifted to 500 mb from the surface, with negative indices indicating that the lifted parcel is warmer than the environment at 500 mb). (Large vertical wind shear also accompanied the large instability; the worst tornado outbreak in the history of Pennsylvania was in progress not far from Pittsburgh at 0000 UTC.) (Markowski and Richardson 2010, Fig. 7.3)

What physical processes drive changes in lapse rate, CAPE, and CIN?



Radar summary maps from WSR-74 at Erie, PA



"This image, courtesy Greg Forbes via Paul Markowski, is from the radar that was atop the Walker Building, home of Penn State Meteorology Department, around 8pm EST. It shows a pronounced hook echo (center of photo) within the storm moving through Moshannon State Forest about 20 miles north of State College, Centre County."

• What physical processes alter the environment lapse rate?

Start with 1st Law of Thermodynamics



• What physical processes alter the environment lapse rate?

Start with 1st Law of Thermodynamics



$$q = C_p \left(\frac{\partial T}{\partial t} + \boldsymbol{v}_h \cdot \boldsymbol{\nabla}_h T + w \frac{\partial T}{\partial z} \right) - \frac{1}{\rho} \left(\frac{\partial p}{\partial t} + \boldsymbol{v}_h \cdot \boldsymbol{\nabla}_h p + w \frac{\partial p}{\partial z} \right) = C_p \left(\frac{\partial T}{\partial t} + \boldsymbol{v}_h \cdot \boldsymbol{\nabla}_h T + w \frac{\partial T}{\partial z} \right) + gw$$

• What physical processes alter the environment lapse rate?





$$q = C_p \left(\frac{\partial T}{\partial t} + \boldsymbol{v_h} \cdot \boldsymbol{\nabla_h} T + w \frac{\partial T}{\partial z} \right) - \frac{1}{\rho} \left(\frac{\partial \boldsymbol{v}}{\partial t} + \boldsymbol{v_h} \cdot \boldsymbol{\nabla_h} p + w \frac{\partial p}{\partial z} \right) = C_p \left(\frac{\partial T}{\partial t} + \boldsymbol{v_h} \cdot \boldsymbol{\nabla_h} T + w \frac{\partial T}{\partial z} \right) + gw$$
Relatively small,
assume hydrostatic
$$= -\rho g$$

• What physical processes alter the environment lapse rate?





$$q = C_p \left(\frac{\partial T}{\partial t} + \boldsymbol{v_h} \cdot \boldsymbol{\nabla_h} T + w \frac{\partial T}{\partial z} \right) - \frac{1}{\rho} \left(\frac{\partial T}{\partial t} + \boldsymbol{v_h} \cdot \boldsymbol{\nabla_h} p + w \frac{\partial p}{\partial z} \right) = C_p \left(\frac{\partial T}{\partial t} + \boldsymbol{v_h} \cdot \boldsymbol{\nabla_h} T + w \frac{\partial T}{\partial z} \right) + gw$$

$$\frac{\text{Differentiate with respect to } -z}{-\frac{\partial q}{\partial z}} = C_p \left[\frac{\partial}{\partial t} \left(-\frac{\partial T}{\partial z} \right) + \boldsymbol{v_h} \cdot \boldsymbol{\nabla_h} \left(-\frac{\partial T}{\partial z} \right) + w \frac{\partial}{\partial z} \left(-\frac{\partial T}{\partial z} \right) - \frac{\partial \boldsymbol{v_h}}{\partial z} \cdot \boldsymbol{\nabla_h} T - \frac{\partial w}{\partial z} \frac{\partial T}{\partial z} \right] - g \frac{\partial w}{\partial z}$$

• What physical processes alter the environment lapse rate?





$$q = C_p \left(\frac{\partial T}{\partial t} + \boldsymbol{v_h} \cdot \boldsymbol{\nabla_h} T + w \frac{\partial T}{\partial z} \right) - \frac{1}{\rho} \left(\frac{\partial T}{\partial t} + \boldsymbol{v_h} \cdot \boldsymbol{\nabla_h} p + w \frac{\partial p}{\partial z} \right) = C_p \left(\frac{\partial T}{\partial t} + \boldsymbol{v_h} \cdot \boldsymbol{\nabla_h} T + w \frac{\partial T}{\partial z} \right) + gw$$

$$\frac{\text{Differentiate with respect to } -z}{-\frac{\partial q}{\partial z}} = C_p \left[\frac{\partial}{\partial t} \left(-\frac{\partial T}{\partial z} \right) + \boldsymbol{v_h} \cdot \boldsymbol{\nabla_h} \left(-\frac{\partial T}{\partial z} \right) + w \frac{\partial}{\partial z} \left(-\frac{\partial T}{\partial z} \right) - \frac{\partial \boldsymbol{v_h}}{\partial z} \cdot \boldsymbol{\nabla_h} T - \frac{\partial w}{\partial z} \frac{\partial T}{\partial z} \right] - g \frac{\partial w}{\partial z}}$$

$$\frac{\partial^2 T}{\partial z^2} \text{ terms}$$

Substitute in definition for environment lapse rate
$$\gamma = -\frac{\partial T}{\partial z}$$
 and dry adiabatic lapse rate $\Gamma_d = \frac{g}{c_p}$
$$\frac{\partial \gamma}{\partial t} = -v_h \cdot \nabla_h \gamma - w \frac{\partial \gamma}{\partial z} + \frac{\partial v_h}{\partial z} \cdot \nabla_h T + \frac{\partial w}{\partial z} (\Gamma_d - \gamma) - \frac{1}{C_p} \frac{\partial q}{\partial z}$$

• What physical processes alter the environment lapse rate?





Expand full derivatives and assume hydrostatic conditions (OK for synoptic and mesoscale)

$$q = C_p \left(\frac{\partial T}{\partial t} + \boldsymbol{v_h} \cdot \boldsymbol{\nabla_h} T + w \frac{\partial T}{\partial z} \right) - \frac{1}{\rho} \left(\frac{\partial \gamma}{\partial t} + \boldsymbol{v_h} \cdot \boldsymbol{\nabla_h} p + w \frac{\partial p}{\partial z} \right) = C_p \left(\frac{\partial T}{\partial t} + \boldsymbol{v_h} \cdot \boldsymbol{\nabla_h} T + w \frac{\partial T}{\partial z} \right) + gw$$

$$\frac{\mathbf{Differentiate with respect to } -z}{-\frac{\partial q}{\partial z}} = C_p \left[\frac{\partial}{\partial t} \left(-\frac{\partial T}{\partial z} \right) + \boldsymbol{v_h} \cdot \boldsymbol{\nabla_h} \left(-\frac{\partial T}{\partial z} \right) + w \frac{\partial}{\partial z} \left(-\frac{\partial T}{\partial z} \right) - \frac{\partial \boldsymbol{v_h}}{\partial z} \cdot \boldsymbol{\nabla_h} T - \frac{\partial w}{\partial z} \frac{\partial T}{\partial z} \right] - g \frac{\partial w}{\partial z}$$

 $\frac{\text{Substitute in definition for environment lapse rate}}{\frac{\partial \gamma}{\partial t} = -v_h \cdot \nabla_h \gamma - w \frac{\partial \gamma}{\partial z} + \frac{\partial v_h}{\partial z} \cdot \nabla_h T + \frac{\partial w}{\partial z} (\Gamma_d - \gamma) - \frac{1}{C_p} \frac{\partial q}{\partial z}} \text{ Lapse rate tendency equation}}$

$$\frac{\partial \gamma}{\partial t} = -\boldsymbol{v}_{h} \cdot \boldsymbol{\nabla}_{h} \gamma - w \frac{\partial \gamma}{\partial z} + \frac{\partial \boldsymbol{v}_{h}}{\partial z} \cdot \boldsymbol{\nabla}_{h} T + \frac{\partial w}{\partial z} (\Gamma_{d} - \gamma) - \frac{1}{C_{p}} \frac{\partial q}{\partial z}$$

A B C D E F



Term A: local time rate of change of environment lapse rate









<u>Term B:</u> horizontal lapse rate advection



Figure 7.4

Analysis of the environmental temperature difference between 500 and 700 mb (K), which is a bulk measure of the midlevel lapse rate (a temperature difference of 27 K between 500 and 700 mb corresponds to an approximately dry adiabatic environmental temperature profile), revealing the presence of horizontal lapse rate advection. Wind barbs depict the mean wind in the 500–700 mb layer. Large lapse rates from the high terrain of northern Mexico and eastern New Mexico are being advected toward the southern Great Plains of the United States. This common warm season phenomenon leads to the formation of the elevated mixed layer that caps soundings in the Great Plains region. (Markowski and Richardson 2010, Fig. 7.4)



<u>Term B:</u> horizontal lapse rate advection

Positive lapse rate advection will contribute to increasing lapse rates

Typically the dominant term on synoptic scales



Figure 7.4

Analysis of the environmental temperature difference between 500 and 700 mb (K), which is a bulk measure of the midlevel lapse rate (a temperature difference of 27 K between 500 and 700 mb corresponds to an approximately dry adiabatic environmental temperature profile), revealing the presence of horizontal lapse rate advection. Wind barbs depict the mean wind in the 500–700 mb layer. Large lapse rates from the high terrain of northern Mexico and eastern New Mexico are being advected toward the southern Great Plains of the United States. This common warm season phenomenon leads to the formation of the elevated mixed layer that caps soundings in the Great Plains region. (Markowski and Richardson 2010, Fig. 7.4)



Nearly neutral layer above boundary layer in
Norman noon sounding – The layer originated from New Mexico plateau



Term C: vertical lapse rate advection

 $\frac{\partial \gamma}{\partial t}$

Α

Figure 7.5

Schematic thermodynamic diagram illustrating the effect of vertical lapse rate advection. The light blue arrows indicate dry adiabatic parcel displacements. At level z_1 , $\partial \gamma / \partial z < 0$, so when upward motion is imposed (w > 0 but $\partial w/\partial z = 0$, so that all of the parcels are displaced upward by the same distance) larger lapse rates are advected from below z_1 upward to z_1 , increasing the lapse rate there. Note that this process occurs adiabatically, so that cooling has occurred at z_1 in addition to increasing the lapse rate there. This cooling associated with upward motion is typically more important for cap removal and thunderstorm initiation than just the increasing lapse rate. For example, dry adiabatic large-scale ascent *always* leads to cooling (and cap weakening) when lapse rates are less than dry adiabatic, but lapse rate changes resulting from large-scale ascent may or may not be significant, depending on the initial γ , $\partial \gamma / \partial z$, and $\partial w / \partial z$. (Markowski and Richardson 2010, Fig. 7.5)



Positive lapse rate advection will contribute to increasing lapse rates

Α

In this case, lapse rates at level z1 increase as steeper lapse rates from below are advected upward

Can be order of magnitude larger than term B on mesoscale

Figure 7.5

Schematic thermodynamic diagram illustrating the effect of vertical lapse rate advection. The light blue arrows indicate dry adiabatic parcel displacements. At level z_1 , $\partial \gamma / \partial z < 0$, so when upward motion is imposed (w > 0but $\partial w/\partial z = 0$, so that all of the parcels are displaced upward by the same distance) larger lapse rates are advected from below z_1 upward to z_1 , increasing the lapse rate there. Note that this process occurs adiabatically, so that cooling has occurred at z_1 in addition to increasing the lapse rate there. This cooling associated with upward motion is typically more important for cap removal and thunderstorm initiation than just the increasing lapse rate. For example, dry adiabatic large-scale ascent *always* leads to cooling (and cap weakening) when lapse rates are less than dry adiabatic, but lapse rate changes resulting from large-scale ascent may or may not be significant, depending on the initial γ , $\partial \gamma / \partial z$, and $\partial w / \partial z$. (Markowski and Richardson 2010, Fig. 7.5)

$$\frac{\partial \gamma}{\partial t} = -\boldsymbol{v}_{h} \cdot \boldsymbol{\nabla}_{h} \gamma - w \frac{\partial \gamma}{\partial z} + \frac{\partial \boldsymbol{v}_{h}}{\partial z} \cdot \boldsymbol{\nabla}_{h} T + \frac{\partial w}{\partial z} (\Gamma_{d} - \gamma) - \frac{1}{C_{p}} \frac{\partial q}{\partial z}$$

A B C D E F

<u>Term D:</u> when combined with term B, this term represents differential temperature advection

$$\frac{\partial \boldsymbol{v}_{h}}{\partial z} \cdot \boldsymbol{\nabla}_{h} T - \boldsymbol{v}_{h} \cdot \boldsymbol{\nabla}_{h} \gamma = -\frac{\partial}{\partial z} (-\boldsymbol{v}_{h} \cdot \boldsymbol{\nabla}_{h} T)$$



Figure 7.6

Schematic thermodynamic diagram illustrating the effect of differential horizontal temperature advection (by the ageostrophic wind) on the lapse rate (temperature changes are indicated by the light blue arrows). Cold advection increases with height at level z_1 , which leads to an increase in the lapse rate at that level. This effect is really the same effect as illustrated in Figure 7.4.

$$\frac{\partial \gamma}{\partial t} = -\boldsymbol{v}_{h} \cdot \boldsymbol{\nabla}_{h} \gamma - w \frac{\partial \gamma}{\partial z} + \frac{\partial \boldsymbol{v}_{h}}{\partial z} \cdot \boldsymbol{\nabla}_{h} T + \frac{\partial w}{\partial z} (\Gamma_{d} - \gamma) - \frac{1}{C_{p}} \frac{\partial q}{\partial z}$$

A B C D E F

<u>Term D:</u> when combined with term B, this term represents differential temperature advection

$$\frac{\partial \boldsymbol{v}_{h}}{\partial z} \cdot \boldsymbol{\nabla}_{h} T - \boldsymbol{v}_{h} \cdot \boldsymbol{\nabla}_{h} \gamma = -\frac{\partial}{\partial z} (-\boldsymbol{v}_{h} \cdot \boldsymbol{\nabla}_{h} T)$$

Lapse rates will increase in situations where cold advection is increasing with height or warm advection is decreasing with height

In this case, lapse rates at level z1 increase in response to cold air advection increasing with height

Can be order of magnitude larger than term B on <u>mesoscale</u>



Figure 7.6

Schematic thermodynamic diagram illustrating the effect of differential horizontal temperature advection (by the ageostrophic wind) on the lapse rate (temperature changes are indicated by the light blue arrows). Cold advection increases with height at level z_1 , which leads to an increase in the lapse rate at that level. This effect is really the same effect as illustrated in Figure 7.4.



<u>Term E:</u> stretching effect on lapse rate

Horizontal convergence increases lapse rate Horizontal divergence decreases lapse rate Term = 0 when environment lapse rate is dry adiabatic ($\gamma = \Gamma_d$)

In this case, lapse rates at level z1 increase in response to convergence $(\frac{\partial w}{\partial z} > 0)$

Can be order of magnitude larger than term B on <u>mesoscale</u>



Figure 7.7

Schematic thermodynamic diagram illustrating the stretching effect on lapse rate. In this example, $\Gamma_d > \gamma$ and $\partial w/\partial z > 0$, therefore the lapse rate at level z_1 increases in time. The light blue arrows indicate dry adiabatic upward parcel displacements (because $\partial w/\partial z > 0$, the displacements increase with height).

$$\frac{\partial \gamma}{\partial t} = -\boldsymbol{v}_h \cdot \boldsymbol{\nabla}_h \gamma - w \frac{\partial \gamma}{\partial z} + \frac{\partial \boldsymbol{v}_h}{\partial z} \cdot \boldsymbol{\nabla}_h T + \frac{\partial w}{\partial z} (\Gamma_d - \gamma) - \frac{1}{C_p} \frac{\partial q}{\partial z}$$

A B C D E F

Term F: diabatic heating effect on lapse rate



In this case, in response to a diabatic heating maximum at level z1, lapse rates increase above and decrease below level z1.



Schematic thermodynamic diagram illustrating the effects of differential diabatic heating on lapse rate (temperature changes are indicated by the light blue arrows). The maximum latent heating occurs at level z_1 , where $\partial q/\partial z = 0$ and the lapse rate is unchanged. The lapse rate increases above the level of maximum heating ($z > z_1$) and decreases below the level of maximum heating ($z < z_1$).

Can be order of magnitude larger than term B on <u>mesoscale</u>

(Markowski and Richardson 2010, Fig. 7.8)

CAPE/CIN Changes Independent of γ Tendency

• CIN can be reduced and/or CAPE increased by:





CIN can be reduced by (a) large-scale rising motion, (b) low-level moistening (e.g., moisture advection), and (c) low-level warming (e.g., insolation), despite the fact that the CIN modifications may not be accompanied by lapse rate changes, at least not over a significant depth. In (a)–(c), the isotherms and isentropes are solid gray lines, the constant mixing ratio lines are gray dashed lines, the sounding and trajectory taken by an air parcel lifted from the surface are solid and dashed black curves, respectively, and the modified sounding and parcel trajectory are blue solid and dashed curves, respectively. In (a), for clarity, only the temperature profile has been modified (the moisture profile has not been modified in accordance with the vertical motion that has been imposed in the layer of the capping inversion). Note that (b) and (c) are also accompanied by increases in CAPE. Conversely, CIN is augmented by large -scale descent, boundary layer cooling (although this would typically not occur without a concurrent stabilization of the lapse rate), and boundary layer drying (not shown). (Markowski and Richardson 2010, Fig. 7.9)



Shreveport soundings

Quality of Surface Observations?

Courtesy of Oklahoma Mesonet

Standard surface observations



Automated Surface/Weather Observing Systems (ASOS/AWOS)

OK mesonet observations at the same time



Dew point analysis for OK mesonet observations



What do these sites have in common?



Quality of Observations Aloft?







Understand the Data and Processes!

- Understanding the processes gives you a sound way to interpret weather data, and recognize errors
- If you don't know what you're using, how do you know if you're using it correctly?
 - Must consider data quality
- Focus on observations!