

1D advection exercises:

Download 1DAdvection_template.ipynb from class materials of March 5.

1. Complete the code for advection in x direction using the if else format (a function using the and `np.absolute(u)` form is provided)
2. Run the code with `u = 10.0` and `dt=4.0s`
3. Rerun the code by setting `u[:, :, :] = 5.0`
4. Rerun the code by setting `u[:, :, :] = 12.0`
5. Change the advection code to always use `i-1` and `i` in the advection term and rerun the code by setting `u[:, :, :] = -10.0` and `-5.0`.

2D advection exercises:

Download 1DAdvection_template.ipynb from class materials of March 5

Add similar codes for vertical theta advection. Set periodic boundary conditions in the vertical also, following the following code for horizontal boundaries:

```
theta[t+1, :, 0] = theta[t+1, :, nx-2]
theta[t+1, :, nx-1] = theta[t+1, :, 1]
```

1. Run the code by setting `u[:, :, :] = 0.0` and `w[:, :, :] = 10.0`
2. Run the code by setting `u[:, :, :] = 10.0` and `w[:, :, :] = 10.0`. Set `dt` so that the Courant number is no greater than $1/\sqrt{2}$.

2D cloud model exercises:

Download 2D_Cloud_template.ipynb, HotBubble.nc and ColdBubble.nc from class materials of March 5 and upload to `jupyter.lib.ou.edu`.

This template has codes to specify 5 K hot bubble or -5 K cold bubble (initial theta perturbation).

- a) You need to add codes to do advection for theta and vort (vorticity).
- b) You need to add codes to calculate buoyancy vorticity generation term.
- c) You need to add codes to solve stream function Poisson equation.
- d) You need to add codes to calculate `u` and `w` from stream function.

Precalculated solutions can be read in (the template code is set up to read in `u`, `w` and stream function) from HotBubble.nc or ColdBubble.nc that contains solutions of all fields at every time step at `dt = 2.0`. For 5 K or -5 K bubbles respectively, do the following:

1. Run the code without any change and examine the animation.

2. Complete step a) above and re-run – examine the solution. Is the bubble rising/sinking now?
3. Add codes to calculate u and w from stream function read in from the *.nc file, and rerun. Is the solution changed?
4. Uncomment `streamf[t+1,:,:] = poisson_fft(vort[t+1,:,:], invlapl)` to call provided FFT Poisson solver to solve for stream function from predicted vorticity. Rerun – how is the solution?
5. Complete function `poisson2d()` to solve the Poisson equation using SOR method to be discussed in class and re-run.

Boundary conditions for the 2D cloud model

We assume a closed model domain of $2560 \times 2560 \text{ m}^2$ in x and z directions.

The x boundaries are at $x = 0$ and $x = \text{lenx}$.

The z boundaries are at $z = 0$ and $z = \text{lenz}$.

The number of grid points in x and z are nx and nz , respectively.

$$dx = \text{lenx}/(nx - 1), dz = \text{lenz}/(nz - 1).$$

If using the FFT version of Poisson solver, preferred values of nx and nz are $2^n + 1$.

Suggested choices for nx and nz are 65, 129 and 257 for low, medium and high resolution runs, corresponding to $dx, dz = 40, 20$ and 10 m . Remember, arrays of shape (nx, nz) have indices going from 0 to $nx-1$, and 0 to $nz-1$.

The domain has rigid wall boundaries, therefore velocity components normal to the boundaries are zero:

$$u(x = 0) = u(x = \text{lenx}) = 0,$$

$$w(z = 0) = w(z = \text{lenz}) = 0.$$

We also assume the velocity components parallel to the boundaries have zero normal gradient, therefore

$$w(x = 0) = w(x = dx)$$

$$w(x = \text{lenx}) = w(x = \text{lenx} - dx)$$

$$u(z = 0) = u(z = dz)$$

$$u(z = \text{lenz}) = u(z = \text{lenz} - dz).$$

For stream function, the boundary condition is $\psi = 0$ at all boundaries.

For vorticity η and potential temperature θ' , we apply zero normal gradient boundary conditions at all boundaries.